Step-by-Step Solutions: Internal Assessment Test 2 – May 2025 Analysis & Design of Algorithms

Question 1: Backtracking - Sum of Subset Problem

Backtracking is a general algorithmic technique that considers searching every possible combination to solve an optimization problem. It incrementally builds candidates to the solution and abandons a candidate ("backtracks") as soon as it determines that the candidate cannot lead to a valid solution.

Given $S = \{5, 10, 12, 13, 15, 18\}$ and d = 30

We find all subsets that sum to 30 using backtracking.

Steps:

- 1. Start from index 0, current sum = 0, empty subset.
- 2. Recursively include or exclude each element.
- 3. Track current sum and subset.
- 4. If current sum equals 30, print the subset.
- 5. If current sum exceeds 30 or index exceeds length, backtrack.

Solutions:

- {12, 13, 5}
- {10, 12, 8}

Question 2: LC Branch and Bound - Knapsack Problem

Weights = $\{2,1,3,2\}$, Profits = $\{12,10,20,5\}$, Capacity = 5

Use LC Branch and Bound Tree to find optimal profit.

Steps:

- 1. Sort items by profit/weight ratio.
- 2. Use a priority queue for nodes (based on upper bound).
- 3. Branch into including or excluding an item.
- 4. Keep track of maximum profit found.

Optimal Solution: Include item 1 (2kg, 12), item 2 (1kg, 10), item 4 (2kg, 5)

Question 3: Heap and Heap Sort

Heap is a complete binary tree satisfying heap property (Max-Heap or Min-Heap).

Bottom-Up Heap Construction:

1. Start from last non-leaf node and heapify up to root.

Heap Sort for list [2,9,7,6,5,8]:

- 1. Build Max Heap: [9,6,8,2,5,7]
- 2. Swap root with last: [7,6,8,2,5,9]
- 3. Heapify and repeat.

Sorted List: [2,5,6,7,8,9]

Question 4: AVL Tree

AVL Tree is a self-balancing binary search tree with height balance factor -1, 0, or 1.

Worst Case Efficiency: O(log n) for insert, delete, search

Keys: 5,6,8,3,2,4,7

Insertions & Rotations:

- Insert 5: Root
- Insert 6: Right of 5
- Insert 8: Right of $6 \rightarrow$ imbalance \rightarrow Left Rotation at 5
- Insert 3: Left of 5
- Insert 2: Left of 3
- Insert 4: Right of 3 → imbalance → Left-Right Rotation at 5
- Insert 7: Insert to right subtree → Rebalance

Final AVL Tree is balanced.

Question 5: Complexity Classes

- i) P Problem: Solvable in polynomial time, e.g., Binary Search.
- ii) NP Problem: Verifiable in polynomial time, e.g., Hamiltonian Path.
- iii) NP-Complete: In NP and all NP problems reduce to it, e.g., SAT.

iv) NP-Hard: As hard as NP-Complete, may not be in NP, e.g., Halting Problem.

Question 6: Backtracking vs Branch and Bound & Horspool Algorithm

- a) Backtracking vs Branch and Bound:
- Backtracking: Explores all possibilities, used for constraint satisfaction.
- Branch and Bound: Uses bound function to prune branches, for optimization problems.
- b) Horspool Shift Table Algorithm in C:

```
void shiftTable(char pattern[], int table[], int m) {
   int i;
   for (i = 0; i < 256; i++) table[i] = m;
   for (i = 0; i < m - 1; i++) table[(int)pattern[i]] = m - 1 - i;
}</pre>
```