

INTERNAL ASSESSMENT TEST - 2.
Design of RC Structural Elements.
October - 2018

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Questi numb	Solution	Marks.
Q.1.	<p>* <u>Dimension</u>: $b = 300\text{mm}$, $\frac{1}{4}d = 20$, $d' = 30\text{mm}$, $D = d + d'$</p> <p>* <u>Effective length</u>: 6.8m.</p> <p>* <u>load calculation</u>: $DL + LL = 14.3\text{ kN/m}$ & $W_u = 21.45\text{ kN/m}$</p> <p>* <u>BM & SF</u>: $M_u = 104.06\text{ kN-m}$ $SF = 66.81\text{ kN}$</p> <p>* <u>Check for depth</u>: $d = 362.13\text{mm} < d_{\text{provi}}$</p> <p>* <u>Check for Section</u>: $M_{u1\text{m}} = 126.96\text{ kN-m} > M_u$</p> <p>* <u>Ast</u>: 850.83 mm^2</p> <p style="margin-left: 20px;">$A_{st\text{min}} = 188.43\text{ mm}^2$</p> <p style="margin-left: 20px;">$A_{st\text{max}} = 1048\text{ mm}^2$</p> <p style="margin-left: 20px;">no. of #c = 5 # or 16 ϕ</p> <p style="margin-left: 20px;">$A_{st\text{provi}} = 1005\text{ mm}^2$</p> <p>* <u>Detailing</u>:</p>	<p>01 mark.</p> <p>01</p> <p>02</p> <p>02</p> <p>01</p> <p>01</p> <p>02</p> <p>01</p> <p>01</p> <p>01</p> <p>02</p>
Q.2.	<p>* <u>Dimension</u>: $\frac{1}{4}l_x$</p> <p style="margin-left: 100px;">$\frac{1}{4}d$, $b = 1000\text{mm}$, $d' = 30\text{mm}$, $D =$</p> <p>* <u>Effective length</u>: $L_{eff} =$</p> <p>* <u>load calculation</u>:</p> <p>* <u>Mu & SF</u>:</p> <p>* <u>Check for depth</u>:</p> <p>* <u>Area of Steel</u>: A_{st}.</p> <p style="margin-left: 20px;">$A_{st\text{min}}$. — Distribution Steel —</p> <p style="margin-left: 20px;">Spacing: main steel.</p> <p style="margin-left: 40px;">: Distribut steel.</p> <p style="margin-left: 20px;">$A_{st\text{provi}}$:</p> <p>* <u>Check for Shear</u>:</p>	<p>02.</p> <p>01</p> <p>02</p> <p>02</p> <p>01</p> <p>02</p> <p>01</p> <p>02</p> <p>02</p> <p>02</p>

Solution

Q. 3. Dimension: $b_f = 2186.6 \text{ mm}$.
 $D = 500 \text{ mm}$.

Effective length: $l_{eff} = 7.3 \text{ m}$.

load calculation: $w = 29.2 \text{ kN/m}$
 $w_u = 43.68 \text{ kN/m}$

SF & Mu: $M_u = 296.96 \text{ kN-m}$.
 $V_u = 159.43 \text{ kN}$

check for depth:

check for section: $M_{u \text{ limit}} = 1003.17 \text{ Mpa}$.

$M_{uf} = 736.7 \text{ Mpa}$.

$\therefore M_{uf} > M_u \quad D_f > X_u \rightarrow \text{Rectangular section.}$

Ast calculation: $A_{st} = 607.44 \text{ mm}^2$.

$A_{st \text{ min}} = 2065.50 \text{ mm}^2$

$A_{st \text{ max}} = 43732 \text{ mm}^2$

no. of #c = 5 no.

check for shear: $\tau_v = 1.18 \text{ Mpa}$.

$\tau_c = 0.759 \text{ Mpa}$.

$S_v = 280 \text{ mm c/c}$.

check for deflection: $15.5 < 16$. OK.

