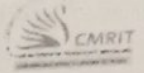


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Internal Assessment Test - I

Sub:	Calculus and Linear Algebra					Code:	18MAT 11
Date:	15/10/2018	Duration:	90 mins	Max Marks:	50	Sem:	I
						Section:	A to F ,N and O

Question 1 is compulsory, Answer any 6 questions from 2 to 8.

	Marks	OBE	
		CO	RBT
1) a) Derive with usual notations $\tan \phi = r \frac{d\theta}{dr}$	[5]	CO1	L3
b) Find the angle between the radius vector and tangent for the curve $r^2 \cos 2\theta = a^2$.	[3]	CO1	L3
2) Find the pedal equation of the curve $r^m = a^m (\cos m\theta + \sin m\theta)$.	[7]	CO1	L3
3) Find the Radius of curvature of the given curve $y^2 = \frac{4a^2(2a-x)}{x}$ where the curve meets the x axis.	[7]	CO1	L3

- 4) Find the coordinates of centre of curvature at any point of the parabola $y^2 = 4ax$. And hence show that the evolute is $27ay^2 = 4(x - 2a)^3$. [7]
- 5) Solve the system of equations by Gauss-seidel method, carryout 4 iterations $2x+17y+4z=35$; $28x+4y-z=32$; $x+3y+10z=24$. [7]
- 6) Examine the following system for consistency and solve them if consistent, using Gauss elimination method $5x+y+z+w=4$; $x+7y+z+w=12$; $x+y+6z+w=-5$; $x+y+z+4w=-6$. [7]
- 7) Reduce the matrix to the diagonal form [7]

$$\begin{bmatrix} -1 & 3 \\ -2 & 4 \end{bmatrix} .$$

- 8) Find the largest eigenvalue and the corresponding eigenvector of the matrix A by using power method by taking initial vector as [7]

$$[1,1,1]^T \quad \text{and} \quad A = \begin{bmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{bmatrix} .$$

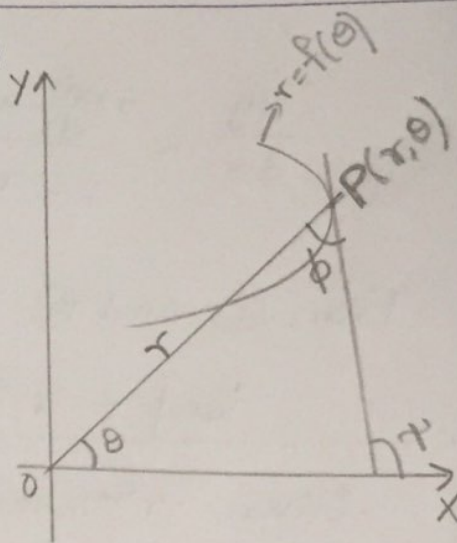
CO1	L3
CO6	L3
CO6	L3
CO6	L3
CO6	L3

Calculus & Linear Algebra - 18MAT11

1.a Consider a polar curve $r = f(\theta)$ and a point $P(r, \theta)$ on the curve.

Let PT be the tangent to the curve at P , meeting the X -axis at the point T .

Let ψ be the angle made by the tangent with the +ve X -axis, and θ be the angle between the radius vectors OP and the tangent PT .



————— (1)

From the figure we have, $\psi = \phi + \theta$

We know that $\frac{dy}{dx} = \text{slope of the tangent}$.

Also slope = $\tan \psi$

$$\therefore \frac{dy}{dx} = \tan \psi = \tan(\phi + \theta)$$

$$\frac{dy}{dx} = \frac{\tan \phi + \tan \theta}{1 - \tan \phi \tan \theta} \quad \rightarrow \text{①}$$

————— (1)

Since (x, y) is the cartesian coordinates of the point P , we have $x = r \cos \theta$ & $y = r \sin \theta$

$$\text{Then } \frac{dx}{d\theta} = -r \sin \theta + \cos \theta \frac{dr}{d\theta}$$

$$\text{and } \frac{dy}{d\theta} = r \cos \theta + \sin \theta \frac{dr}{d\theta}$$

$$\therefore \frac{dy}{dx} = \frac{\frac{dy}{d\theta}}{\frac{dx}{d\theta}} = \frac{r \cos \theta + \sin \theta \frac{dr}{d\theta}}{-r \sin \theta + \cos \theta \frac{dr}{d\theta}} \quad \text{————— (1)}$$

