

USN



Internal Assessment Test 3 – AUG 2024

Sub:	Analysis and Design of Algorithms				Sub Code:	BCS401	Branch:	CSE
Date:	07-08-2024	Duration:	90 mins	Max Marks:	50	Sem / Sec:	IV (A, B & C)	OBE

Answer any FIVE FULL Questions

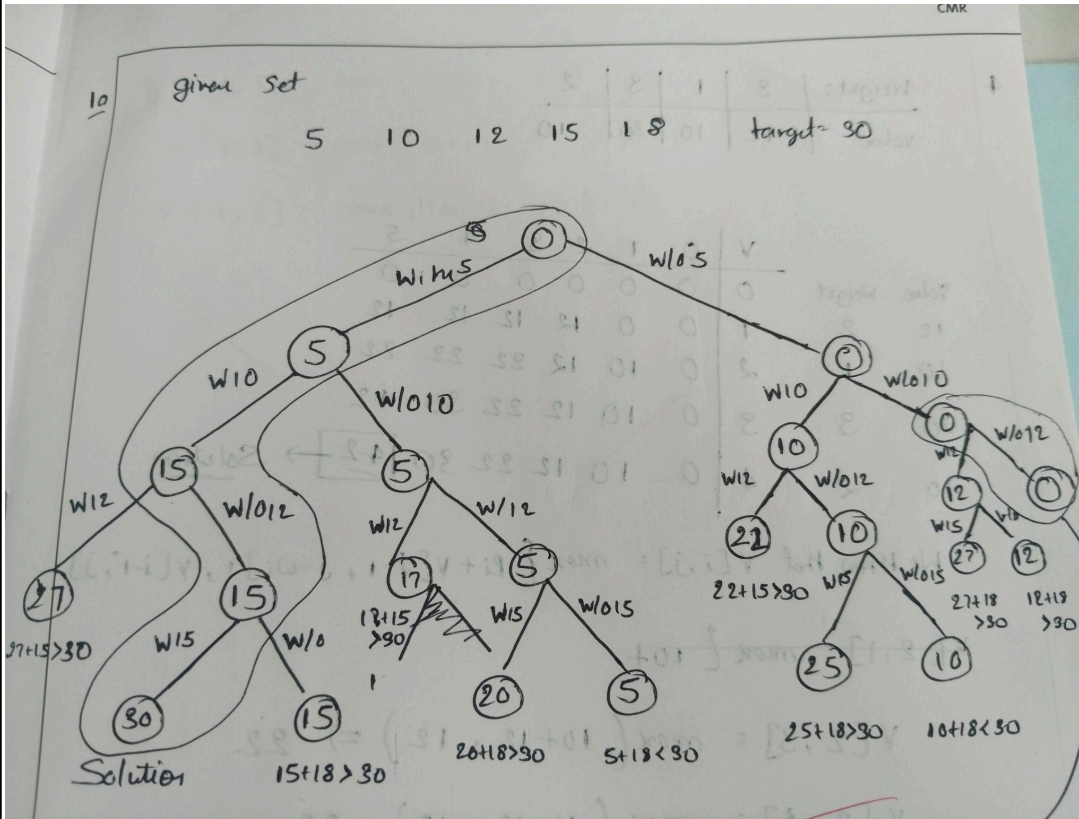
MARK
S

CO
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T

1 (a) Apply Backtracking method to solve sum of subset problem for the instance $d=30$, $S=\{5,10,12,15,18\}$. Give all possible solution with state space tree construction