1a) Given: $l = 6\text{ m}$
 $w_{DL} = 12\text{ kN/m}$
 $f_{ck} = 25\text{ Mpa}$
 $f_y = 415\text{ Mpa}$

Step 1: Fixing dimensions

$$\frac{L}{d} = 20$$

$$d = 300\text{ mm} + 100\text{ mm} = 400\text{ mm}$$

$$\text{Assume } d' = 50\text{ mm}$$

$$\therefore D = 450\text{ mm}$$

$$\text{Assume } b = 230\text{ mm}$$

Step 2: Lateral stability

$$60b = 60 \times 230 = 13800$$

$$\frac{250b^2}{d} = \frac{250 \times 230^2}{400} = 33062.5$$

Step 3: Effective length

$$1) \cdot l = L + d = 6 + 0.4 = 6.4\text{ m}$$

$$2) L = L + \frac{1}{2} ts + \frac{1}{2} ts = 6 + \frac{0.23}{2} + \frac{0.23}{2} = 6.23\text{ m}$$

$$\therefore l_{\text{eff}} = 6.23\text{ m}$$

Step 4: Load Calculations

$$DL = b \times D \times \delta = 0.23 \times 0.45 \times 25 = 2.58 \text{ KN/m}$$

$$LL = 12 \text{ KN/m}$$

$$\text{Total load } W = 14.58 \text{ KN/m}$$

$$W_u = 14.58 \times 1.5 \\ = 21.87 \text{ KN/m}$$

Step 5: BM and SF

$$M_u = \frac{W_u l^2}{8} = \frac{21.87 \times 6.23^2}{8} = 106.10 \text{ KN.m}$$

$$V_u = \frac{W_u l}{2} = \frac{21.87 \times 6.23}{2} = 68.12 \text{ KN}$$

Step 6: Check for depth

$$M_{u, \text{lim}} = 0.138 f_{ck} b d^2$$

$$d_{\text{req}} = \sqrt{\frac{M_{u, \text{lim}}}{0.138 f_{ck} b}} = \sqrt{\frac{106.10 \times 10^6}{0.138 \times 20 \times 230}}$$

$$d_{\text{req}} = 408.82 \text{ mm} \quad \therefore d = 410 \text{ mm}$$

Step 7: Ast calculation

$$M_u = 0.87 f_y A_{st} d \left[1 - \frac{f_y A_{st}}{f_{ck} b d} \right]$$

$$106.10 \times 10^6 = 0.87 \times 415 A_{st} \times 410 \left[1 - \frac{415 A_{st}}{20 \times 230 \times 410} \right]$$

$$6.10 \times 10^6 = 148030.5 A_{st} - 32.57 A_{st}^2$$

$$A_{st1} = 3653.31 \text{ mm}^2 \quad A_{st2} = 891.68 \text{ mm}^2$$

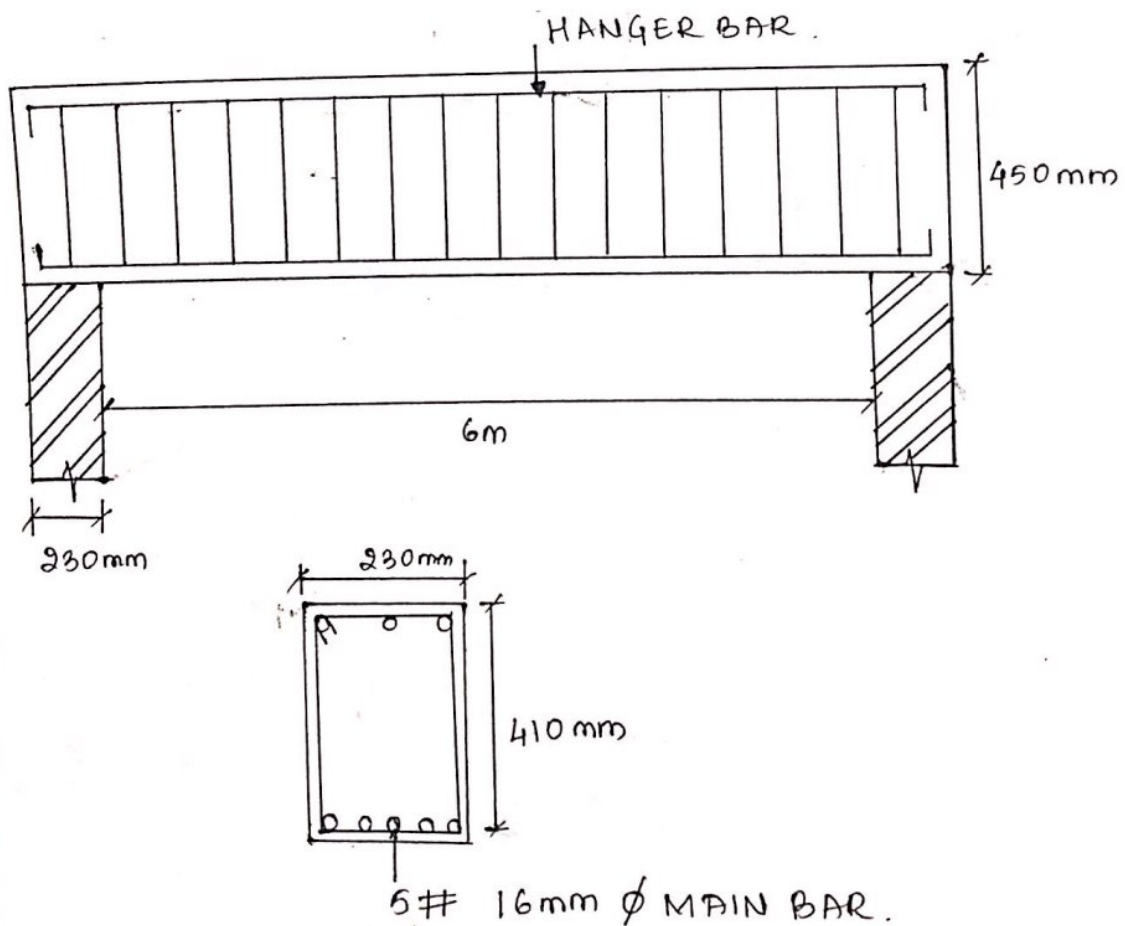
$$A_{st \text{ max}} = 0.04 b D = 0.04 \times 230 \times 450 = 4140 \text{ mm}^2$$

