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## Third Semester B.E. Degree Examination, Dec.2023/Jan.2024 Engineering Electromagnetics

Max. Marks: 80

**Note: Answer any FIVE full questions, choosing ONE full question from each module.**

### Module-1

- 1 a. State vector form of Coloumb's law of force between two point charges and indicate the units of the quantities in the equation. (04 Marks)
- b. Let a point charge  $Q_1 = 25\text{nC}$  be located at  $A(4, -2, 7)$  and charge  $Q_2 = 60\text{nC}$  be at  $B(-3, 4, -2)$ . Find  $\vec{E}$  at  $C(1, 2, 3)$  and find the direction of  $\vec{E}$ . (10 Marks)
- c. Define Electric Field intensity due to number of point charge in a vector form. (02 Marks)

**OR**

- 2 a. Derive an expression for the electric field intensity due infinite line charge. (06 Marks)
- b. Define electric flux density. Find  $\vec{D}$  in Cartesian co-ordinate system at a point  $p(6, 8, -10)$  due to a point charge of  $40\text{mC}$  at the origin and a uniform line charge of  $\rho_L = 40\mu\text{C/m}$  on the z-axis. (10 Marks)

### Module-2

- 3 a. State and prove Gauss law and derive first Maxwell's equations from it. (05 Marks)
- b. Given a  $60\mu\text{C}$  point charge located at the origin. Find the total electric flux passing through the closed surface defined by  $\rho = 26\text{ cm}$  and  $z = \pm 26\text{ cm}$ . (04 Marks)
- c. State and prove the Divergence theorem. (05 Marks)
- d. Given the electric flux density  $D = 0.3r^2\hat{a}_r$ ,  $\text{nc/m}^2$  in free space. Find  $E$  at the point  $P(r = 2, \theta = 25^\circ, \phi = 90^\circ)$ . (02 Marks)

**OR**

- 4 a. Prove that the work done in moving a charge in the electric field is 
$$W = -Q \int_{\text{initial}}^{\text{final}} E \cdot d\ell.$$
 (06 Marks)
- b. Calculate the work done in moving a  $4\text{C}$  charge from  $B(1, 0, 0)$  to  $A(0, 2, 0)$  along the path  $y = 2 - 2x, \tau = 0$  in the field  $E = (5x\hat{a}_x + 5y\hat{a}_y)\text{ V/m}$ . (05 Marks)
- c. Show that  $\nabla \cdot \mathbf{J} = -\frac{\partial \rho_v}{\partial t}$  with usual notations. (05 Marks)

### Module-3

- 5 a. State and explain Biot-Savart's law. (05 Marks)
- b. Two parallel conducting discs are separated by distance  $5\text{mm}$  at  $z = 0$  and  $z = 5\text{mm}$ . If  $v = 0$  at  $z = 0$  and  $v = 100\text{v}$  at  $z = 5\text{mm}$ , find the charge densities on the discs. (05 Marks)
- c. Using Poisson's equation obtain the expression for the junction potential in a p-n junction. (06 Marks)

**OR**

- 6 a. Derive Laplace and Poisson's equation starting from the Gauss's law and also write Laplace's equation in Cartesian, cylindrical and spherical coordinate system. (08 Marks)
- b. Evaluate both sides of the Stoke's theorem for the field  $\vec{H} = 6xy \hat{a}_x - 3y^2 \hat{a}_y$  A/m and the rectangular path around the region  $2 \leq x \leq 5$ ,  $-1 \leq y \leq 1$ ,  $z = 0$  let the positive direction of  $\vec{ds}$  be  $\hat{a}_z$ . (08 Marks)

**Module-4**

- 7 a. The field  $B = (-2a_x + 3a_y + 4\hat{a}_z)$  mT is present in free space. Find the vector force exerted on a straight wire carrying a current of 12A in the  $a_{AB}$  direction. Given  $A(1, 1, 1)$  and  $B(2, 1, 1)$ . (04 Marks)
- b. Two differential current elements,  $I_1 \Delta L_1 = 3 \times 10^{-6}$  A-m at  $P_1(1, 0, 0)$  and  $I_2 \Delta L_2 = 3 \times 10^{-6} (-0.5 \hat{a}_x + 0.4 \hat{a}_y + 0.3 \hat{a}_z)$  A-m at  $P_2(2, 2, 2)$  are located in free space. Find the vector force exerted on  $I_2 \Delta L_2$  by  $I_1 \Delta L_1$ . (06 Marks)
- c. Find the magnetization in a magnetic material where
- $\mu = 1.8 \times 10^{-5}$  H/m and  $H = 120$  A/m.
  - $\mu_r = 22$ , there are  $8.3 \times 10^{22}$  atoms/m and each atom has a dipole moment of  $4.5 \times 10^{-27}$  A/m<sup>2</sup>.
  - $B = 300 \mu T \times \chi_m = 15$ . (06 Marks)

**OR**

- 8 a. Derive the Magnetic Boundary Condition? (06 Marks)
- b. Let the permittivity is  $5\mu H/m$  in the region 1 where  $x < 0$  and  $20 \mu H/m$  in the region 2 where  $x > 0$ , and if  $H = (300a_x - 400a_y + 500\hat{a}_z)$  A/m and if there is a surface current density  $K = (150 \hat{a}_y - 200 \hat{a}_z)$  A/m at  $x = 0$ .  
Find i)  $|H_{t_1}|$  ii)  $|H_{N_1}|$  iii)  $|H_{t_2}|$  iv)  $|H_{N_2}|$ . (06 Marks)
- c. Derive the expression for the energy density in a magnetic field. (04 Marks)

**Module-5**

- 9 a. Explain Displacement current density and conduction current density. (04 Marks)
- b. List Maxwell's equations for steady and time varying fields in
- Point form
  - Integral form. (06 Marks)
- c. Do the fields  $\vec{E} = E_m \sin x \sin t \hat{a}_y$  and  $\vec{H} = \frac{E_m}{\mu_0} \cos x \cos t \hat{a}_z$  satisfy Maxwell's equations? (06 Marks)

**OR**

- 10 a. What is Forward travelling wave and Backward travelling wave in free space? (02 Marks)
- b. A uniform plane wave in free space is given by  $E_s = 200 \angle 30^\circ \cdot e^{-j250z} \hat{a}_x$  V/m.  
Find  $\beta$ ,  $w$ ,  $f$ ,  $\lambda$ ,  $\eta$ ,  $|\vec{H}|$ . (06 Marks)
- c. State and prove Poynting theorem. (08 Marks)

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