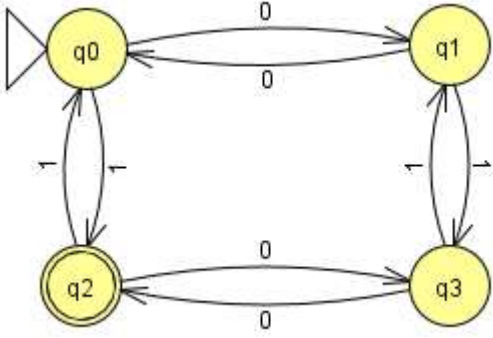


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**Internal Assessment Test 1 – Nov 2024**

Sub:	Theory of Computation					Sub Code:	BCS503	Branch:	CSE														
Date:	11.11.2024	Duration:	90 mins	Max Marks:	50	Sem/Sec:	5 B		OBE														
<u>Answer any FIVE FULL Questions</u>								MARKS	CO	RBT													
<p><i>*For all DFA, NFA questions, write the sample string in <math>L</math> and <math>\bar{L}</math>, the definition and transition table. Give Extended transition function for the strings give and state formally whether the string is accepted or rejected by the machine.</i></p>																							
1 (a)	<p>Define i)alphabet ii)Powers of alphabet with examples                  An alphabet is a finite non-empty set of symbols. <math>\Sigma</math> denotes an alphabet.                  1. <math>\Sigma=\{0,1\}</math> is the binary alphabet                  2. <math>\Sigma=\{a,b,\dots,z\}</math> is the set of lower case letters                  3. The set of all printable ASCII characters</p> <p>ii) Powers of alphabet                  If <math>\Sigma</math> is an alphabet, we can express the set of all strings of a certain length from that alphabet as <math>\Sigma^k</math>  <math>\Sigma^0 = \{\epsilon\}</math>  <math>\Sigma = \{0,1\}</math>, then <math>\Sigma^1 = \{0,1\}</math>, <math>\Sigma^2 = \{00,01,10,11\}</math>, <math>\Sigma^3 = \{000,001,010,011,100,101,110,111\}</math>  <math>\Sigma^* = \Sigma^0 \cup \Sigma^1 \cup \Sigma^2 \dots</math></p>					3M	CO1	L1															
(b)	<p>Design DFA for alphabet over <math>\{0,1\}</math></p> <p>i) Set of all strings where number of 0's is even and number of 1's is odd. Write extended transition function for <math>w_1=001</math>, <math>w_2=1100</math></p>  <p><math>A = (Q, \Sigma, \delta, q_0, F)</math>  <math>A = (\{q_0, q_1, q_2, q_3\}, \{0,1\}, \delta, q_0, \{q_2\})</math></p> <table border="1" style="margin-left: auto; margin-right: auto;"> <thead> <tr> <th><math>\delta</math></th> <th>0</th> <th>1</th> </tr> </thead> <tbody> <tr> <th><math>\rightarrow q_0</math></th> <td>q1</td> <td>q2</td> </tr> <tr> <th>q1</th> <td>q0</td> <td>q3</td> </tr> <tr> <th>* q2</th> <td>q3</td> <td>q0</td> </tr> <tr> <th>q3</th> <td>q2</td> <td>q1</td> </tr> </tbody> </table>					$\delta$	0	1	$\rightarrow q_0$	q1	q2	q1	q0	q3	* q2	q3	q0	q3	q2	q1	7	CO1	L3
$\delta$	0	1																					
$\rightarrow q_0$	q1	q2																					
q1	q0	q3																					
* q2	q3	q0																					
q3	q2	q1																					

### Extended Transition Function

i)  $w_1=001, w_2=1100$

$$\hat{\delta}(q_0, \epsilon) = q_0$$

$$\hat{\delta}(q_0, 0) = \delta(\hat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = q_1$$

$$\hat{\delta}(q_0, 00) = \delta(\hat{\delta}(q_0, 0), 0) = \delta(q_1, 0) = q_0$$

$$\hat{\delta}(q_0, 001) = \delta(\hat{\delta}(q_0, 00), 1) = \delta(q_0, 1) = q_2$$

As  $q_2 \in F$ , the string  $w=001$  is accepted by the automaton A.

$$\hat{\delta}(q_0, \epsilon) = q_0$$

$$\hat{\delta}(q_0, 1) = \delta(\hat{\delta}(q_0, \epsilon), 1) = \delta(q_0, 1) = q_2$$