$$A_{st \text{ min}} = \frac{0.85 b d}{f_y} = \frac{0.85 \times 230 \times 410}{415} = 193.14 \text{ mm}^2$$

$$A_{st \text{ req}} = 892 \text{ mm}^2$$

$$\text{No of } \# 'C = \frac{A_{st \text{ req}}}{\frac{\pi}{4} \times \phi^2} = \frac{892}{\frac{\pi}{4} \times 16^2} = 4.4 \approx 5 \text{ Nos}$$

\therefore Provide 5 # - 16 mm ϕ as tension steel.



2) Design a RC slab supported of $6m \times 3m$. Live Load acting is 2 kN/m^2 and the floor finish is 0.6 kN/m^2 . Use M20 grade concrete and 415 grade steel.

Given:-

$$l_x = 3 \text{ m}$$

$$l_y = 6 \text{ m}$$

$$f_{ck} = 20 \text{ kN/m}^2$$

$$f_y = 415 \text{ kN/m}^2$$

$$FF = 0.6 \text{ kN/m}^2$$

$$L.L = 2 \text{ kN/m}^2$$

step 1:-

$$\frac{l_y}{l_x} = \frac{6}{3} = 2 \dots$$

\therefore Given slab is one way slab.

step 2:- Fixing dimensions.

$$\frac{l}{d} \text{ ratio} = 20 \times 1.3 \quad \therefore l = 3 \text{ m}$$

$$\frac{3000}{d} = 20 \times 1.3$$

$$\therefore d = 115.38 \text{ mm} \approx \underline{120 \text{ mm}}$$

$$d' = 20 \text{ mm}$$

$$D = d + d' = 120 + 20 = \underline{\underline{140 \text{ mm}}}$$

step 3:- Effective length.

$$l = L + \frac{1}{9} t_s + \frac{1}{2} t_s$$

$$l = 3000 + \frac{1}{9} \times 230 + \frac{1}{2} \times 230$$

$$l = \underline{\underline{3230 \text{ mm}}}$$

② $L + d = l$

$$l = 3000 + 140 = \cancel{3140} - 140$$

$$l = \underline{\underline{3140 \text{ mm}}}$$

$$\therefore l = \underline{\underline{3230 \text{ mm}}}$$

step 4: Load calculation \therefore assume $b = 1 \text{ m}$

$$W_D = \text{Dead load} = d \times f \times b = 0.14 \times 25 \times 1 = \underline{\underline{3.5 \text{ kN/m}}}$$

$$W_L = \text{Live load} = 2 \times 1 = 2 \text{ kN/m}^2$$

$$\text{Floor finish on slab} = 0.6 \times 1 = 0.6 \text{ kN/m}^2$$

step $\text{Total working load} = 6.1 \text{ kN/m}$

$$\text{ultimate load} = \underline{\underline{9.15 \text{ kN/m}}}$$

steps:- Bending moment & shear force.

