

Sub: Theory of Computation

Sub Code: BCS503

Ans ① Input string $w = 0 + ((1 * 0) - 1)$ LRD

$$E \Rightarrow E + T$$

$$\Rightarrow T + T \quad (E \rightarrow T)$$

$$\Rightarrow F + T \quad (T \rightarrow F)$$

$$\Rightarrow 0 + T \quad (F \rightarrow 0)$$

$$\Rightarrow 0 + F \quad (T \rightarrow F)$$

$$\Rightarrow 0 + (E) \quad (F \rightarrow (E))$$

$$\Rightarrow 0 + (E - T) \quad (E \rightarrow E - T)$$

$$\Rightarrow 0 + (T - T) \quad (E \rightarrow T)$$

$$\Rightarrow 0 + (F - T) \quad (T \rightarrow F)$$

$$\Rightarrow 0 + ((E) - T) \quad (F \rightarrow (E))$$

$$\Rightarrow 0 + ((T) - T) \quad (E \rightarrow T)$$

$$\Rightarrow 0 + ((T * F) - T) \quad (T \rightarrow T * F)$$

$$\Rightarrow 0 + ((F * F) - T) \quad (T \rightarrow F)$$

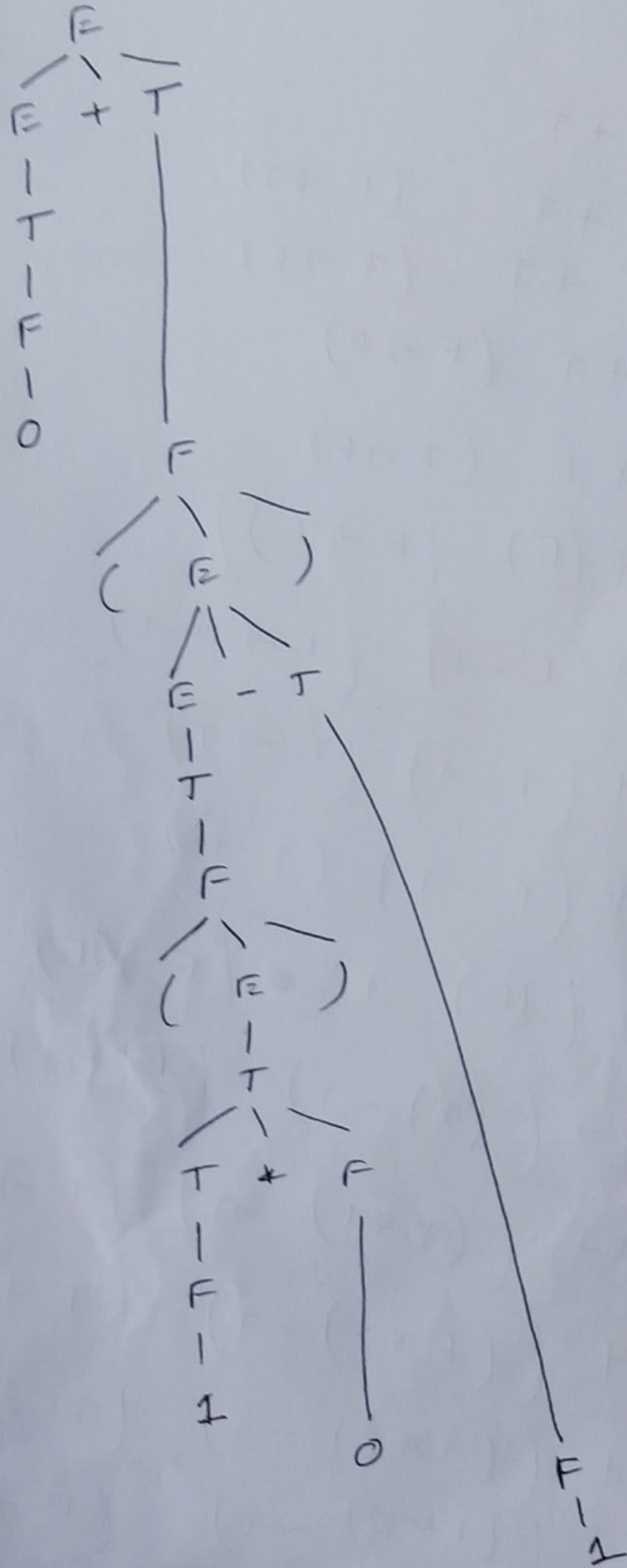
$$\Rightarrow 0 + ((1 * F) - T) \quad (F \rightarrow 1)$$