10

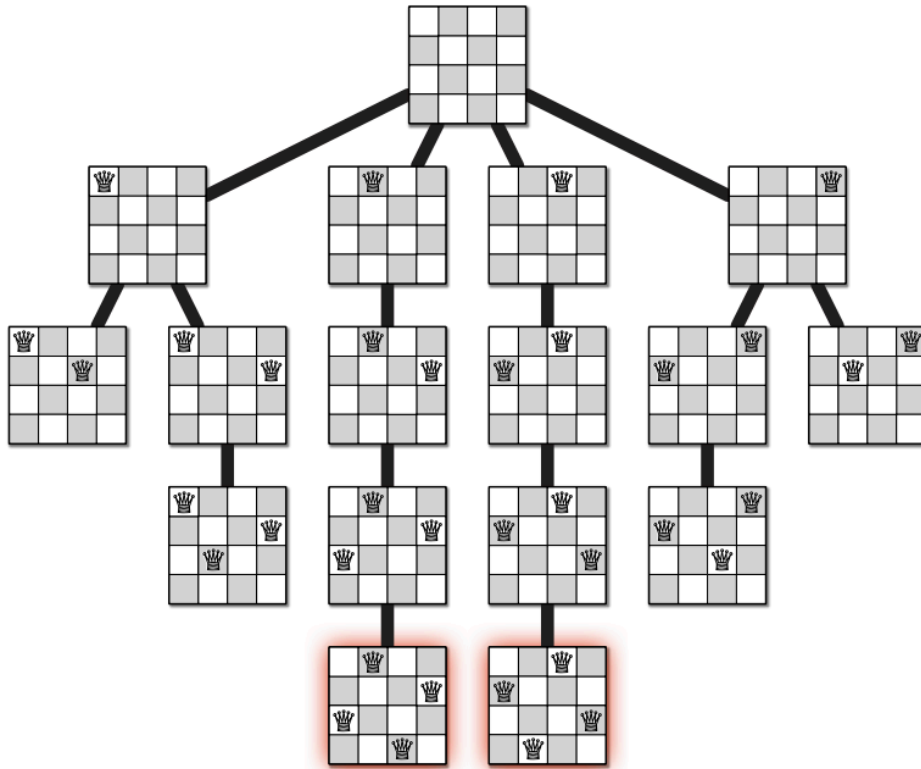
CO5 L3



2 (a) Draw the state space tree to generate solutions to 4-queen's problem

5

CO5 L2



2 (b) Construct the heap for the list 50 25 30 75 100 45 80 using top down approach

5

CO3

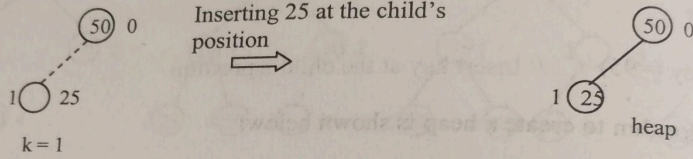
L3

using top-down approach

Step 1: Item = 50. Inserting the item into an empty tree, we get the tree as shown below.

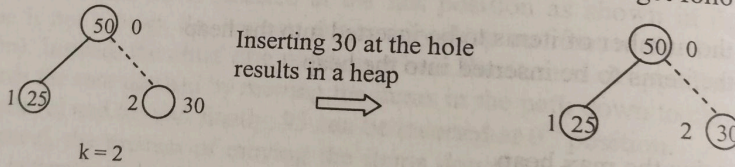


Step 2: Item = 25. Inserting the item into above heap at position 1, following heap is obtained



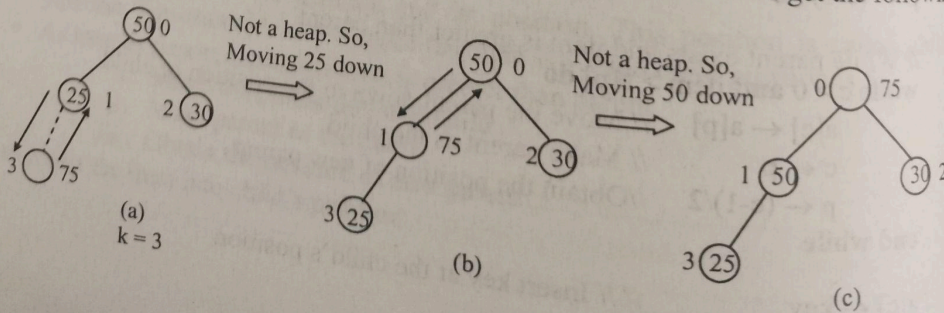
Observe that the parent 50 is greater than the child 25 and so, it can be inserted at the child's position and the resulting tree is a heap.