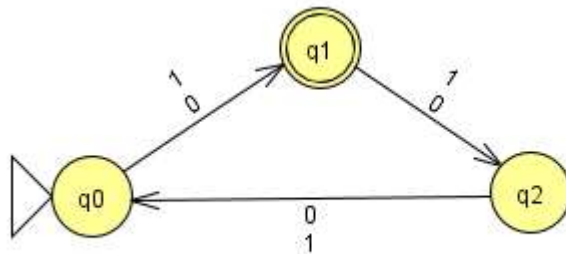
$$\hat{\delta}(q_0, 11) = \delta(\hat{\delta}(q_0, 1), 1) = \delta(q_2, 1) = q_0$$

$$\hat{\delta}(q_0, 110) = \delta(\hat{\delta}(q_0, 11), 0) = \delta(q_0, 0) = q_1$$

$$\hat{\delta}(q_0, 1100) = \delta(\hat{\delta}(q_0, 110), 0) = \delta(q_1, 0) = q_0$$

As  $q_0 \notin F$ , the string  $w=1100$  is rejected by the automaton A.

ii)  $\{w: |w| \bmod 3 = 1\}$  Write extended transition function for  $w_1=1001, w_2=010$



$$A = (Q, \Sigma, \delta, q_0, F)$$

$$A = (\{q_0, q_1, q_2\}, \{0, 1\}, \delta, q_0, \{q_1\})$$

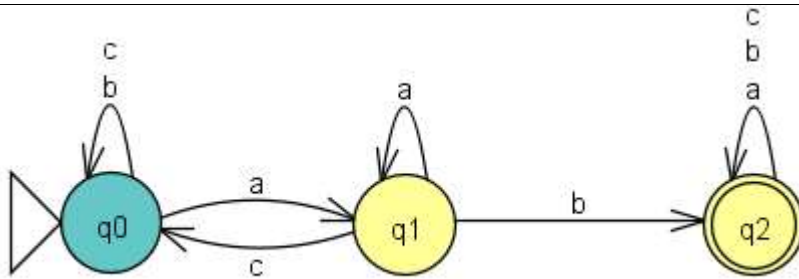
### Extended Transition Function

i)  $w_1=1001, w_2=010$

$\delta$	0	1
$\rightarrow q_0$	q1	q1
* q1	q2	q2
* q2	q0	q0

$$\hat{\delta}(q_0, \epsilon) = q_0$$

	$\widehat{\delta}(q_0, 1) = \delta(\widehat{\delta}(q_0, \epsilon), 1) = \delta(q_0, 1) = q_1$ $\widehat{\delta}(q_0, 10) = \delta(\widehat{\delta}(q_0, 1), 0) = \delta(q_1, 0) = q_2$ $\widehat{\delta}(q_0, 100) = \delta(\widehat{\delta}(q_0, 10), 0) = \delta(q_2, 0) = q_0$ $\widehat{\delta}(q_0, 1001) = \delta(\widehat{\delta}(q_0, 100), 1) = \delta(q_0, 1) = q_1$ <p><b>As <math>q_1 \in F</math>, the string <math>w=1001</math> where <math> w  = 4</math> and <math>4 \bmod 3 = 1</math> is accepted by the automaton A.</b></p> $\widehat{\delta}(q_0, \epsilon) = q_0$ $\widehat{\delta}(q_0, 0) = \delta(\widehat{\delta}(q_0, \epsilon), 0) = \delta(q_0, 0) = q_1$ $\widehat{\delta}(q_0, 01) = \delta(\widehat{\delta}(q_0, 0), 1) = \delta(q_1, 1) = q_2$ $\widehat{\delta}(q_0, 010) = \delta(\widehat{\delta}(q_0, 01), 0) = \delta(q_2, 0) = q_0$ <p><b>As <math>q_0 \notin F</math>, the string <math>w=010</math> where <math> w  = 3</math> and <math>3 \bmod 3 = 0</math> is rejected by the automaton A.</b></p>			
2 (a)	<p>Define i)string ii)language</p> <p>i) <b>String</b> : A string(word) is a finite sequence of symbols chosen from an alphabet. Eg. <math>w=01101</math> is from the alphabet <math>\Sigma=\{0,1\}</math></p> <p>Empty string is a string with 0 occurrences denoted by <math>\epsilon</math>.</p> <p>Length of a string : the number of positions for symbols in a string <math>w=00101</math>, <math> w  = 5</math>.</p> <p>Powers of alphabet can also be used to form strings from an alphabet of varying lengths.</p> <p>ii) <b>Language</b> : A set of all strings which are chosen from <math>\Sigma^*</math> where <math>\Sigma</math> is a particular alphabet.</p> <p>If <math>\Sigma</math> is an alphabet, and <math>L \subseteq \Sigma^*</math>, then L is the language of <math>\Sigma</math></p> <p>Eg. 1. Set of all strings consisting of n 0's followed by n 1s, <math>n \geq 0</math>  <math>\{\epsilon, 01, 0011, 000111, \dots\}</math></p> <p>2. Set of binary numbers whose value is prime  <math>\{01, 10, 11, 101, 111, \dots\}</math></p>	3	CO1	L1
(b)	<p>Design DFA for alphabet over <math>\{a,b,c\}</math></p> <p>i) <b>Set of strings that have ab as a substring. Write extended transition function for <math>w_1=cabc</math></b></p>	7	CO1	L3



