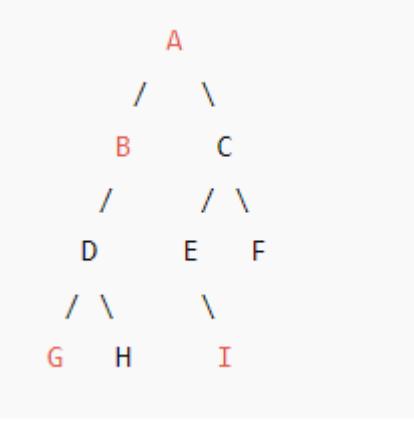


Internal Assessment Test II –January 2026  
 ANSWER KEY

| Sub:                                  | Data Structures and Applications   |           |        |            | Sub Code: | BCS304    | Branch:     | AIML/CSE<br>AIML |         |
|---------------------------------------|--|-----------|--------|------------|-----------|-----------|-------------|------------------|---------|
| Date:                                 | 8.1.26   | Duration: | 90 min | Max Marks: | 50        | Sem/Sec : | III A, B, C | OBE              |         |
| <u>Answer any FIVE FULL Questions</u> |  |           |        |            |           |           | MARKS       | CO               | RB<br>T |
| 1 a                                   | <p>Define Binary Search tree. Construct a binary search tree (BST) for the following elements: 100, 85, 45, 55, 120, 20, 70, 90, 115, 65, 130, 145. Traverse using in-order, pre-order, and post-order traversal techniques.</p> <p>BST definition and construction -3Marks</p> <p><b>A Binary Search Tree (BST)</b> is a binary tree in which:</p> <ul style="list-style-type: none"> <li>• Each node has <b>at most two children</b>.</li> <li>• The <b>left subtree</b> of a node contains values <b>less than</b> the node's key.</li> <li>• The <b>right subtree</b> of a node contains values <b>greater than</b> the node's key</li> </ul> <pre>           100           /   \         85     120         / \   / \       45  90  115  130       / \           \     20  55         145       \     70       \     65     </pre> <p>Traversals-3x1=3marks</p> <p>In-order:</p> <p>20, 45, 55, 65, 70, 85, 90, 100, 115, 120, 130, 145</p> <p>Pre-order:</p> <p>100, 85, 45, 20, 55, 70, 65, 90, 120, 115, 130, 145</p> <p>Post-order:</p> | 6M        |        | CO4        | L3        |           |             |                  |         |

|    |   |    |     |     |
|----|---|----|-----|-----|
|    | 20, 65, 70, 55, 45, 90, 85, 115, 145, 130, 120, 100   |    |     |     |
| 1b | <p>Construct a binary tree from the Inorder and Postorder sequence given below</p> <p>In-order: GDHBAEICF</p> <p>Post-order: GHDBIEFCA</p> <p>Construction of Tree-4Marks</p>  <pre>       A      / \     B   C    /   / \   D   E   F  / \   \ G   H   I   </pre>   | 4M | CO4 | L 3 |
| 2a | <p>Write C function for Depth First Search(DFS) and show the graph traversal by taking an example.</p> <p>DFS</p> <p>Algorithm-3Marks</p> <pre> void DFS(int v) {     int i;     visited[v] = 1;     // Mark current     vertex as visited     printf("%d ", v);     // Visit the vertex      for (i = 1; i &lt;= n; i++)     {         if (adj[v][i] == 1 &amp;&amp; visited[i] == 0)         {             DFS(i);             // Recursive call         }     } }   </pre> | 5M | CO4 | L 2 |