$$\Rightarrow 0 + ((1 * 0) - T) \quad (F \rightarrow 0)$$

$$\Rightarrow 0 + ((1 * 0) - F) \quad (T \rightarrow F)$$

$$\Rightarrow 0 + ((1 * 0) - 1) \quad (F \rightarrow 1)$$

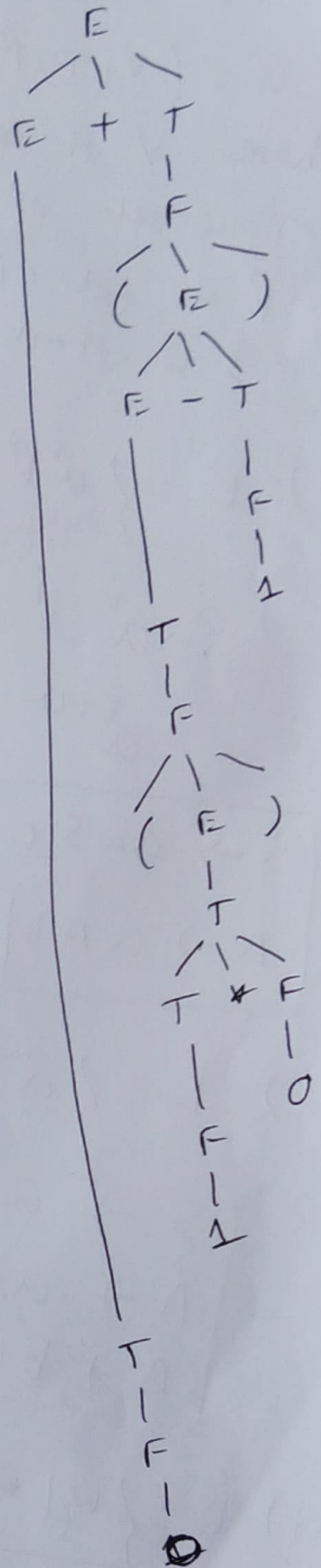
LAD Parse Tree



RMD

(2)

- $E \rightarrow E + T$
- $\Rightarrow E + F \quad (T \rightarrow F)$
- $\Rightarrow E + (E) \quad (F \rightarrow (E))$
- $\Rightarrow E + (E - T) \quad (E \rightarrow E - T)$
- $\Rightarrow E + (E - F) \quad (T \rightarrow F)$
- $\Rightarrow E + (E - 1) \quad (F \rightarrow 1)$
- $\Rightarrow E + (T - 1) \quad (E \rightarrow T)$
- $\Rightarrow E + (F - 1) \quad (T \rightarrow F)$
- $\Rightarrow E + ((E) - 1) \quad (F \rightarrow (E))$
- $\Rightarrow E + ((T) - 1) \quad (E \rightarrow T)$
- $\Rightarrow E + ((T * F) - 1) \quad (T \rightarrow T * F)$
- $\Rightarrow E + ((T * 0) - 1) \quad (F \rightarrow 0)$
- $\Rightarrow E + ((F * 0) - 1) \quad (T \rightarrow F)$
- $\Rightarrow E + ((1 * 0) - 1) \quad (F \rightarrow 1)$
- $\Rightarrow T + ((1 * 0) - 1) \quad (E \rightarrow T)$
- $\Rightarrow F + ((1 * 0) - 1) \quad (T \rightarrow F)$
- $\Rightarrow 1 + ((1 * 0) - 1) \quad (F \rightarrow 0)$



② CFG is defined by 4 tuples.

$$G = (V, T, P, S)$$

where V is set of Variables or Non terminals.

T is set of terminals

P is set of rules or productions

S is start symbol.

$$(i) L = \{ a^i b^j c^k \mid i = j + 2k \text{ and } j, k \geq 1 \}$$

$$a^i b^j c^k$$

$$a^{j+2k} b^j c^k$$

$$\Rightarrow a^{2k} a^j b^j c^k$$

$$\begin{array}{l} S \rightarrow a a S c \mid a a A c \\ A \rightarrow a A b \mid a b \end{array}$$

$$(ii) L = \{ a^m b^n \mid m \neq n, \text{ and } m, n \geq 1 \}$$

$$\begin{array}{l} S \rightarrow a S b \mid a A b \mid a B b \\ A \rightarrow a A \mid a \\ B \rightarrow b B \mid b \end{array}$$