$L = \{ab, cab, cabbc, aaccbab, \dots\}$

$\bar{L} = \{\epsilon, aacc, bcaac, \dots\}$

**Definition**

$A = (Q, \Sigma, \delta, q_0, F)$

$A = (\{q_0, q_1, q_2\}, \{a, b, c\}, \delta, q_0, \{q_2\})$

$\delta$	a	b	c
$\rightarrow q_0$	q1	q0	q0
<b>q1</b>	q1	q2	q0
<b>* q2</b>	q2	q2	q2

**Extended Transition Function**

$$\hat{\delta}(q_0, \epsilon) = q_0$$

$$\hat{\delta}(q_0, c) = \delta(\hat{\delta}(q_0, \epsilon), c) = \delta(q_0, c) = q_0$$

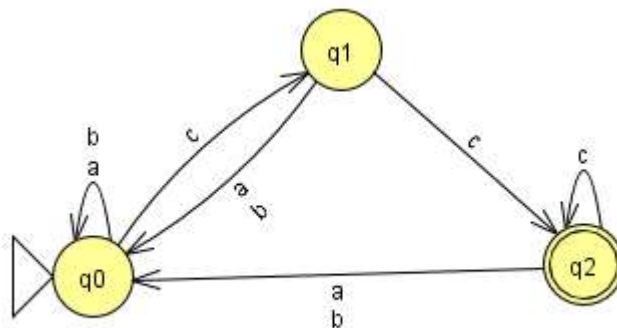
$$\hat{\delta}(q_0, ca) = \delta(\hat{\delta}(q_0, c), a) = \delta(q_0, a) = q_1$$

$$\hat{\delta}(q_0, cab) = \delta(\hat{\delta}(q_0, ca), b) = \delta(q_1, b) = q_2$$

$$\hat{\delta}(q_0, cabc) = \delta(\hat{\delta}(q_0, cab), c) = \delta(q_2, c) = q_2$$

As  $q_2 \in F$ , the string  $w=cabc$  is accepted by the automaton A.

ii) **Set of strings that end in cc. Write extended transition function for  $w_1=abcc$**



$L = \{cc, abcc, bacacc, \dots\}$

$$\bar{L} = \{\epsilon, a, b, c, aa, ab, baccab, \dots\}$$

**Definition**

$$A = (Q, \Sigma, \delta, q_0, F)$$

$$A = (\{q_0, q_1, q_2\}, \{a, b, c\}, \delta, q_0, \{q_2\})$$

$\delta$	a	b	c
$\rightarrow q_0$	q0	q0	q1
<b>q1</b>	q0	q0	q2
<b>* q2</b>	q0	q0	q2

**Extended Transition Function**

$$\hat{\delta}(q_0, \epsilon) = q_0$$

$$\hat{\delta}(q_0, a) = \delta(\hat{\delta}(q_0, \epsilon), a) = \delta(q_0, a) = q_0$$

$$\hat{\delta}(q_0, ab) = \delta(\hat{\delta}(q_0, a), b) = \delta(q_0, b) = q_0$$

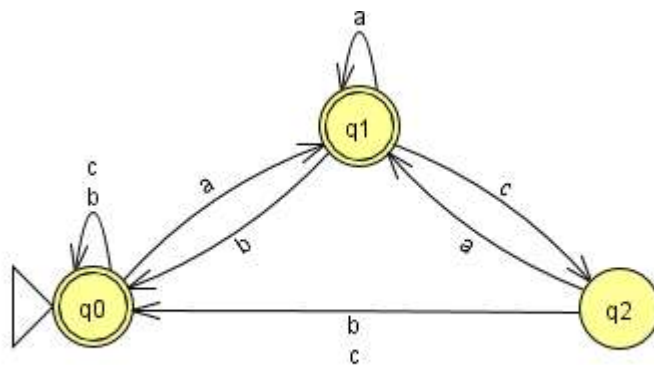
$$\hat{\delta}(q_0, abc) = \delta(\hat{\delta}(q_0, ab), c) = \delta(q_0, c) = q_1$$

$$\hat{\delta}(q_0, abcc) = \delta(\hat{\delta}(q_0, abc), c) = \delta(q_1, c) = q_2$$

As  $q_2 \in F$ , the string  $w=abcc$  is accepted by the automaton A.

iii) **Set of strings that do not end in ac. Write extended transition function for  $w_1=cca$**