Dividing both Nr and Dr of RHS by $\cos\theta \frac{dr}{d\theta}$ (2)

we get,
$$\frac{dy}{dx} = \frac{r \frac{d\theta}{dr} + \tan\theta}{-r \frac{d\theta}{dr} \tan\theta + 1}$$

$$\frac{dy}{dx} = \frac{r \frac{d\theta}{dr} + \tan\theta}{1 - r \frac{d\theta}{dr} \tan\theta} \rightarrow (2)$$

From (1) and (2) we get

$$\tan\phi = r \frac{d\theta}{dr}$$

1.b

Given $r^2 \cos 2\theta = a^2$

Taking log on BS

$$2 \log r + \log(\cos 2\theta) = 2 \log a \quad \text{--- (1)}$$

Diff w.r.to θ

$$2 \frac{1}{r} \frac{dr}{d\theta} + \frac{1}{\cos 2\theta} (-\sin 2\theta) 2 = 0$$

$$\frac{1}{r} \frac{dr}{d\theta} = \tan 2\theta \quad \text{--- (1)}$$

we have $\cot \phi = \frac{1}{r} \frac{dr}{d\theta}$

$$\therefore \cot \phi = \tan 2\theta = \tan(\frac{\pi}{2} - 2\theta)$$

$$\cot \phi = \cot(\frac{\pi}{2} - 2\theta)$$

$$\Rightarrow \phi = \frac{\pi}{2} - 2\theta \quad \text{--- (1)}$$

2 Given $r^m = a^m (\cos m\theta + \sin m\theta) \rightarrow (1)$

Taking log on BS

$$m \log r = m \log a + \log(\cos m\theta + \sin m\theta) \quad \text{--- (2)}$$

Diff w.r.to θ

$$m \frac{1}{r} \frac{dr}{d\theta} = 0 + \frac{1}{\cos m\theta + \sin m\theta} (-\sin m\theta + \cos m\theta) m$$

$$\frac{1}{r} \frac{dr}{d\theta} = \frac{\cos m\theta - \sin m\theta}{\cos m\theta + \sin m\theta} \quad (3)$$

Dividing both Nr + Dr of RHS by $\cos m\theta$

$$\frac{1}{r} \frac{dr}{d\theta} = \frac{1 - \tan m\theta}{1 + \tan m\theta}$$

$$\frac{1}{r} \frac{dr}{d\theta} = \tan\left(\frac{\pi}{4} - m\theta\right)$$

We have $\cot \phi = \frac{1}{r} \frac{dr}{d\theta}$

$$\therefore \cot \phi = \tan\left(\frac{\pi}{4} - m\theta\right)$$

$$= \cot\left(\frac{\pi}{2} - \frac{\pi}{4} + m\theta\right)$$

$$\cot \phi = \cot\left(\frac{\pi}{4} + m\theta\right)$$

$$\Rightarrow \phi = \frac{\pi}{4} + m\theta \quad \text{--- (2)}$$

Consider $p = r \sin \phi$

$$p = r \sin\left(\frac{\pi}{4} + m\theta\right)$$

$$= r \left[\sin \frac{\pi}{4} \cos m\theta + \cos \frac{\pi}{4} \sin m\theta \right] \quad \text{--- (2)}$$

$$p = \frac{r}{\sqrt{2}} [\cos m\theta + \sin m\theta]$$

From (1) $\frac{r^m}{a^m} = \cos m\theta + \sin m\theta$

$$\therefore p = \frac{r}{\sqrt{2}} \frac{r^m}{a^m} = \frac{r^{m+1}}{a^m \sqrt{2}}$$

$$\Rightarrow \underline{\underline{r^{m+1} = p a^m \sqrt{2}}} \quad \text{--- (1)}$$

3

$$\text{Given } y^2 = \frac{4a^2(2a-x)}{x}$$

4

The curve meets the x -axis $\Rightarrow y = 0$.