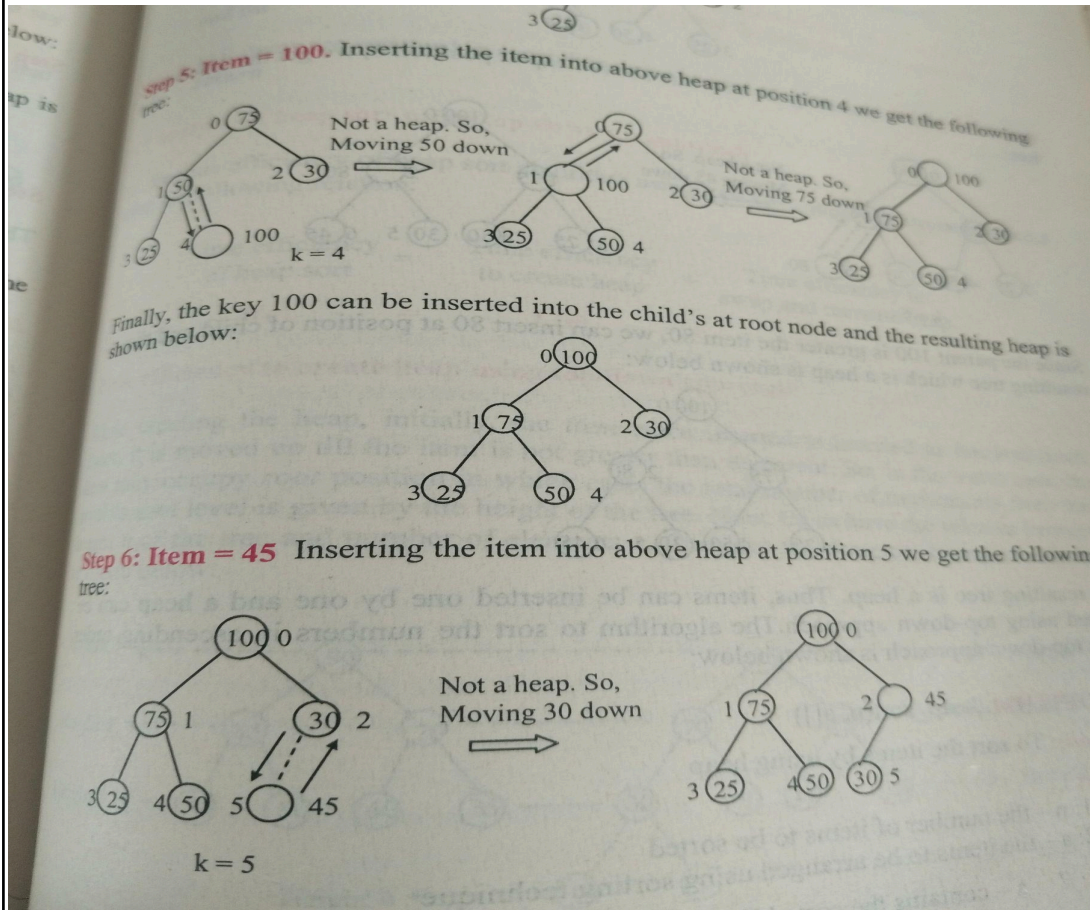
Step 3: Item = 30. After inserting into above heap at position 2 we get following heap



Observe that the parent 50 is greater than the child 30 and so, it can be inserted at the child's position and the resulting tree is a heap.

Step 4: Item = 75. Inserting the item into above heap at position 3 we get the following heap:





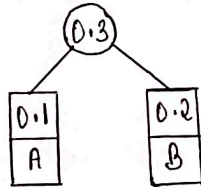
3	<p>A message consisting of the characters given in the table below has to be transmitted over a network in the secured manner</p> <table border="1" data-bbox="161 562 772 734"> <tr> <td data-bbox="161 562 376 647">Character</td> <td data-bbox="376 562 475 647">A</td> <td data-bbox="475 562 574 647">M</td> <td data-bbox="574 562 673 647">R</td> <td data-bbox="673 562 772 647">-</td> </tr> <tr> <td data-bbox="161 647 376 734">Probability</td> <td data-bbox="376 647 475 734">0.4</td> <td data-bbox="475 647 574 734">0.2</td> <td data-bbox="574 647 673 734">0.3</td> <td data-bbox="673 647 772 734">0.1</td> </tr> </table> <p>a)Construct the Huffman Tree for the following characters (Branch Label:Left(0),Right(1)). b)Derive the Huffman code for the given characters. c)Decode the text whose encoding is 1000101 d)Encode the text RAMA_RAMAR</p>	Character	A	M	R	-	Probability	0.4	0.2	0.3	0.1	10	CO4	L3
Character	A	M	R	-										
Probability	0.4	0.2	0.3	0.1										

Step 1: Arrange the keys in ascending order of their probability/frequency

0.1	0.2	0.3	0.4
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A B D C

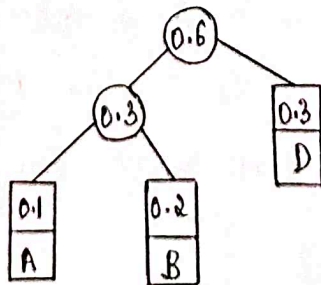
Select the first 2 minimum keys to construct the tree.



Step 2: Arrange in ascending order again

0.3	0.3	0.4
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*1 D C



(ii)

Character	Code
A	0
M	101
R	11
-	100

(iii)

$\underline{1000} \underline{101}$
- A M

$\therefore 1000101 \Rightarrow \text{-AM}$

(iv)

R A M A - R A M A R
↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓ ↓
11 0 101 0 100 11 0 101 0 11

$\therefore \text{RAMA-RAMAR} \Rightarrow 110101010101011$

4 Apply the memory function method to solve the following instance of the Knapsack problem with capacity $M=5$

10

CO4

L3

Item	Weight	Value
1	2	12
2	1	10
3	3	20
4	2	10

5(a) Apply the greedy method to obtain optimal solution to the knapsack problem given $M=60$.

