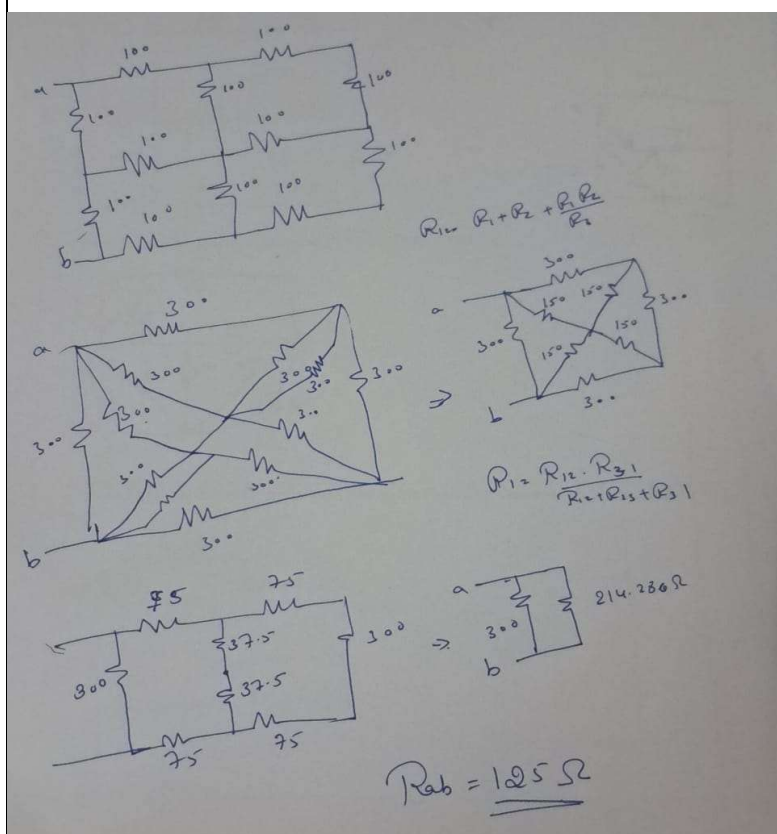
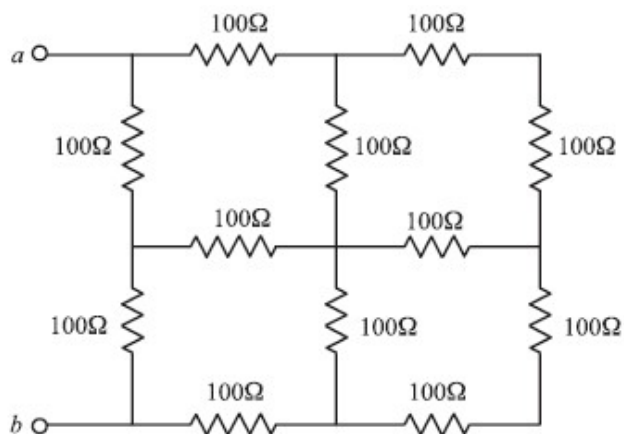


Scheme and solution

Mark
s

1. Find the equivalent resistance R_{ab} for the circuit shown.

[10]

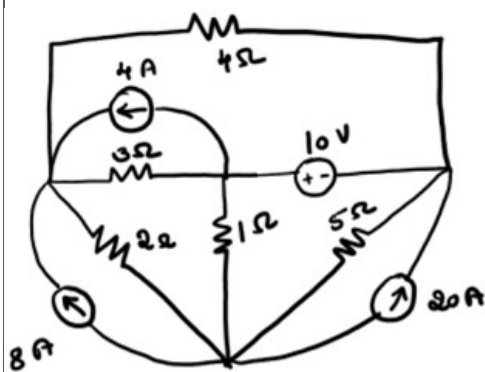


Each step: $2 \times 4 = 8$ Marks

Correct answer: 2 Marks

2. Determine all the node voltages in the circuit using nodal analysis.

[10]



$$V_B - V_C = 10 \text{ V} \quad \text{--- (1)}$$

At supernode B-C.