|    |  |     |     |     |
|----|--|-----|-----|-----|
|    | <p>}</p> <p>Example-3Marks</p>   |     |     |     |
| 2b | <p>Define graph. Explain Adjacency list and Adjacency matrix by taking an example.</p> <p>Graph-1Mark</p> <p>A <b>graph</b> is a mathematical structure used to represent relationships between objects.</p> <ul style="list-style-type: none"> <li>• It consists of: <ul style="list-style-type: none"> <li>◦ <b>Vertices (nodes):</b> Represent objects.</li> <li>◦ <b>Edges (links):</b> Represent connections or relationships between the vertices.</li> </ul> </li> <li>• Notation: <math>\mathbf{G} = (\mathbf{V}, \mathbf{E})</math> <ul style="list-style-type: none"> <li>◦ <math>\mathbf{V}</math> = set of vertices</li> <li>◦ <math>\mathbf{E}</math> = set of edges</li> </ul> </li> </ul> <p>Adjacency List-1 Mark</p> <p><b>Adjacency List</b></p> <ul style="list-style-type: none"> <li>• Each vertex has a <b>list of vertices it is connected to</b></li> </ul> <p>Example -1Mark</p> <p>Adjacency Matrix -1Mark</p> <p><b>Adjacency Matrix</b></p> <ul style="list-style-type: none"> <li>• A <b>2D array</b> of size <math>n \times n</math> where <math>n</math> = number of vertices</li> <li>• Element <code>matrix[i][j] = 1</code> if there is an edge from vertex <code>i</code> to vertex <code>j</code> (0 otherwise)</li> </ul> <p>Example -1Mark</p> | 5M  | CO4 | L 2 |
| 3a | <p>Define hashing. Explain different hashing functions with examples.</p> <p>Hashing-2Marks</p> <p>Hashing function-</p> <p>i)Division Method 2Marks</p> <p>ii)MidsquareHash Function 2 Marks</p> <p>iii)Folding Method 2Marks</p> <p>iv)Digit analysis-1Mark</p> <p>v)Converting keys to integers-1Mark</p>   | 10M | CO5 | L 2 |

## Hashing – 2 Marks

### Definition:

Hashing is a technique used to map **keys** to **indices of a hash table** using a **hash function** to allow **fast insertion, deletion, and searching**.

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## Hashing Function – Methods

### i) Division Method – 2 Marks

- Formula:

$$h(k) = k \bmod m \quad mh(k) = k \bmod m \quad mh(k) = k \bmod m$$

- **k** = key, **m** = size of the hash table
- Example: Key = 123, Table size = 10  $\rightarrow 123 \bmod 10 = 3$   $123 \bmod 10 = 3$
- **Pros:** Simple and fast
- **Cons:** Table size should preferably be a prime number to reduce collisions

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### ii) Mid-Square Method – 2 Marks

- Steps:

1. Square the key:  $k^2$
2. Take the middle digits as the hash value

- Example: Key = 123  $\rightarrow 123^2 = 15129$   $123^2 = 15129$   $123^2 = 15129 \rightarrow$  middle digits = 512  $\rightarrow$  index
- **Pros:** Good distribution
- **Cons:** Slightly more computation

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### iii) Folding Method – 2 Marks

- Steps:

1. Divide key into equal parts
2. Add the parts together
3. Apply modulo table size (optional)

- Example: Key = 123456, divide into 3 parts: 12, 34, 56 → 12+34+56 = 102 → index
- **Pros:** Handles large keys easily

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#### iv) Digit Analysis – 1 Mark

- Use **specific digits of the key** as the hash value
- Example: Key = 45678 → use last 2 digits → 78 → index

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#### v) Converting Keys to Integers – 1 Mark

- For **alphanumeric keys**, convert letters to numbers before hashing
- Example: Key = "ABC" → A=1, B=2, C=3 → 123 → use in hash function

|    |   |     |     |     |
|----|---|-----|-----|-----|
| 4a | <p>What is a leftist tree? Give the C declaration of it .Explain how meld operation is applied to two minimum leftist tree with the help of an example.</p> <p><b>Leftist Tree</b></p> <p><b>Definition (2 Marks):</b><br/> A <b>Leftist Tree</b> is a type of <b>priority queue</b> implemented as a binary tree where:</p> <ol style="list-style-type: none"> <li>1. It satisfies the <b>heap property</b>: the key at each node is smaller (min-leftist) or larger (max-leftist) than the keys of its children.</li> <li>2. It satisfies the <b>leftist property</b>: the <b>rank</b> (distance to nearest null node, also called <b>null path length, npl</b>) of the <b>left child</b> is always greater than or equal to the rank of the right child.</li> </ol> <p>The purpose of the leftist property is to keep the tree <b>skewed to the left</b>, which ensures that <b>merging (meld) operations are efficient</b>.</p> | 10M | CO5 | L 2 |
|----|---|-----|-----|-----|

### C Declaration (2 Marks)

```
typedef struct LeftistNode {  
    int key;                      // Value of the node  
    int npl;                      // Null Path Length  
    struct LeftistNode *left;      // Pointer to left  
    child  
    struct LeftistNode *right;    // Pointer to right  
    child  
} LeftistNode;  
  
typedef LeftistNode* LeftistTree; // Pointer to  
root of the tree
```

- **npl** = null path length = shortest distance from node to a node without two children (null node).

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### Meld Operation (6 Marks)

#### Meld Operation:

The **meld** operation combines two leftist trees into one while maintaining **heap** and **leftist** properties.