$$\therefore \frac{4a^2(2a-x)}{x} = 0 \Rightarrow 4a^2(2a-x) = 0$$

$$\Rightarrow x = 2a$$

Thus $(2a, 0)$ is the point on the curve. — (1)

$$y^2 = \frac{4a^2(2a-x)}{x}$$

Diff w.r. to x

$$2yy_1 = \frac{x[4a^2(0-1)] - 4a^2(2a-x)(1)}{x^2}$$

$$= \frac{-4a^2x - 8a^3 + 4a^2x}{x^2}$$

$$2yy_1 = \frac{-8a^3}{x^2}$$

$$y_1 = \frac{-4a^3}{x^2y}$$

At $(2a, 0)$, $y_1 = \infty$ — (2)

$$\text{Now } x_1 = \frac{dx}{dy} = \frac{1}{\frac{dy}{dx}} = \frac{1}{y_1} = \frac{-x^2y}{4a^3}$$

At $(2a, 0)$, $x_1 = 0$ — (1)

$$x_2 = \frac{-1}{4a^3} [x^2y_1 + y_2x]$$

$$= \frac{-1}{4a^3} [x^2y_1 + 2xy]$$

At $(2a, 0)$

$$x_2 = -$$

$$x_2 = \frac{-1}{4a^3} [x^2 + 4ax_1] \quad (5)$$

At $(2a, 0)$

$$x_2 = \frac{-1}{4a^3} [4a^2 + 0]$$

$$= \frac{-1}{a} \quad \text{--- (1)}$$

$$f = \frac{(1+x_1^2)^{3/2}}{x_2} \quad \text{--- (1)}$$

$$= \frac{(1+0)^{3/2}}{-1/a}$$

$$f = -a$$

$$\underline{|f| = a} \quad \text{--- (1)}$$

4

$$y^2 = 4ax$$

$$\frac{\partial y}{\partial x} = \frac{2a}{y}$$

$$y_1 = \frac{2a}{y} \quad \text{--- (1)}$$

$$y_2 = \frac{\partial}{\partial y} \left(\frac{-1}{y^2} \right) y_1$$

$$y_2 = -\frac{2a}{y^2} \left(\frac{2a}{y} \right) = \frac{-4a^2}{y^3} \quad \text{--- (1)}$$

$$\bar{x} = x - \frac{y_1(1+y_1^2)}{y_2} \quad \text{--- (1)}$$

$$= x + \frac{\left(\frac{2a}{y} \right) \left(1 + \frac{4a^2}{y^2} \right)}{-4a^2/y^3}$$

$$\bar{x} = x + \frac{1}{2a} (4ax + 4a^2)$$

(6)

$$\bar{x} = 3x + 2a \quad \text{--- (1)}$$

$$\bar{y} = y + \frac{(1+y^2)}{y^2} \quad \text{--- (1/2)}$$

$$= y + \frac{(1 + \frac{4a^2}{y^2})}{-4a^2/y^3}$$

$$\bar{y} = y - \frac{y}{4a^2} (y^2 + 4a^2)$$

$$= \frac{\cancel{4a^2}y - y^3 - \cancel{4a^2}y}{4a^2}$$

$$= \frac{-y^3}{4a^2} = \frac{-2x^{3/2}}{\sqrt{a}} \quad \text{--- (1)}$$

∴ The coordinates of centre of curvature

are $\bar{x} = 3x + 2a \rightarrow \textcircled{1}$

$\bar{y} = \frac{-2x^{3/2}}{\sqrt{a}} \rightarrow \textcircled{2}$

To find evolute we have to eliminate x from $\textcircled{1}$ & $\textcircled{2}$.

From $\textcircled{2}$ $(\bar{y})^2 = \frac{4x^3}{a}$

$$\Rightarrow (\bar{y})^2 = \frac{4}{a} \left(\frac{\bar{x} - 2a}{3} \right)^3$$

$$\Rightarrow (\bar{y})^2 = \frac{4(\bar{x} - 2a)^3}{27a}$$

$$\Rightarrow 27a(\bar{y})^2 = 4(\bar{x} - 2a)^3$$

$$\text{--- (2)}$$

∴ From $\textcircled{1}$
 $x = \frac{\bar{x} - 2a}{3}$

∴ The evolute is

$$27ay^2 = 4(x - 2a)^3$$

$$\begin{aligned}
 5. \quad & 2x + 17y + 4z = 35 \\
 & 28x + 4y - z = 32 \\
 & x + 3y + 10z = 24
 \end{aligned}$$

The given system is not diagonally dominant
 We re-arrange the equations to make it diagonally dominant.