$$\frac{V_B}{1} + \frac{V_B - V_A}{3} + \frac{V_C}{5} - 20 + \frac{V_C - V_A}{4} = 0$$

$$\frac{V_A}{2} - 8 + \frac{V_A - V_B}{3} - 4 + \frac{V_A - V_C}{4} = 0$$

$$V_A \left(\frac{1}{2} + \frac{1}{3} + \frac{1}{4} \right) - \frac{V_B}{3} - \frac{V_C}{4} = 12 \quad \text{--- (2)}$$

$$-V_A \left(\frac{1}{3} + \frac{1}{4} \right) + V_A \left(1 + \frac{1}{3} \right) + V_C \left(\frac{1}{5} + \frac{1}{4} \right) = 16 \quad \text{--- (3)}$$

$V_A = 18.15 \text{ V}$ $V_B = 17.43 \text{ V}$ $V_C = 7.43 \text{ V}$

Identifying supernode: 2 Marks

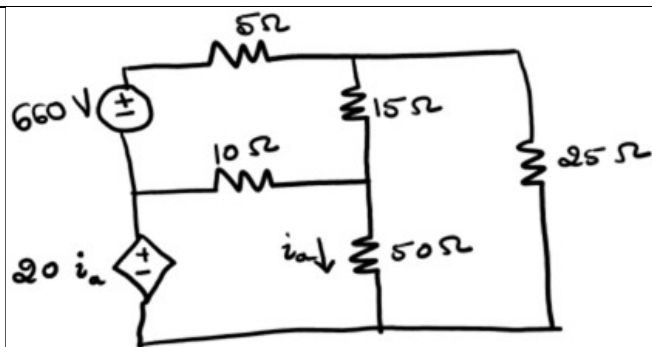
Nodal analysis equation: 3 Marks

Solution: 3 Marks

Correct answer: 2 Marks

3. Use mesh analysis to find the power delivered by the dependent source in the circuit.

[10]



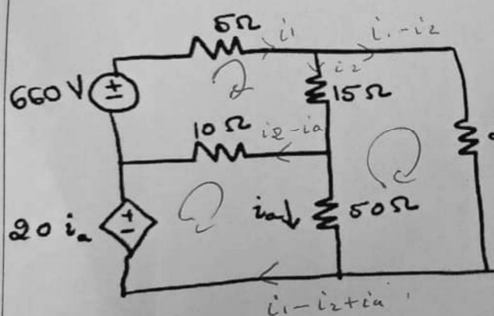
3.

Use mesh analysis to find the power delivered by the dependent source in the circuit.

[10]

CO2

L3



$$\begin{aligned}
 660 - 5i_1 - 15i_2 - 10(i_2 - i_1) &= 0 \\
 -5i_1 - 25i_2 + 10i_1 &= -660 \quad (1) \\
 -5i_1 - 25i_2 + 10i_1 - 50i_a &= 0 \\
 +20i_a + 10i_2 - 10i_1 - 50i_a &= 0 \quad (2) \\
 10i_2 - 40i_a &= 0 \quad (3) \\
 15i_2 - 25i_1 + 25i_2 + 50i_a &= 0 \\
 -25i_1 + 40i_2 + 50i_a &= 0 \quad (4)
 \end{aligned}$$

$$\begin{aligned}
 i_1 &= 42 \\
 i_2 &= 20 \\
 i_a &= 5
 \end{aligned}$$

$$P = 20i_a \times (i_1 - i_2 + i_a) = 20 \times 5 \times (42 + 5) = 2.7 \text{ kW}$$