First design a machine that ends in ac, then invert the accepting and non-accepting states



$$L = \{ab, cabb, aaca\}$$

$$\bar{L} = \{ac, abac, aaac, \dots\}$$

**Definition**

$$A = (Q, \Sigma, \delta, q_0, F)$$

$$A = (\{q_0, q_1, q_2\}, \{a, b, c\}, \delta, q_0, \{q_0, q_1\})$$

$\delta$	a	b	c
* $\rightarrow q_0$	q <sub>1</sub>	q <sub>0</sub>	q <sub>0</sub>
*q <sub>1</sub>	q <sub>1</sub>	q <sub>0</sub>	q <sub>2</sub>
q <sub>2</sub>	q <sub>1</sub>	q <sub>0</sub>	q <sub>0</sub>

### Extended Transition Function

$$\widehat{\delta}(q_0, \epsilon) = q_0$$

$$\widehat{\delta}(q_0, c) = \delta(\widehat{\delta}(q_0, \epsilon), c) = \delta(q_0, c) = q_0$$

$$\widehat{\delta}(q_0, cc) = \delta(\widehat{\delta}(q_0, c), c) = \delta(q_0, c) = q_0$$

$$\widehat{\delta}(q_0, cca) = \delta(\widehat{\delta}(q_0, cc), a) = \delta(q_0, a) = q_1$$

As  $q_1 \in F$ , the string  $w = cca$  is accepted by the automaton A.

Differentiate NFA and DFA. (Clearly explain the difference in transition functions formally)

DFA	NFA
Deterministic	Non-deterministic
Transition function for each input symbol to exactly one state $\delta(s, a) = r$ where $r \in Q$	Transition relation on input symbol results in a $\Phi$ set or more than one states Eg. $\delta(s, a) = \Phi$ $\Delta(s, b) = \{p, r\}$
Running time is $O(n)$ where $n$ is the length of the input string	Worst case time complexity is $O(N*S)$ where $N$ is the length of the strings and $S$ is the number of states.
There is exactly one path to accept or reject a string	There are multiple paths. Some paths may lead to accepting states.
A string is accepted when $\widehat{\delta}(q_0, w) = f$ and $f \in F$	A string is accepted when $\widehat{\delta}(q_0, w) = \{a_1, a_2, \dots, a_n\}$ where $= \{a_1, a_2, \dots, a_n\} \cap F \neq \Phi$
Difficult to construct	Simple to construct

3 (a)

4

CO1

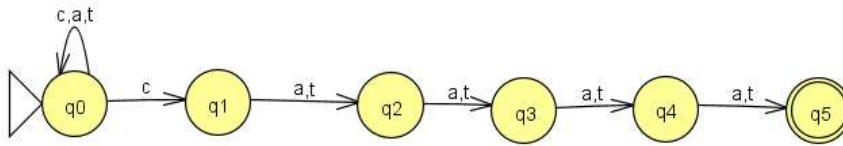
L1

Does not contain  $\epsilon$ -Transitions

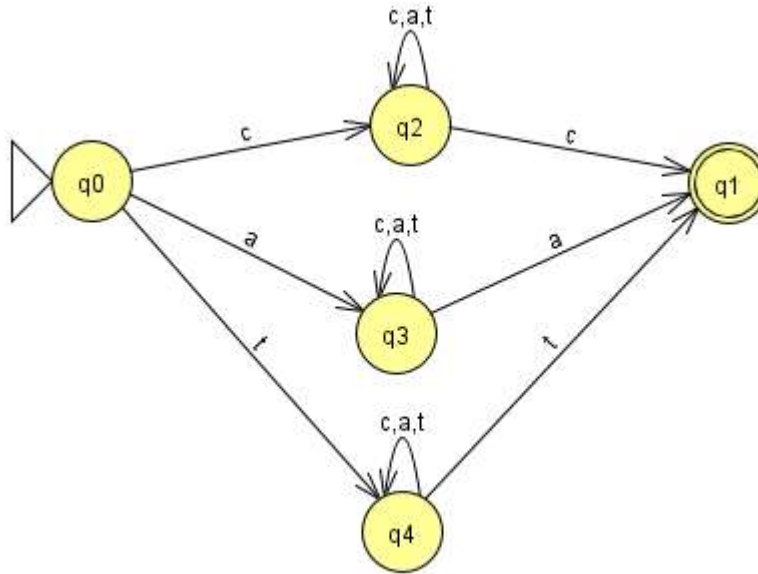
May contain  $\epsilon$ - transitions

Design NFA for the following over the alphabet  $\{c,a,t\}$

i) Accepts strings where the 5<sup>th</sup> last letter from the right is c, eg. taacaatc



ii) Accepts strings that begins and ends with the same letter.