$$M_u = \frac{w_u l^2}{8} = \frac{9.15 \times 3.23^2}{8} = 11.93 \text{ kN-m}$$

$$V_u = \frac{w_u l}{2} = \frac{9.15 \times 3.23}{2} = 14.77 \text{ kN-m}$$

step 6:- Check for depth

$$M_u = 0.138 f_{ck} b d^2$$

$$11.93 \times 10^6 = 0.138 \times 20 \times 1000 \times d^2$$

$$d_{\text{req}} = \underline{\underline{65.74 \text{ mm}}} < d_{\text{prov}} = 120 \text{ mm} \quad \text{Hence Safe.}$$

step 7:- Area of steel

$$M_u = 0.87 f_y A_{st} d \left(1 - \frac{f_y A_{st}}{f_{ck} b d} \right)$$

$$\frac{11.93}{\times 10^6} = 0.87 \times 415 \times A_{st} \times 120 \left(1 - \frac{415 A_{st}}{20 \times 1000 \times 120} \right)$$

$$A_{st} = \underline{\underline{289.88 \text{ mm}^2}}$$

$$\text{Spacing} = \frac{\frac{\pi \times 10^2}{4}}{289.88} = 270.89 \text{ mm}$$

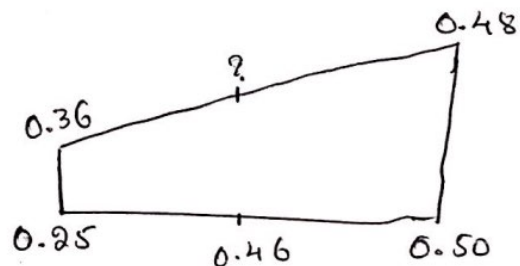
$$A_{st} \text{ Provid} = \frac{\pi \times 10^2}{4 \times 140} \times 1000 = \underline{\underline{560.99 \text{ mm}^2}}$$

step 8:- check for shear:

$$\tau_v = \frac{V_u}{b d} = \frac{25.18 \times 10^3}{1000 \times 120} = 0.123 \text{ N/mm}^2$$

$$P_t = \frac{100 A_{st}}{b d} = \frac{100 \times 560.99}{1000 \times 120} = \underline{\underline{0.46 \text{ mm}^2}}$$

$\tau_c =$	P_t
0.48	0.50
?	0.46
0.36	0.25



$$\tau_c = 0.36 + (0.48 - 0.36) \frac{(0.46 - 0.25)}{(0.50 - 0.25)}$$

$$\therefore \tau_c = \underline{\underline{0.46 \text{ N/mm}^2}}$$

$$z_v = 0.12 < z_c = 0.46$$

∴ Min shear reinforcement shall be provided.

step ∴ check for deflection.

$$(y/d)_{\text{allow}} = (y/d)_{\text{basic}} \times k_f \times k_c \times k_p = \underline{\underline{53.82}}$$

$$(y/d)_{\text{actual}} = \frac{3230}{120} \times \cancel{26.91} \times \cancel{2} \times \cancel{1} \times \cancel{1}$$

$$(y/d)_{\text{actu}} = \underline{\underline{26.91}} \times \cancel{2} \times \cancel{1} \times \cancel{1} = \underline{\underline{53.82}}$$

$$\cancel{(y/d)_{\text{allowable}}} = \cancel{(y/d)} \times \cancel{k_f} \times \cancel{k_c} \times \cancel{k_p}$$
$$= 20 \times$$

