

18EC55

Fifth Semester B.E. Degree Examination, June/July 2024

Electromagnetic Waves

Time: 3 hrs. Max. Marks: 100

Note: Answer any FIVE full questions, choosing ONE full question from each module.

Module-1

- 1 a. State and derive Coulomb's law. (06 Marks)
 - b. Find the force on charge Q_1 located at (4, -2, 1) m due to charge Q_2 located at (3, -1, -2) m. $Q_1 = 200 \ \mu\text{C}, \ Q_2 = 300 \ \mu\text{C}.$ (07 Marks)
 - c. Calculate the electric field intensity E at (-1, 3, -2) m due to infinite line charges with $\rho_1 = 25 \,\text{nC/m}$ lying along x-axis and $\rho_1 = 50 \,\text{nC/m}$ lying along y-axis. (07 Marks)

OR

- 2 a. Derive electric field intensity E due to infinite line charge. (06 Marks)
 - b. Two point charges $Q_1 = 5 \mu C$ and $Q_2 = -3 \mu C$ are located in free space at (1, 0, -2) m and (-2, 1, 3) m respectively. Find electric field intensity E at P(-3, 2, -1) m. (07 Marks)
 - c. Calculate the electric field intensity E at (-2, 1, -3) m due to infinite sheet charges:

 $\rho_{\rm S} = \frac{1}{6\pi} {\rm nC/m^2}$ located at y = 3 m and

$$\rho_{\rm S} = \frac{1}{3\pi} \, \text{nC/m}^2 \, \text{located at z} = 5 \, \text{m}$$

(07 Marks)

Module-2

3 a. State and prove Gauss law.

(06 Marks)

- b. Given $D = \frac{5r^3}{y} a_r C/m^2$ in cylindrical co-ordinates. Prove divergence theorem for the volume enclosed by r = 2m, r = 3m, z = 0 and z = 5m. (07 Marks)
- c. Find the total charge in a volume defined by six planes for which, $2 \le x \le 3$, $3 \le y \le 4$, $4 \le z \le 5$, if $D = 5x^2a_x + 4y^2a_y + 3za_zC/m^2$. (07 Marks)

OR

- 4 a. Using Gauss's law, derive the expressions for \overline{D} and \overline{E} due to co-axial cylindrical conductors. (06 Marks)
 - b. Calculate the total electric flux density due to two uniform line charges of 30 μ C/m lying along x-axis and 50 μ C/m lying along z-axis, at (2, 3, 4)m. (07 Marks)
 - c. In an electric field, potential field is $V = 5x^2 + 3y^3 + 8z$ volts. Find
 - (i) \overline{E} (ii) \overline{D} at (-3, 2, 4) m (07 Marks)

Module-3

- 5 a. Using Laplace's equation, derive the expression for potential (V) and electric field strength E due to two concentric cylinders of infinite length. (06 Marks)
 - b. In spherical co-ordinates V = 750 volts at r = 25 cm and E = 825 a_r V/m at r = 75 cm. Determine the location of voltage reference if potential depends only on r. (07 Marks)
 - e. State and prove Ampere's circuital law. (07 Marks)

OR

- 6 a. Using Biot-Savart's law, derive the expression for magnetic field intensity "H" due to infinite long conductor. (06 Marks)
 - b. In spherical co-ordinates, V = 0 for r = 0.2 m and V = 200 volts for r = 3 m. Assuming free space between concentric spheres (Shells) find electric field intensity E and flux density D. (07 Marks)
 - c. Find magnetic field intensity H at the center of a square loop of sides equal to 10 m and carrying a current of 5 amp. (07 Marks)

Module-4

- 7 a. Derive the equation for magnetic force on a differential current element in a magnetic field.
 (06 Marks)
 - b. Calculate the force on a straight conductor of length 0.5 m carrying a current of 10 amp in the z-direction, where $\overline{B} = 5 \times 10^{-3} a_x$ Tesla and $B = 6 \times 10^{-3} a_y$ Tesla. (07 Marks)
 - c. A solenoid with air core has 2000 turns and a length of 700 mm. Core radius is 50 mm. Find self inductance. (07 Marks)

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- 8 a. Derive the equation for force between two parallel current carrying conductors. (06 Marks)
 - b. Derive tangential and normal boundary conditions (magnetic) between two media of permeabilities μ_1 and μ_2 . (07 Marks)
 - c. Find the inductance per unit length of a co-axial conductor with an inner radius of a=4 mm and outer radius of b=10 mm. Assume $\mu_r=1$. (07 Marks)

Module-5

- 9 a. State the inconsistency of Ampere's law, for time varying fields. Derive Maxwell's equation to correct it. (06 Marks)
 - b. Derive general plane wave equation in terms of E, taking help of the Maxwell's equation (for free space). (07 Marks)
 - c. A plane wave travelling in positive z-direction in a lossless unbounded medium has permeability 5 times that of free space and a dielectric constant 3 times that of free space.
 - (i) Find phase velocity of the wave
 - (ii) If E has only x-component with amplitude 25 V/m, find amplitude and direction of H. (07 Marks)

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OR

- 10 a. Prove that conduction current and displacement current are equal.
- (06 Marks)

b. State and explain Poynting theorem.

- (05 Marks)
- c. Determine following parameters for a medium with $\epsilon_r = 4$, $\mu_r = 1$, $\sigma = 20 \times 10^{-2} \text{ S/m}$, f = 1 mHz.
 - (i) Attenuation constant
 - (ii) Phase shift constant
 - (iii) Propagation constant
 - (iv) Wavelength
 - (v) Phase velocity
 - (vi) Intrinsic impedance
 - (vii) Skin depth (δ)

(09 Marks)

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