KVL:2Marks

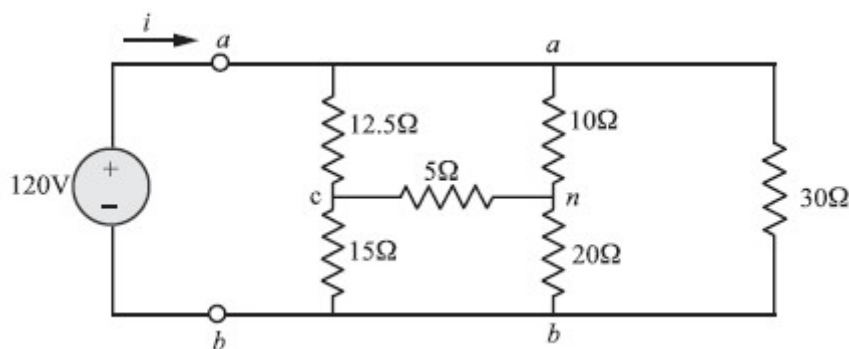
Solution to get current values: 6 Marks

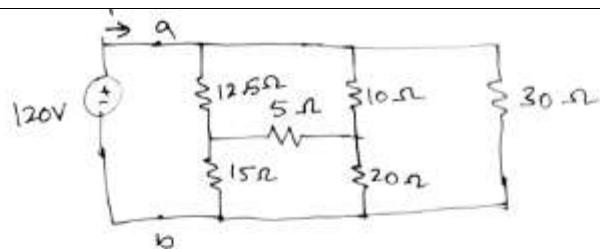
Power: 2Marks

4.

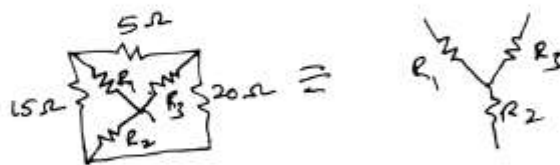
Obtain the equivalent resistance R_{ab} for the circuit and hence find i .

[10]





$15\Omega, 5\Omega, 20\Omega$ Delta network is converted into Star network as

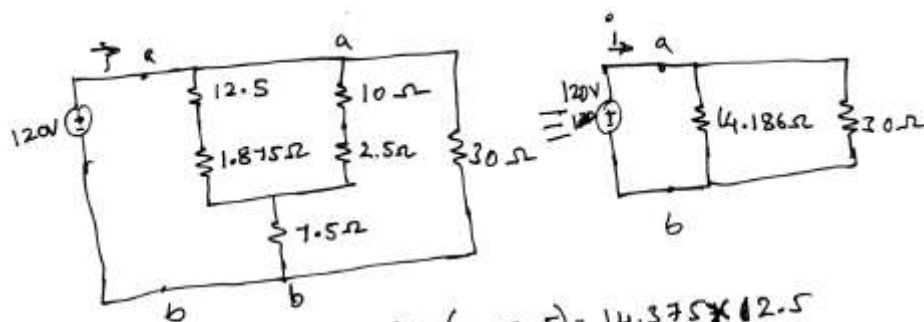


$$R_1 = \frac{15 \times 5}{15 + 5 + 20} = \frac{75}{40} = 1.875\Omega$$

$$R_2 = \frac{15 \times 20}{15 + 5 + 20} = 7.5\Omega$$

$$R_3 = \frac{20 \times 5}{15 + 5 + 20} = 2.5\Omega$$

.....4Marks



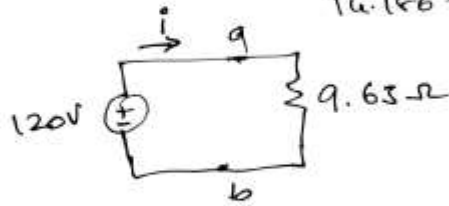
$$(12.5 + 1.875) \parallel (10 + 2.5) = \frac{14.375 \times 12.5}{14.375 + 12.5} = 6.686\Omega$$