5

CO3

L3

W={5,10,20,30,40}
P={30,20,100,90,60}

Find the total profit earned.

Ans:- Step 1: Calculate Profit/weight ratio.

Items	Profit	Weight	Profit/Weight
1	30	5	6
2	20	10	2
3	100	20	5
4	90	30	3
5	160	40	4

Step 2: Arrange all items in non-ascending order of Profit/Weight ratio.

Items	Profit	Weight	Profit/Weight	Remaining weight	Total Profit
1	30	5	6	60-5=55kg	30
3	100	20	5	55-20=35kg	30+100
5	160	40	4	35-35=0kg	$\frac{35 \times 160}{40} + 130$
4	90	30	3	-	
2	20	10	2	-	

$$\text{Total profit} = \left(\frac{35}{40} \times 160\right) + 130 = 140 + 130 = 170$$

$$\therefore \text{Total profit} = 170.$$

(b) Write the algorithm of Counting Sort. Sort the following numbers using the same. 10,1,0,2,5,6.

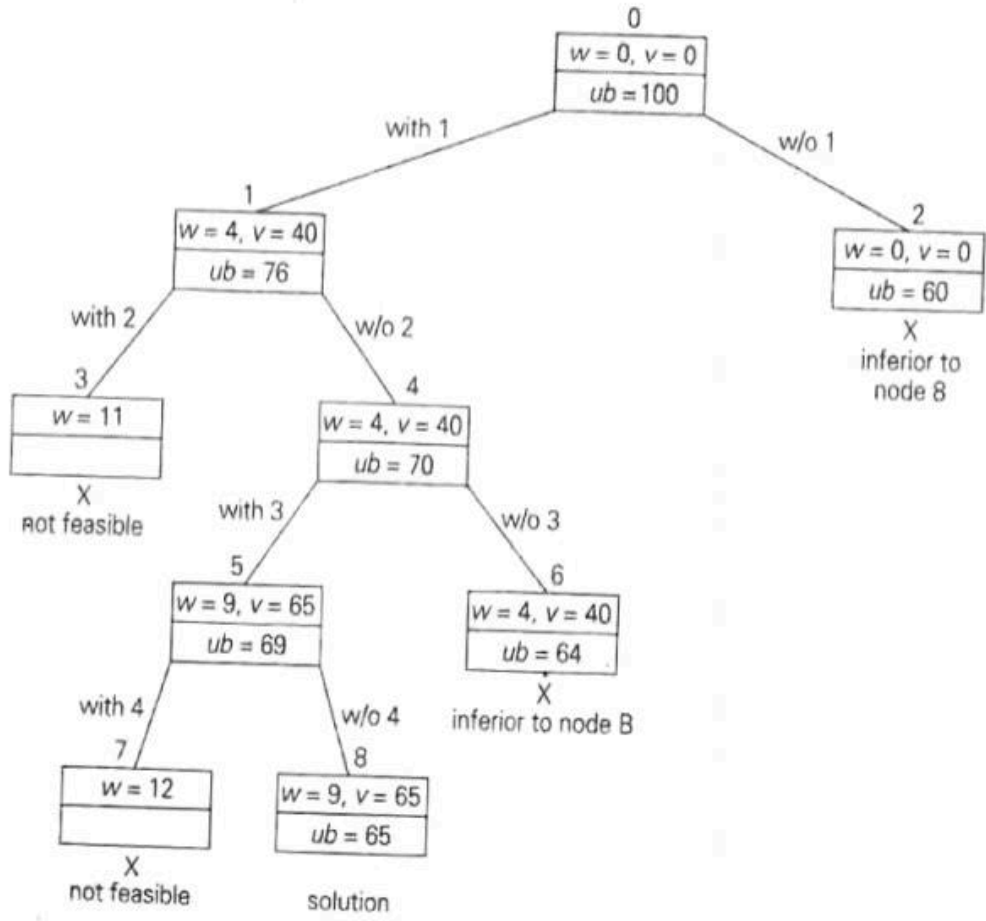
5 CO3 L2

6 Apply the branch and bound to solve the instance of 0/1 knapsack problem

10 CO5 L3

Item	1	2	3	4
Weight	4	7	5	3
Profit	\$40	\$42	\$25	\$12

knapsack capacity $W=10$



CI

CCI

HOD