$$\begin{aligned}
 28x + 4y - z &= 32 & |28| > |4| + |-1| \\
 2x + 17y + 4z &= 35 & |17| > |2| + |4| \\
 x + 3y + 10z &= 24 & |10| > |1| + |3|
 \end{aligned}$$

Now, the system is diagonally dominant.

$$\begin{aligned}
 \text{Thus, } x &= \frac{1}{28} (32 - 4y + z) & \text{--- (1)} \\
 y &= \frac{1}{17} (35 - 2x - 4z) & \text{--- (1)} \\
 z &= \frac{1}{10} (24 - x - 3y) & \text{--- (1)}
 \end{aligned}$$

Let $(x_0, y_0, z_0) = (0, 0, 0)$.

Iteration (1) :-

$$\begin{aligned}
 x_1 &= \frac{1}{28} [32 - 4(0) + 0] = 1.14286 \\
 y_1 &= \frac{1}{17} [35 - 2(0) - 4(0)] = 2.0588 \\
 z_1 &= \frac{1}{10} [24 - 0 - 3(0)] = 2.4
 \end{aligned}
 \text{--- (1)}$$

Iteration (2) :-

$$\begin{aligned}
 x_2 &= \frac{1}{28} (32 - 4y_1 + z_1) = 0.93446 \\
 y_2 &= \frac{1}{17} (35 - 2x_2 - 4z_1) = 1.38418 \\
 z_2 &= \frac{1}{10} (24 - x_2 - 3y_2) = 1.8913
 \end{aligned}
 \text{--- (1)}$$

Iteration (3):-

$$x_3 = \frac{1}{28} [32 - 4y_2 + z_2] = 1.01266$$

$$y_3 = \frac{1}{17} [35 - 2x_3 - 4z_2] = 1.4947$$

$$z_3 = \frac{1}{10} [24 - x_3 - 3y_3] = 1.850324$$

(8)
— (1)

Iteration (4):-

$$x_4 = \frac{1}{28} [32 - 4y_3 + z_3] = 0.9954$$

$$y_4 = \frac{1}{17} [35 - 2x_4 - 4z_3] = 1.50635$$

$$z_4 = \frac{1}{10} [24 - x_4 - 3y_4] = 1.84855$$

— (1)

$$\therefore x = 0.9954$$

$$y = 1.50635$$

$$z = 1.8485$$

— (1)

$$\begin{aligned}
 6. \quad & 5x + y + z + w = 4 \\
 & x + 7y + z + w = 12 \\
 & x + y + 6z + w = -5 \\
 & x + y + z + 4w = -6.
 \end{aligned}$$

The augmented matrix is,

$$(A:B) = \left(\begin{array}{cccc|c} 5 & 1 & 1 & 1 & 4 \\ 1 & 7 & 1 & 1 & 12 \\ 1 & 1 & 6 & 1 & -5 \\ 1 & 1 & 1 & 4 & -6 \end{array} \right) \quad \text{--- (1)}$$

$$R_1 \leftrightarrow R_2$$

$$\sim \left(\begin{array}{cccc|c} 1 & 7 & 1 & 1 & 12 \\ 5 & 1 & 1 & 1 & 4 \\ 1 & 1 & 6 & 1 & -5 \\ 1 & 1 & 1 & 4 & -6 \end{array} \right)$$

$$R_2 \rightarrow 5R_1 - R_2, \quad R_3 \rightarrow R_1 - R_3, \quad R_4 \rightarrow R_1 - R_4$$

$$\sim \left(\begin{array}{cccc|c} 1 & 7 & 1 & 1 & 12 \\ 0 & 34 & 4 & 4 & 56 \\ 0 & 6 & -5 & 0 & 17 \\ 0 & 6 & 0 & -3 & 18 \end{array} \right)$$

$$R_2 \rightarrow \frac{1}{34} R_2$$

$$\sim \left(\begin{array}{cccc|c} 1 & 7 & 1 & 1 & 12 \\ 0 & 1 & 2/17 & 2/17 & 28/17 \\ 0 & 6 & -5 & 0 & 17 \\ 0 & 6 & 0 & -3 & 18 \end{array} \right)$$