$$6.686\Omega \text{ in series with } 7.5\Omega = 6.686 + 7.5 = 14.186\Omega$$

.....4Marks

14.186 Ω is in parallel with 30 Ω

$$(14.186 || 30) = \frac{14.186 \times 30}{14.186 + 30} = 9.63 \Omega$$



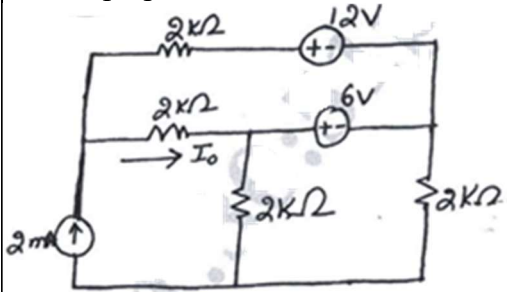
Equivalent resistance between
a, terminals a & b is
 $R_{ab} = 9.63 \Omega$

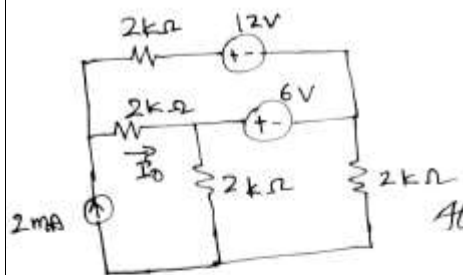
Then
$$i = \frac{120V}{9.63 \Omega} = 12.46 A$$

.....2 Marks

5. State superposition theorem. Use the superposition theorem to find I_0 in the circuit shown below:

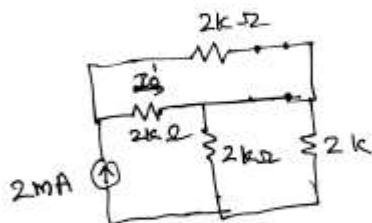
[3]



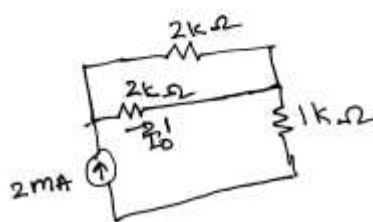


There are three sources
Hence I_0 can be found using
activating each source alone
using superposition theorem
Hence $I_0 = I_0' + I_0'' + I_0'''$

Deactivate 6V and 12V source to find current I_0'



$$2k \parallel 2k = \frac{2k \times 2k}{2k + 2k} = 1k\Omega$$

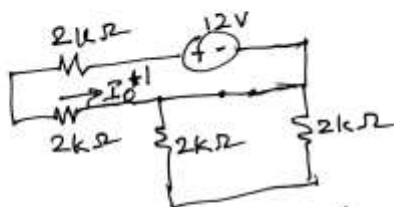


Using current divider formula

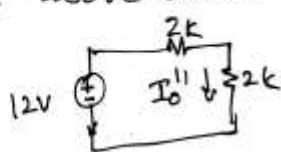
$$I_0' = \frac{2mA \times 2k\Omega}{(2k + 2k)\Omega}$$

$$I_0' = \frac{4}{4k\Omega} = 1mA$$

Deactivate 6V and 2mA source to find I_0''

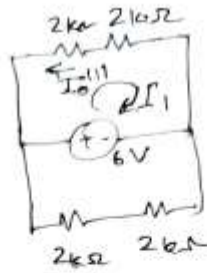
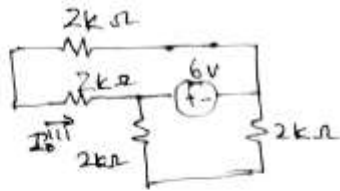


The above circuit can be further simplified as



$$I_0'' = \frac{12V}{4k\Omega} = 3mA$$

Deactivate 2mA and 12V source to find I_0^{III} circuit will be.