$$(iii) L = \{ w \mid w \text{ contains balanced parenthesis} \}$$

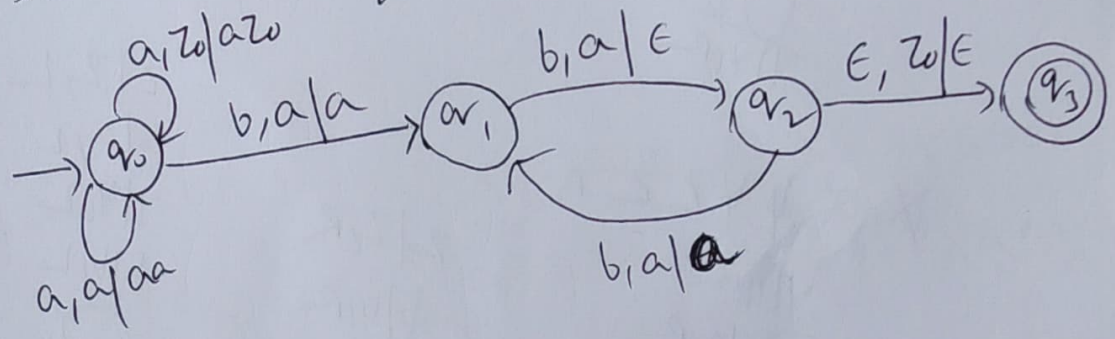
$$S \rightarrow (S) \mid \{S\} \mid [S] \mid SS$$

Ans 3. PDA is defined by 7-tuples

$$M = (Q, \Sigma, \Gamma, \delta, q_0, z_0, F)$$

- Where Q is a set of states
- Σ is set of input symbols
- Γ is stack symbols
- δ is transition function
- q_0 is start state
- z_0 is initial stack symbol
- F is final state.