Steps (for **min-leftist tree**):

1. Compare the roots of both trees. Make the root with the **smaller key** the new root.
2. Recursively **meld** the **right child** of this root with the other tree.
3. Swap **left and right children** if necessary to maintain the leftist property (**npl(left) ≥ npl(right)**).
4. Update the **npl** of the root.

5a

Write C Functions for the following,  
i) Inserting a node at the beginning of a Doubly linked list.

C function-2.5Marks

```
Node* insertAtBeginning(Node* head, int newData) {  
    // Step 1: Allocate memory for the new node  
    Node* newNode = (Node*)malloc(sizeof(Node));  
    if (!newNode) {  
        printf("Memory allocation failed\n");  
        return head; // return existing head if malloc fails  
    }
```

```
// Step 2: Assign data to the new node
```

5M

CO3

L 2

|  |  |  |  |
|--|--|--|--|
|  | <pre> newNode-&gt;data = newData; newNode-&gt;prev = NULL; // New node becomes the first node newNode-&gt;next = head; // Next points to the current head  // Step 3: Update previous head's prev pointer if list is not empty if (head != NULL) {     head-&gt;prev = newNode; }  // Step 4: Return new node as the new head return newNode; } </pre> |  |  |
|--|--|--|--|

|  |  |  |  |
|--|--|--|--|
|  | <p>ii) Deleting a node at the end of the Doubly linked list.</p> <p>C function-2.5Marks</p> <pre> Node* deleteAtEnd(Node* head) {     // If the list is empty, nothing to delete     if (head == NULL) {         printf("List is empty.\n");         return NULL;     }      // If the list has only one node     if (head-&gt;next == NULL) {         free(head);         return NULL; // List becomes empty     }      // Traverse to the last node     Node* temp = head;     while (temp-&gt;next != NULL) {         temp = temp-&gt;next;     }      // Update previous node's next to NULL     temp-&gt;prev-&gt;next = NULL;      // Free the last node     free(temp);      // Return head of the list     return head; } </pre> |  |  |
|--|--|--|--|

|    |  |    |         |
|----|--|----|---------|
| 5b | <p>Write C functions for the following,</p> <p>a) To search an item within a SLL(Singly Linked List)</p> <p>C function-2 .5Marks</p> <pre> Node* searchSLL(Node* head, int key) {     Node* temp = head;      // Traverse the list     while (temp != NULL) { </pre> | 5M | CO3 L 2 |
|----|--|----|---------|

```

    if (temp->data == key) {
        return temp; // Item found, return pointer to the node
    }
    temp = temp->next;
}

// Item not found
return NULL;
}

```

b) To concatenate two SLL.

C function-2.5Marks

```

Node* concatenateSLL(Node* head1, Node* head2) {
    // If the first list is empty, return the second list
    if (head1 == NULL)
        return head2;

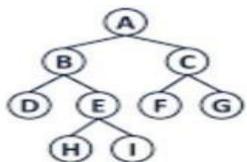
    // Traverse to the end of the first list
    Node* temp = head1;
    while (temp->next != NULL) {
        temp = temp->next;
    }

    // Link the last node of list1 to head of list2
    temp->next = head2;

    return head1; // Return the head of the concatenated list
}

```

6a Write recursive C functions for inorder, preorder and postorder traversals of a binary tree. Also, find all the traversals for the given tree.



Each traversal -3 Marks

**Preorder** ABDEHICFG

**INORDER:** DBHEIAFCG

**POSTODER:** DHIEBFGCA

C function for each traversal -3Marks

/ Preorder traversal: Root -> Left -> Right

```

void preorder(Node* root) {
    if (root == NULL) return;
    printf("%c ", root->data);
    preorder(root->left);
    preorder(root->right);
}

```

// Inorder traversal: Left -> Root -> Right

```

void inorder(Node* root) {
    if (root == NULL) return;
    inorder(root->left);
    inorder(root->right);
}

```

6M CO3 L 3

```

        printf("%c ", root->data);
        inorder(root->right);
    }

// Postorder traversal: Left -> Right -> Root
void postorder(Node* root) {
    if (root == NULL) return;
    postorder(root->left);
    postorder(root->right);
    printf("%c ", root->data);
}

```

|    |  |    |     |     |
|----|--|----|-----|-----|
| 6b | Define Binary tree. Explain the representation of a binary tree with a suitable example. | 4M | CO3 | L 2 |
|----|--|----|-----|-----|

### Definition (2 Marks)

A **binary tree** is a hierarchical data structure in which each node has at most **two children**, called **left child** and **right child**.

Array and Linked list representation of Binary tree-2Marks