(b)

6

CO1

L3

Write the procedure to compute  $\epsilon$ -CLOSE

Basis :The state q is in  $\epsilon$ -CLOSE(q)

Induction: If state p is in  $\epsilon$ -CLOSE(q) and there is a transition from state p to state r labeled  $\epsilon$ , then r is in  $\epsilon$ -CLOSE(q)

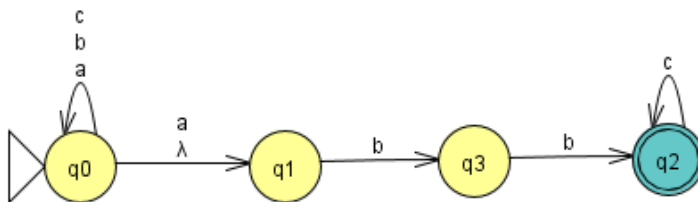
4 (a)

3

CO1

L1

Convert the following  $\epsilon$ -NFA ( $\lambda$  is empty transition) to a DFA by first computing  $\epsilon$ -CLOSE of all the states.



(b)

7

CO1

L3

$\delta$	a	b	c	$\epsilon$ -close
$\rightarrow q_0$	{q <sub>0</sub> , q <sub>1</sub> }	q <sub>0</sub>	q <sub>0</sub>	{q <sub>0</sub> ,q <sub>1</sub> }
<b>q<sub>1</sub></b>	$\Phi$	q <sub>3</sub>	$\Phi$	{q <sub>1</sub> }

q3	Φ	q2	Φ	{ q3 }
*q2	Φ	Φ	q2	{ q2 }

### Lazy Subset Construction

$$\delta(\{q_0, q_1\}, a) = \delta(q_0, a) \cup \delta(q_1, a) = \{q_0, q_1\} \cup \Phi = \varepsilon\text{-close}(q_0) \cup \varepsilon\text{-close}(q_1) = \{q_0, q_1\} \cup \{q_1\} = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1\}, b) = \delta(q_0, b) \cup \delta(q_1, b) = \{q_0\} \cup \{q_3\} = \varepsilon\text{-close}(q_0) \cup \varepsilon\text{-close}(q_3) = \{q_0, q_1\} \cup \{q_3\} = \{q_0, q_1, q_3\}$$

$$\delta(\{q_0, q_1\}, c) = \delta(q_0, c) \cup \delta(q_1, c) = \{q_0\} \cup \Phi = \varepsilon\text{-close}(q_0) = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1, q_3\}, a) = \delta(q_0, a) \cup \delta(q_1, a) \cup \delta(q_3, a) = \{q_0, q_1\} \cup \Phi \cup \Phi = \varepsilon\text{-close}(q_0) = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1, q_3\}, b) = \delta(q_0, b) \cup \delta(q_1, b) \cup \delta(q_3, b) = \{q_0\} \cup \{q_3\} \cup \{q_2\} = \varepsilon\text{-close}(q_0) \cup \varepsilon\text{-close}(q_3) \cup \varepsilon\text{-close}(q_2) = \{q_0, q_1\} \cup \{q_3\} \cup \{q_2\} = \{q_0, q_1, q_3, q_2\}$$

$$\delta(\{q_0, q_1, q_3\}, c) = \delta(q_0, c) \cup \delta(q_1, c) \cup \delta(q_3, c) = \{q_0\} \cup \Phi \cup \Phi = \varepsilon\text{-close}(q_0) = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1, q_3, q_2\}, a) = \delta(q_0, a) \cup \delta(q_1, a) \cup \delta(q_3, a) \cup \delta(q_2, a) = \{q_0, q_1\} \cup \Phi \cup \Phi \cup \Phi = \varepsilon\text{-close}(q_0) = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1, q_3, q_2\}, b) = \delta(q_0, b) \cup \delta(q_1, b) \cup \delta(q_3, b) \cup \delta(q_2, b) = \{q_0\} \cup \{q_3\} \cup \{q_2\} \cup \Phi = \varepsilon\text{-close}(q_0) \cup \varepsilon\text{-close}(q_3) \cup \varepsilon\text{-close}(q_2) = \{q_0, q_1\} \cup \{q_3\} \cup \{q_2\} = \{q_0, q_1, q_3, q_2\}$$

$$\delta(\{q_0, q_1, q_3, q_2\}, c) = \delta(q_0, c) \cup \delta(q_1, c) \cup \delta(q_3, c) \cup \delta(q_2, c) = \{q_0\} \cup \Phi \cup \Phi \cup \Phi = \varepsilon\text{-close}(q_0) \cup \varepsilon\text{-close}(q_2) = \{q_0, q_1\} \cup \{q_2\} = \{q_0, q_1, q_2\}$$

$$\delta(\{q_0, q_1, q_2\}, a) = \delta(q_0, a) \cup \delta(q_1, a) \cup \delta(q_2, a) = \{q_0, q_1\} \cup \Phi \cup \Phi = \varepsilon\text{-close}(q_0) = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1, q_2\}, b) = \delta(q_0, b) \cup \delta(q_1, b) \cup \delta(q_2, b) = \{q_0\} \cup \{q_3\} \cup \Phi = \varepsilon\text{-close}(q_0) \cup \varepsilon\text{-close}(q_3) = \{q_0, q_1\} \cup \{q_3\} = \{q_0, q_1, q_3\}$$