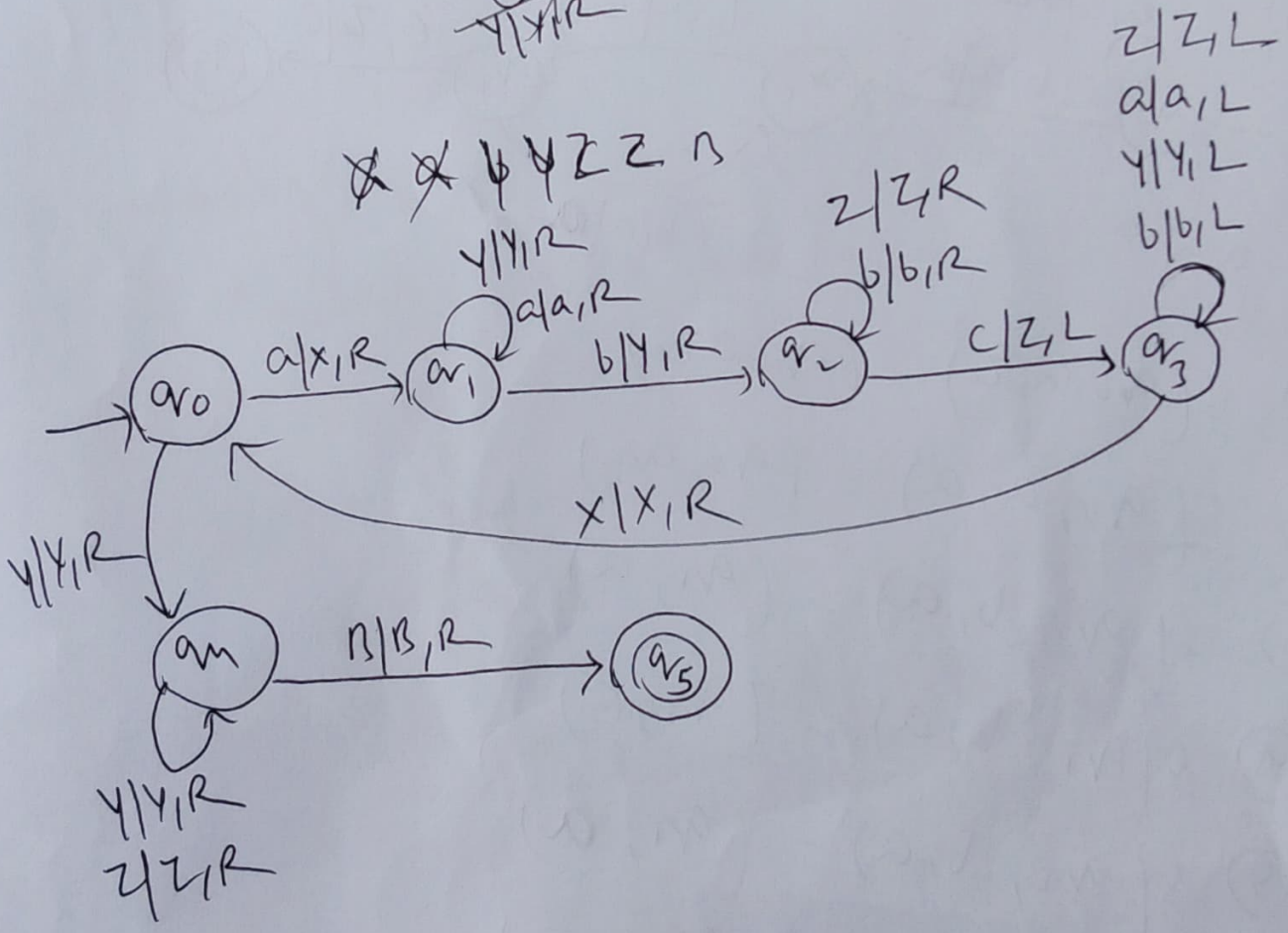
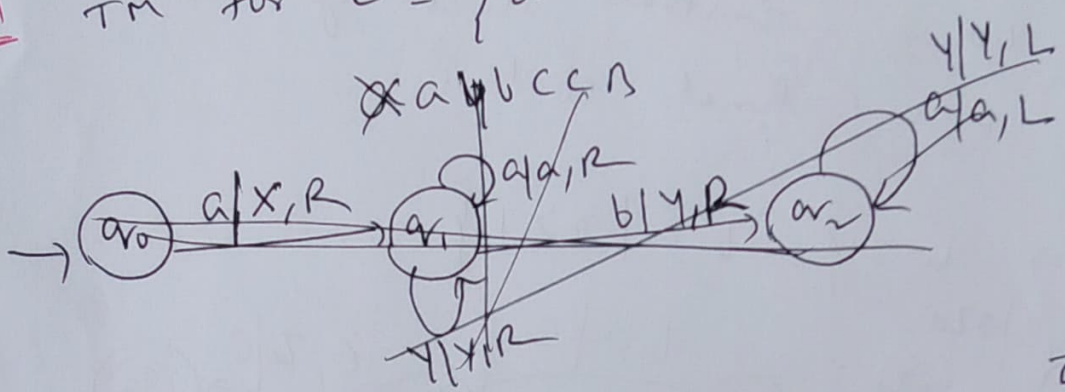
PDA for $L = \{a^m b^{2m} \mid m \geq 1\}$



- ① $\delta(q_0, a, z_0) = (q_0, a z_0)$
- ② $\delta(q_0, a, a) = (q_0, a a)$
- ③ $\delta(q_0, b, a) = (q_1, a)$
- ④ $\delta(q_1, b, a) = (q_2, E)$
- ⑤ $\delta(q_1, b, a) = (q_1, a)$
- ⑥ $\delta(q_2, E, z_0) = (q_3, E)$

$q_0, aaabbbbb, z_0 \vdash q_0, aabbbbb, az_0 \vdash q_0, abbbbb, aaz_0$
 $\vdash q_0, bbbbb, aaz_0 \vdash q_1, bbbbb, aaz_0$
 $\vdash q_2, bbbb, aaz_0 \vdash q_1, bbb, aaz_0$
 $\vdash q_2, bb, aaz_0 \vdash q_1, b, aaz_0$
 $\vdash q_2, \epsilon, z_0 \vdash q_3, \epsilon, \epsilon$ Accepted

Ans 4 TM for $L = \{a^m b^m c^m \mid m \geq 1\}$.