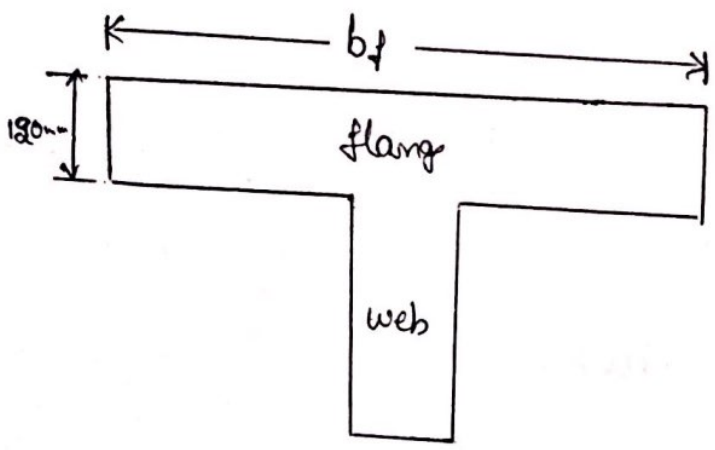
$$(y/d)_{\text{allowable}} = \cancel{26.91} \times \cancel{2} \times \cancel{1} \times \cancel{1}$$

$$(y/d)_{\text{allowable}} = \cancel{53.82}$$

$$(y/d)_{\text{actual}} < (y/d)_{\text{allowable}}$$

Hence safe.

be



$D_f = 180 \text{ mm}$

$l = 7 \text{ m}$

$f_{ck} = 20 \text{ mpa}$

Assume = $b_w = 300$

Step ①:- Determination

Pg No 37 & 38

$D_f = 180 \text{ mm}$

$d = \frac{1}{d} \text{ ratio}$

$d = \frac{7000}{20} = 350 \Rightarrow 350 + 100 = \underline{\underline{450 \text{ mm}}}$

$d' = \text{Assume} = 30$

$b_w = \text{Assume} = 300 \text{ mm}$

$\therefore D = d + d' = 450 + 30 = \underline{\underline{480 \text{ mm}}}$

step ②

$l_{eff} = L + d = 7000 + 450 = \underline{\underline{7450 \text{ mm}}}$

$l_{eff} = \text{clear span} + \frac{1}{9} \text{ thickness of support} + \frac{1}{9} \text{ thickness of support}$

$= 7000 + \frac{1}{9} \times 300 + \frac{1}{9} \times 300$

$= \underline{\underline{7300 \text{ mm}}}$

$\therefore l_{eff} = \underline{\underline{7300 \text{ mm}}}$

Step ③ :-

$$\begin{aligned} b_f &= \frac{d_{\text{eff}}}{6} + b_w + 6D_f \\ &= \frac{7300}{6} + 300 + 6(120) \\ b_f &= \underline{\underline{2236.66}} \end{aligned}$$

∴ c/c distance b/w slab (reqd) :-

$$b_f = \underline{\underline{3200 \text{ mm}}}$$

$$\therefore b_f = \underline{\underline{2236.66 \text{ mm}}}$$

Step ④ :- Load calculation :-

$$\begin{aligned} \text{Self weight of slab} &= D_f \times \text{c/c distance} \times \gamma \\ &= 0.12 \times 3.2 \times 25 = 9.6 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} \text{web} &= b_w \times (D - D_f) \times \gamma \\ &= 0.3 \times (0.48 - 0.12) \times 25 = 2.7 \text{ kN/m} \end{aligned}$$

$$\text{Flooring} = 0.6 \times 3.2 = 1.92 \text{ kN/m}$$

$$\text{Live load} = 4.6 \times 3.2 = 14.72 \text{ kN/m}$$

$$\therefore W_u = \underline{\underline{28.94 \text{ kN/m}}}$$

$$\therefore W_u = W \times 1.5 = 28.94 \times 1.5 = \underline{\underline{43.41 \text{ kN/m}}}$$

$$\text{Step ④} :- M_u = \frac{W_u l_{\text{eff}}^2}{8} = \frac{43.41 \times (7.3)^2}{8} = \underline{\underline{289.16 \text{ kNm}}}$$

$$V_u = \frac{W_u l_{\text{eff}}}{2} = \frac{43.41 \times 7.3}{2} = \underline{\underline{158.44 \text{ kNm}}}$$

Step ⑤ :-

$$\begin{aligned} M_{uf} &= 0.36 f_c k D_f b_f \left(d - \frac{D_f}{3}\right) \\ &= 0.36 \times 20 \times 120 \times 2236.66 \left(450 - \frac{120}{3}\right) \end{aligned}$$

$$M_{uf} = \underline{\underline{753.66 \text{ kN-m}}}$$

∴ $M_u < M_{uf}$ ∴ It is Rectangular Behaviour.

$$M_{lim} = 0.138 f_{ck} b_f d^3$$

$$= 0.138 \times 20 \times 2236.66 \times (450)^3$$

$$M_{u,lim} = \underline{\underline{1250.06 \text{ kN-m}}}$$

$M_u < M_{u,lim}$ \therefore It is singly reinforced.