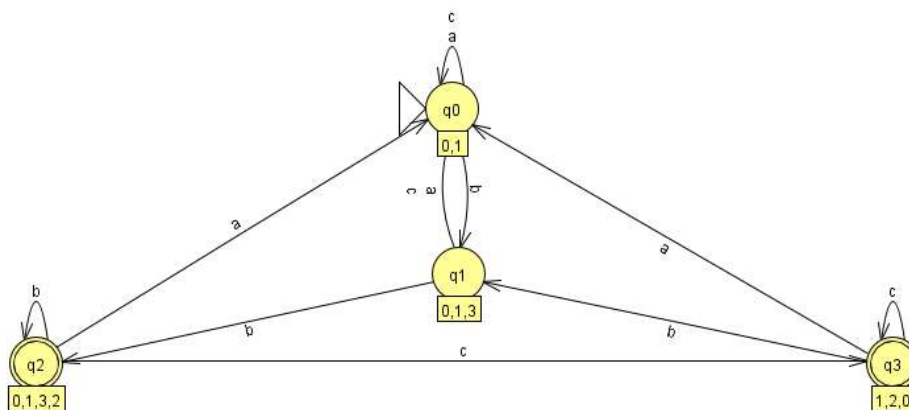
$$\delta(\{q_0, q_1, q_2\}, c) = \delta(q_0, c) \cup \delta(q_1, c) \cup \delta(q_2, c) = \{q_0\} \cup \Phi \cup \{q_2\} = \varepsilon\text{-close}(q_0)$$

$$\cup \varepsilon\text{-close}(q_2) = \{q_0, q_1\} \cup \{q_2\} = \{q_0, q_1, q_2\}$$

$\delta_D$	a	b	c
$\rightarrow \{q_0, q_1\}$	$\{q_0, q_1\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_1\}$
$\{q_0, q_1, q_3\}$	$\{q_0, q_1\}$	$\{q_0, q_1, q_3, q_2\}$	$\{q_0, q_1\}$
$*\{q_0, q_1, q_3, q_2\}$	$\{q_0, q_1\}$	$\{q_0, q_1, q_3, q_2\}$	$\{q_0, q_1, q_2\}$
$*\{q_0, q_1, q_2\}$	$\{q_0, q_1\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_1, q_2\}$

$$A = (Q, \Sigma, \delta, q_0, F)$$

$$A = (\{ \{q_0, q_1\}, \{q_0, q_1, q_3\}, \{q_0, q_1, q_3, q_2\}, \{q_0, q_1, q_2\} \}, \{a, b, c\}, \delta_D, \{q_0, q_1\}, \{ \{q_0, q_1, q_3, q_2\}, \{q_0, q_1, q_2\} \} )$$



Define NFA

$$A = (Q, \Sigma, \delta, q_0, F)$$

1.  $Q$  is the finite set of states
2.  $\Sigma$  is the finite set of input symbols
3.  $q_0 \in Q$  is the start state
4.  $\delta$  is the transition function that takes a state in  $Q$  and an input symbol in  $\Sigma$  and returns a subset of  $Q$ . If there is no state, it returns  $\Phi$ .

5 (a)

4

CO1

L1

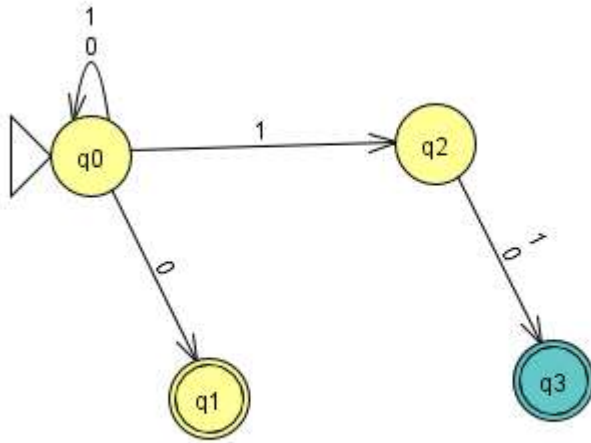
(b)

Convert the following NFA into DFA using subset construction. Expand only accessible states. Write the Definition and transition table of the DFA.