$R_3 \rightarrow 6R_2 - R_3, R_4 \rightarrow 6R_2 - R_4$

$$\sim \left(\begin{array}{cccc|c} 1 & 7 & 1 & 1 & 12 \\ 0 & 1 & 2/17 & 2/17 & 28/17 \\ 0 & 0 & 97/17 & 12/17 & -121/17 \\ 0 & 0 & 12/17 & 63/17 & -138/17 \end{array} \right)$$

(3)

$R_3 \rightarrow 17R_3, R_4 \rightarrow 17R_4$

$$\sim \left(\begin{array}{cccc|c} 1 & 7 & 1 & 1 & 12 \\ 0 & 1 & 2/17 & 2/17 & 28/17 \\ 0 & 0 & 97 & 12 & -121 \\ 0 & 0 & 12 & 63 & -138 \end{array} \right)$$

(1)

$R_4 \rightarrow 12R_3 - 97R_4$

$$\sim \left(\begin{array}{cccc|c} 1 & 7 & 1 & 1 & 12 \\ 0 & 1 & 2/17 & 2/17 & 28/17 \\ 0 & 0 & 97 & 12 & -121 \\ 0 & 0 & 0 & -5967 & 11934 \end{array} \right)$$

$R = R' = 4$.
The system is consistent and has unique solution.

$\Rightarrow -5967w = 11934$
 $w = \frac{11934}{-5967} = -2$

$97z + 12w = -121$
 $\Rightarrow z = \frac{1}{97} (-121 - 12(-2)) = -1$

Also, $y + \frac{2}{17}z + \frac{2}{17}w = \frac{28}{17} \Rightarrow y = \frac{28}{17} - \frac{2}{17}(-1) - \frac{2}{17}(-2)$
 $= 2$

And $x + 7y + z + w = 12 \Rightarrow x = 12 - 14 + 1 + 2 = 1$

(2) $\left\{ \begin{array}{l} x = 1 \\ y = 2 \\ z = -1 \\ w = -2 \end{array} \right.$

7. Let $A = \begin{pmatrix} -1 & 3 \\ -2 & 4 \end{pmatrix}$

The characteristic equation is

$$|A - \lambda I| = 0$$

$$\begin{vmatrix} -1-\lambda & 3 \\ -2 & 4-\lambda \end{vmatrix} = 0$$

$$(-1-\lambda)(4-\lambda) + 6 = 0$$

$$\Rightarrow -4 + \lambda - 4\lambda + \lambda^2 + 6 = 0$$

$$\Rightarrow \lambda^2 - 3\lambda + 2 = 0$$

$$\Rightarrow \lambda^2 - 2\lambda - 1\lambda + 2 = 0$$

$$\Rightarrow \lambda(\lambda - 2) - 1(\lambda - 2) = 0$$

$$\Rightarrow \lambda = 1, 2. \quad \leftarrow (2)$$

The eigenvalues are 1, 2.

The matrix equation is

$$(A - \lambda I)X = 0$$

$$\Rightarrow \begin{pmatrix} -1-\lambda & 3 \\ -2 & 4-\lambda \end{pmatrix} \begin{pmatrix} x \\ y \end{pmatrix} = \begin{pmatrix} 0 \\ 0 \end{pmatrix}$$

$$\Rightarrow (1-\lambda)x + 3y = 0$$

$$-2x + (4-\lambda)y = 0.$$

Let $\lambda = 1$

$$-2x + 3y = 0$$

$$-2x + 3y = 0$$

$$n = 2$$

$$\begin{pmatrix} -2 & 3 \\ -2 & 3 \end{pmatrix} \xrightarrow{R_2 \rightarrow R_1 - R_2} \begin{pmatrix} -2 & 3 \\ 0 & 0 \end{pmatrix} \quad (12)$$

$$n - r = 2 - 1 \\ = 1$$

$$r = 1.$$

$$\text{Let } y = k_1, \quad k_1 \neq 0$$

$$\Rightarrow x = \frac{3}{2} k_1$$

$$\text{Let } k_1 = 2.$$

$$\therefore X_1 = \begin{pmatrix} 3 \\ 2 \end{pmatrix} \quad \leftarrow (1|2)$$

$$\text{Let } \lambda = 2$$

$$-3x + 3y = 0$$

$$n = 2$$

$$-2x + 2y = 0$$

$$\begin{pmatrix} -3 & 3 \\ -2 & 2 \end{pmatrix} \xrightarrow{R_2 \rightarrow (-2)R_1 + (+3)R_2} \begin{pmatrix} -3 & 3 \\ 0 & 0 \end{pmatrix}$$

$$\text{Let } y = k_2, \quad k_2 \neq 0. \quad r = 1.$$

$$\Rightarrow x = k_2.$$

$$\text{Let } k_2 = 1$$

$$\therefore X_2 = \begin{pmatrix} 1 \\ 1 \end{pmatrix} \quad \leftarrow (1|1)$$

$$\text{The modal matrix is } P = \begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix}$$

$$\therefore P^{-1} = \frac{1}{1} \begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix}$$