6: Area of steel cal.

$$x = 0.87 f_y A_{st} d \left(1 - \frac{f_y A_{st}}{b_f d f_{ck}} \right)$$

$$39.16 \times 10^6 = 0.87 \times 415 \times A_{st} \times 450 \left(1 - \frac{415 \times A_{st}}{2236.66 \times 450 \times 20} \right)$$

$$A_{st,req} = \underline{\underline{1850.33 \text{ mm}^2}}$$

Assume dia of bar. = 20 mm

$$\therefore \text{No. of bars} = \frac{A_{st,req}}{\frac{\pi}{4} \times d^2} = \frac{1850.33}{\frac{\pi}{4} \times 20^2} = 5.88 \approx \underline{\underline{6 \text{ no.}}}$$

$$A_{st, max} = 0.04 b_f D = 0.04 \times 2236.66 \times 480 = \underline{\underline{42943.8 \text{ mm}^2}}$$

\therefore Provide #6 - 20 mm ϕ in Tension Zone.

$$A_{st} (prov) = 6 \times \frac{\pi}{4} \times 20^2 = \underline{\underline{1884.95 \text{ mm}^2}}$$

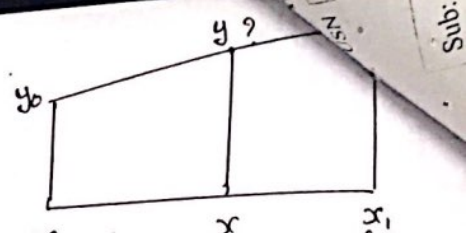
step (7): Check Shear :-

$$\tau_v = \frac{V_u}{bd} = \frac{158.44 \times 10^3}{300 \times 450} = \underline{\underline{1.17}}$$

$$P_f = \frac{100 (A_{st,prov})}{bd} = \frac{100 \times 1884.95}{300 \times 500} = \underline{\underline{1.25}}$$

By Interpolation

$$\tau_c = 0.67.$$



$\therefore \tau_c < \tau_v$ Minimum Design shear reinforcement is required.

Step ⑧ :-

4 legged vertical stirrups @ 8 ϕ

$$A_{sv} = 4 \times \frac{\pi}{4} \times 8^2 = \underline{\underline{801.06 \text{ mm}^2}}$$

Vertical stirrups \rightarrow Pg no. ⑦③

$$\begin{aligned} \therefore V_{us} &= V_u - b d \tau_c \\ &= 158.44 \times 10^3 - 300 \times 450 \times 0.67. \end{aligned}$$

$$V_{us} = \underline{\underline{67990 \text{ mm}}}$$

$$V_u = \frac{0.87 f_y A_{sv} d}{S_v} \Rightarrow 67990 = \frac{0.87 \times 415 \times 801.06 \times 450}{S_v}$$

$$\therefore S_v = \underline{\underline{480.46 \text{ mm}}}$$

$$\Rightarrow \text{Spacing} = 300 \text{ mm.}$$

$$\Rightarrow 0.75 \times d = 0.75 \times 450 = \underline{\underline{337.5 \text{ mm}}}$$

\therefore Provide 4 LVS = 8 ϕ @ 300 mm c/c

Step ⑨ :- check for deflection :-

$$\frac{L}{d} (\text{actual}) = \frac{7000}{450} = \underline{\underline{15.56}}$$

Pg no. ③⑧

$$f_x = 0.58 f_y \left(\frac{A_{d \text{ req}}}{A_{d \text{ prov}}} \right) = 0.58 \times 415 \left(\frac{1850.33}{1884.95} \right) = \underline{\underline{236.27 \text{ N/mm}^2}}$$

From Pg. No. ③⑧

$$\therefore K_f = 1.1,$$

$$K_f = 0.8,$$

$$K_c = 1$$

$$\frac{1}{d} (\text{allowable}) = \frac{7000}{20} \times 1.1 \times 0.8 \times 1 = \underline{\underline{17.6}}$$

$$\therefore \frac{L}{d} (\text{act}) < \frac{1}{d} (\text{allowable})$$

\therefore Hence it is safe.