$$I_1 = -I_0^{III}$$

Applying KVL to mesh containing current I_1

$$I_1$$

$$-6 + (2k + 2k)I_1 = 0$$

$$4kI_1 = 6$$

$$I_1 = \frac{6}{4k} = 1.5 \text{ mA}$$

$$I_1 = -I_0^{III} = 1.5 \text{ mA}$$

$$\text{Hence } \boxed{I_0^{III} = -1.5 \text{ mA}}$$

$$\text{So current } I_0 = I_0^I + I_0^{II} + I_0^{III}$$

$$= 1 \text{ mA} + 3 \text{ mA} - 1.5 \text{ mA}$$

$$\boxed{I_0 = 2.5 \text{ mA}}$$

Each case: $3 \times 3 = 9$ marks

Final current 1 Mark

6. Find current through galvanometer of 50Ω using thevenin's theorem for the circuit shown below:

[10]



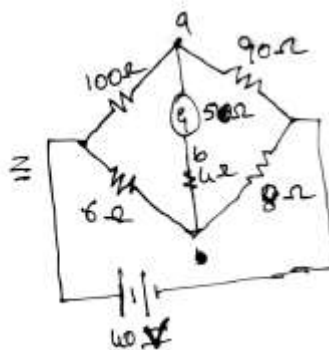
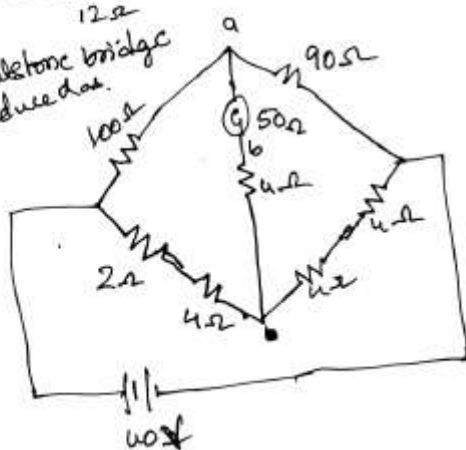
Three 12Ω resistors can be reduced to a star network as.

$$R_1 = R_2 = R_3 = \frac{12 \times 12}{12 + 12 + 12}$$

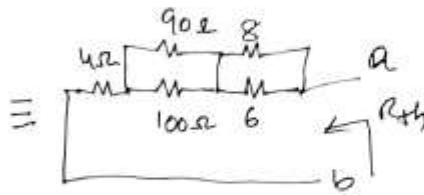
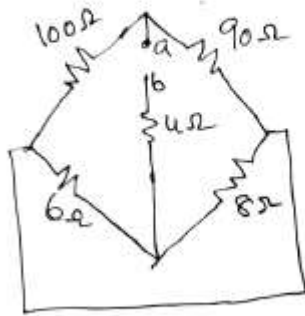
$$R_1 = R_2 = R_3 = 4\Omega$$



above wheatstone bridge can be reduced as.



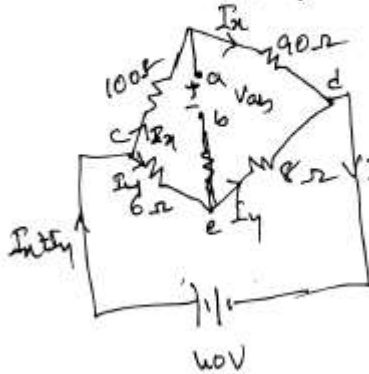
Let us remove part B of the circuit and find thevenin's equivalent resistance R_{th} by deactivating ^{40V} voltage source.



$$(90 \parallel 100) + (8 \parallel 6) + 4 = (47.38 + 3.42 + 4) \Omega$$

$$R_{th} = 54.8 \Omega$$

Find V_{th} (V_{ab}):



Apply KVL to caba loop

$$100I_x + V_{ab} - 6I_y = 0 \rightarrow (1)$$

Apply KVL to adba loop

$$90I_x - 8I_y - V_{ab} = 0 \rightarrow (2)$$

Apply KVL to cedc loop

$$-40 + 6I_y + 8I_y = 0$$

$$I_y = 40 / 14 = 2.857 A$$

R_{th} calculation: 4 marks

V_{th} : 4 marks

I: 2 Marks