6

CO1

L3



$\delta$	0	1
$\rightarrow q_0$	{q <sub>0</sub> , q <sub>1</sub> }	{q <sub>0</sub> , q <sub>2</sub> }
<b>q<sub>1</sub></b>	$\Phi$	$\Phi$
<b>q<sub>2</sub></b>	{q <sub>3</sub> }	{q <sub>3</sub> }
<b>*q<sub>3</sub></b>	$\Phi$	$\Phi$

### Lazy Subset Construction

$$\delta(\{q_0\}, 0) = \{q_0, q_1\}, \delta(\{q_0\}, 1) = \{q_0, q_2\}$$

$$\delta(\{q_0, q_1\}, 0) = \delta(q_0, 0) \cup \delta(q_1, 0) = \{q_0, q_1\} \cup \Phi = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1\}, 1) = \delta(q_0, 1) \cup \delta(q_1, 1) = \{q_0, q_2\} \cup \Phi = \{q_0, q_2\}$$

$$\delta(\{q_0, q_2\}, 0) = \delta(q_0, 0) \cup \delta(q_2, 0) = \{q_0, q_1\} \cup \{q_3\} = \{q_0, q_1, q_3\}$$

$$\delta(\{q_0, q_2\}, 1) = \delta(q_0, 1) \cup \delta(q_2, 1) = \{q_0, q_2\} \cup \{q_3\} = \{q_0, q_2, q_3\}$$

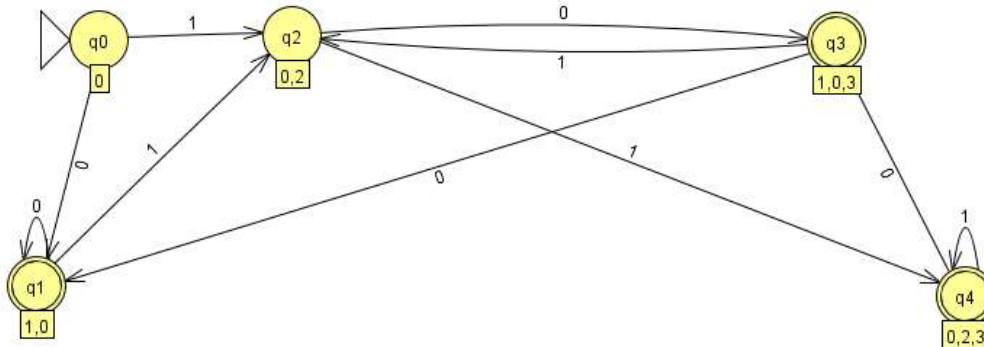
$$\delta(\{q_0, q_1, q_3\}, 0) = \delta(q_0, 0) \cup \delta(q_1, 0) \cup \delta(q_3, 0) = \{q_0, q_1\} \cup \Phi \cup \Phi = \{q_0, q_1\}$$

$$\delta(\{q_0, q_1, q_3\}, 1) = \delta(q_0, 1) \cup \delta(q_1, 1) \cup \delta(q_3, 1) = \{q_0, q_2\} \cup \Phi \cup \Phi = \{q_0, q_2\}$$

$$\delta(\{q_0, q_2, q_3\}, 0) = \delta(q_0, 0) \cup \delta(q_2, 0) \cup \delta(q_3, 0) = \{q_0, q_1\} \cup \{q_3\} \cup \Phi = \{q_0, q_1, q_3\}$$

$$\delta(\{q_0, q_2, q_3\}, 1) = \delta(q_0, 1) \cup \delta(q_2, 1) \cup \delta(q_3, 1) = \{q_0, q_2\} \cup \{q_3\} \cup \Phi = \{q_0, q_2, q_3\}$$

$\delta_D$	0	1
$\rightarrow q_0$	$\{q_0, q_1\}$	$\{q_0, q_2\}$
$*\{q_0, q_1\}$	$\{q_0, q_1\}$	$\{q_0, q_2\}$
$\{q_0, q_2\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_2, q_3\}$
$*\{q_0, q_1, q_3\}$	$\{q_0, q_1\}$	$\{q_0, q_2\}$
$*\{q_0, q_2, q_3\}$	$\{q_0, q_1, q_3\}$	$\{q_0, q_2, q_3\}$



$A = (Q, \Sigma, \delta, q_0, F)$

$A = (\{q_0, q_1, q_2, q_3, q_4\}, \{0, 1\}, \delta, q_0, \{q_3, q_4\})$

What are Regular expressions? Explain the construction of regular expression.

A regular expression is a declarative way to express strings we want to accept.