- ① $\delta(q_0, a) = (q_1, X, R)$
- ② $\delta(q_1, a) = (q_1, a, R)$
- ③ $\delta(q_1, Y) = (q_1, Y, R)$
- ④ $\delta(q_1, b) = (q_2, Y, R)$
- ⑤ $\delta(q_2, b) = (q_2, b, R)$
- ⑥ $\delta(q_2, Z) = (q_2, Z, R)$
- ⑦ $\delta(q_2, c) = (q_3, Z, L)$
- ⑧ $\delta(q_3, b) = (q_3, b, L)$
- ⑨ $\delta(q_3, Y) = (q_3, Y, L)$
- ⑩ $\delta(q_3, a) = (q_3, a, L)$
- ⑪ $\delta(q_3, Z) = (q_3, Z, L)$
- ⑫ $\delta(q_3, X) = (q_0, X, R)$
- ⑬ $\delta(q_0, Y) = (q_m, Y, R)$
- ⑭ $\delta(q_m, Y) = (q_m, Y, R)$
- ⑮ $\delta(q_m, Z) = (q_m, Z, R)$
- ⑯ $\delta(q_m, b) = (q_5, b, R)$

ID for aabbcc

$q_0 a a b b c c \epsilon \vdash X q_1 a b b c c \epsilon \vdash X a q_1 b b c c \epsilon$
 $\vdash X a Y q_2 b b c c \epsilon \vdash X a Y b q_2 c c \epsilon \vdash X a Y q_3 b Z c \epsilon$
 $\vdash X a q_3 Y b Z c \epsilon \vdash X q_3 a Y b Z c \epsilon \vdash q_3 X a Y b Z c \epsilon$
 $\vdash X q_0 a Y b Z c \epsilon \vdash X X q_1 Y b Z c \epsilon \vdash X X Y q_1 b Z c \epsilon$
 $\vdash X X Y q_2 Z c \epsilon \vdash X X Y Y Z q_2 c \epsilon \vdash X X Y Y q_3 Z Z \epsilon$
 $\vdash X X Y q_3 Y Z Z \epsilon \vdash X X q_3 Y Y Z Z \epsilon \vdash X q_3 X Y Y Z Z \epsilon$
 $\vdash X X q_0 Y Y Z Z \epsilon \vdash X X Y q_m Y Z Z \epsilon \vdash X X Y Y q_m Z Z \epsilon$
 $\vdash X X Y Y Z q_m \epsilon \vdash X X Y Y Z Z q_m \epsilon \vdash X X Y Y Z Z \epsilon q_5$

Accepted

⑤ (a) A grammar is in CNF, if the productions are in the following form.

$$\begin{array}{l} A \rightarrow BC \\ A \rightarrow a \end{array}$$

Conversion of CFG to CNF

Step 1 :

$$\text{Null set} = \{B, D\}$$

After removing NULL productions,

$$S \rightarrow ABC \mid BAn \mid AC \mid Ba \mid aB \mid a$$

$$A \rightarrow aA \mid BaC \mid aa \mid aC$$

$$B \rightarrow bnb \mid a \mid D \mid bb$$

$$C \rightarrow CA \mid AC$$

Step 2 Removal of useless symbols

C, D are useless.

$$S \rightarrow BAn \mid Ba \mid aB \mid a$$

$$A \rightarrow aA \mid aa$$

$$B \rightarrow bnb \mid a \mid bb$$

Now A is useless

$$S \rightarrow BAn \mid Ba \mid aB \mid a$$

$$B \rightarrow bnb \mid a \mid bb$$

Step 3 No unit production.

Step 4 Convert to CNF

$$\begin{aligned} S &\rightarrow ZB \mid BX \mid XB \mid a \\ B &\rightarrow PY \mid a \mid YY \\ X &\rightarrow a \\ Y &\rightarrow b \\ Z &\rightarrow BX \\ P &\rightarrow YB \end{aligned}$$

Ans 5. (b)

CFG to PDA

$$\textcircled{1} \delta(q, \epsilon, \epsilon) = \left\{ (q, \epsilon + T), (q, \epsilon - T), (q, T) \right\}$$

$$\textcircled{2} \delta(q, \epsilon, T) = \left\{ (q, T * F), (q, F) \right\}$$

$$\textcircled{3} \delta(q, \epsilon, F) = \left\{ (q, (\epsilon)), (q, 0), (q, 1) \right\}$$

$$\textcircled{4} \delta(q, +, +) = (q, \epsilon)$$

$$\textcircled{10} \delta(q, -, -) = (q, \epsilon)$$

$$\textcircled{11} \delta(q, *, *) = (q, \epsilon)$$

$$\textcircled{12} \quad s(q, c, c) = (q, \epsilon)$$

$$\textcircled{13} \quad s(q, \gamma, \gamma) = (q, \epsilon)$$

$$\textcircled{14} \quad s(q, 0, 0) = (q, \epsilon)$$

$$\textcircled{15} \quad s(q, 1, 1) = (q, \epsilon)$$