(13)

$$P^{-1}AP = \begin{pmatrix} 1 & -1 \\ -2 & 3 \end{pmatrix} \begin{pmatrix} -1 & 3 \\ -2 & 4 \end{pmatrix} \downarrow \begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix}$$

$$= \begin{pmatrix} -1+2 & 3-4 \\ 2-6 & -6+12 \end{pmatrix} \begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix}$$

$$= \begin{pmatrix} 1 & -1 \\ -4 & 6 \end{pmatrix} \begin{pmatrix} 3 & 1 \\ 2 & 1 \end{pmatrix} \downarrow$$

$$= \begin{pmatrix} 3-2 & 1-1 \\ -12+12 & -4+6 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 0 & 2 \end{pmatrix}$$

$$= \text{Diag}(1, 2) = D$$

8. By data $X^{(0)} = \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix}$

$$AX^{(0)} = \begin{pmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{pmatrix} \begin{pmatrix} 1 \\ 1 \\ 1 \end{pmatrix} = \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = 1 \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = \lambda_1 X_1$$

$$AX_1 = \begin{pmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{pmatrix} \begin{pmatrix} 1 \\ 0 \\ 1 \end{pmatrix} = \begin{pmatrix} 2 \\ -2 \\ 2 \end{pmatrix} = 2 \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix} = \lambda_2 X_2$$

$$AX_2 = \begin{pmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{pmatrix} \begin{pmatrix} 1 \\ -1 \\ 1 \end{pmatrix} = \begin{pmatrix} 3 \\ -4 \\ 3 \end{pmatrix} = 4 \begin{pmatrix} 0.75 \\ -1 \\ 0.75 \end{pmatrix} = \lambda_3 X_3$$

$$Ax_3 = \begin{pmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{pmatrix} \begin{pmatrix} 0.75 \\ -1 \\ 0.75 \end{pmatrix} = \begin{pmatrix} 2.5 \\ -3.5 \\ 2.5 \end{pmatrix} = 3.5 \begin{pmatrix} 0.71 \\ -1 \\ 0.71 \end{pmatrix} \quad (14)$$

$$= \lambda_4 x_4$$

$$Ax_4 = \begin{pmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{pmatrix} \begin{pmatrix} 0.71 \\ -1 \\ 0.71 \end{pmatrix} = \begin{pmatrix} 2.42 \\ -3.42 \\ 2.42 \end{pmatrix} = 3.42 \begin{pmatrix} 0.708 \\ -1 \\ 0.708 \end{pmatrix}$$

$$= \lambda_5 x_5$$

$$Ax_5 = \begin{pmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{pmatrix} \begin{pmatrix} 0.708 \\ -1 \\ 0.708 \end{pmatrix} = \begin{pmatrix} 2.416 \\ -3.416 \\ 2.416 \end{pmatrix} = 3.416 \begin{pmatrix} 0.7073 \\ -1 \\ 0.7073 \end{pmatrix}$$

$$= \lambda_6 x_6$$

$$Ax_6 = \begin{pmatrix} 2 & -1 & 0 \\ -1 & 2 & -1 \\ 0 & -1 & 2 \end{pmatrix} \begin{pmatrix} 0.7073 \\ -1 \\ 0.7073 \end{pmatrix} = \begin{pmatrix} 2.4146 \\ -3.4146 \\ 2.4146 \end{pmatrix} \quad (15)$$

$$= 3.4146 \begin{pmatrix} 0.7071 \\ -1 \\ 0.7071 \end{pmatrix} +$$

$$= \lambda_7 x_7$$

Largest eigenvalue = 3.4146

Corresponding eigenvector = $\begin{pmatrix} 0.7071 \\ -1 \\ 0.7071 \end{pmatrix}$ } (2)