Building RE

**Basis :**

1.  $\epsilon$  and  $\Phi$  are regular expressions denoting the languages  $\{\epsilon\}$  and  $\Phi$
2. If  $a$  is a symbol, then  $a$  is a regular expression  $\{a\}$  and  $L(a) = \{a\}$
3. A variable  $L$  representing the language

6 (a) **Induction:**

1. If  $E$  and  $F$  are regular expressions, the union of  $E$  and  $F$  is also a RE  
 $E+F, L(E+F) = L(E) + L(F)$ .
2. If  $E$  and  $F$  are regular expressions, the concatenation of  $E$  and  $F$  is also a RE  
 $EF, L(EF) = L(E) L(F)$
3. If  $E$  is a regular expression  $E^*$  is also RE denoting closure of  $E$ .  $L(E^*) = (L(E))^*$

4

CO2

L2

	4. If E is a regular expression, (E) is also RE.			
(b)	<p>Form regular expressions for the following:</p> <p>For alphabet over {0,1}</p> <p>i) The length of the string is odd  <math>(0+1) ((0+1)(0+1))^*</math></p> <p>ii) Contains the substring 001  <math>(0+1)^* 001 (0+1)^*</math></p> <p>iii) Number of 0s is a multiple of 3  <math>(1^*01^*01^*01^*)^*</math></p> <p>For alphabet over {t,o,c}</p> <p>iv) Containing at least 2 o's  <math>(t+c+o)^* o (t+c+o)^* o (t+c+o)^*</math></p> <p>v) <math>t^n c^m o^n</math>: <math>n \geq 2, m &lt; 3</math>  <math>ttt^*(\epsilon + c + cc)ooo^*</math></p> <p>vi) at least one c and at least one t  <math>(t+c+o)^* c (t+c+o)^* t (t+c+o)^* +</math>  <math>(t+c+o)^* t (t+c+o)^* c (t+c+o)^*</math></p>	<b>6</b>	<b>CO2</b>	<b>L3</b>

CI

CCI

HOD

Course Outcomes		Blooms Level	Modules covered	PO 1	PO 2	PO 3	PO 4	PO 5	PO 6	PO 7	PO 8	PO 9	PO 10	PO 11	PO 12	PSO 1	PSO 2	PSO 3	PSO 4
CO1	Apply the fundamentals of automata theory to write DFA, NFA, Epsilon-NFA and conversion between them.	L1, L2, L3	1	3	2	2	-	2	-	-	-	-	-	-	-	2	2	-	3
CO2	Prove the properties of regular languages using regular expressions.	L1, L2	2	3	3	2	3	-	-	-	-	-	-	-	-	2	2	-	3
CO3	Design context-free grammars (CFGs) and pushdown automata (PDAs) for formal languages.	L1, L2, L3	3,4	3	3	2	3	2	-	-	-	-	-	-	-	-	2	-	3
CO4	Design Turing machines to solve the computational problems.	L1, L2, L3	5	2	3	2	3	2	-	-	-	-	-	-	-	-	2	-	3
CO5	Explain the concepts of decidability and undecidability	L1, L2, L3	5	3	2	2	3	-	-	-	-	-	-	-	-	-	2	-	3

## CO PO Mapping

COGNITIVE LEVEL	REVISED BLOOMS TAXONOMY KEYWORDS
L1	List, define, tell, describe, identify, show, label, collect, examine, tabulate, quote, name, who, when, where, etc.
L2	summarize, describe, interpret, contrast, predict, associate, distinguish, estimate, differentiate, discuss, extend
L3	Apply, demonstrate, calculate, complete, illustrate, show, solve, examine, modify, relate, change, classify, experiment, discover.
L4	Analyze, separate, order, explain, connect, classify, arrange, divide, compare, select, explain, infer.
L5	Assess, decide, rank, grade, test, measure, recommend, convince, select, judge, explain, discriminate, support, conclude, compare, summarize.

PROGRAM OUTCOMES (PO), PROGRAM SPECIFIC OUTCOMES (PSO)				CORRELATION LEVELS	
PO1	Engineering knowledge	PO7	Environment and sustainability	0	No Correlation
PO2	Problem analysis	PO8	Ethics	1	Slight/Low
PO3	Design/development of solutions	PO9	Individual and team work	2	Moderate/ Medium

PO4	Conduct investigations of complex problems	PO10	Communication	3	Substantial/High
PO5	Modern tool usage	PO11	Project management and finance		
PO6	The Engineer and society	PO12	Life-long learning		
PSO1	Develop applications using different stacks of web and programming technologies				
PSO2	Design and develop secure, parallel, distributed, networked, and digital systems				
PSO* 3	Apply software engineering methods to design, develop, test and manage software systems.				
PSO4	Develop intelligent applications for business and industry				

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