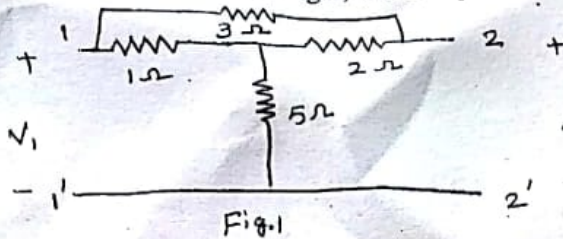


Internal Assessment Test II - Oct. 2018

Sub:	Network Analysis	Sub Code:	17EC35	Branch:	ECE
Date:	15/10/2018	Duration:	90 min's	Max Marks:	50
		Sem / Sec:	3A/3B/3C	OBE	

Answer any FIVE FULL Questions

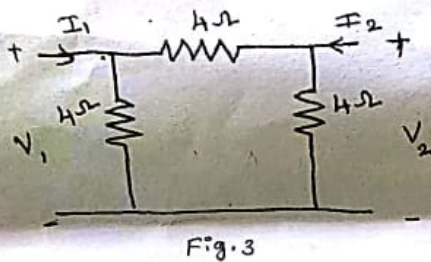
- 1 Obtain the relationship between 'y' and 'h' Parameters
Obtain the reciprocity condition for ABCD parameters. MARKS [10] CO6 L2
- 2 For the network shown in Fig.2, obtain Z parameters $AD-BC=1$ MARKS [10] CO6 L3



$$h = \begin{bmatrix} \frac{1}{h_{11}} & -\frac{h_{12}}{h_{11}} \\ \frac{h_{21}}{h_{11}} & \frac{\Delta h}{h_{11}} \end{bmatrix}$$

$$Z = \begin{bmatrix} 5.83 & 16/3 \\ 16/3 & 19/3 \end{bmatrix}$$

- 3 For the network shown in Fig.3, obtain ABCD parameters MARKS [10] CO6 L3



$$Y = \begin{bmatrix} \frac{1}{2} \times 10^{-3} & \frac{1}{4} \times 10^{-3} \\ -\frac{1}{4} \times 10^{-3} & \frac{1}{2} \times 10^{-3} \end{bmatrix}$$

$$T = \begin{bmatrix} 2 & 4000 \\ 0.75 \times 10^{-3} & 2 \end{bmatrix}$$

- 4 Show that the resonant frequency is the geometric mean of the half power frequencies. MARKS [10] CO5 L2

- 5 Derive the expression for the resonant frequency of the circuit where R_L resistance in inductor branch and R_C resistance in the capacitor branch. Also show MARKS [10] CO5 L3

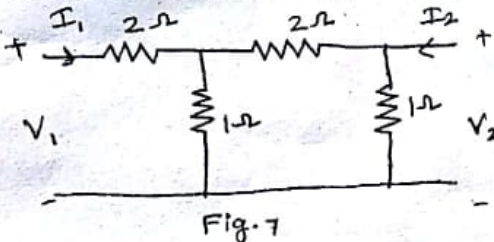
that the circuit will resonate at all frequencies if $R_L = R_C = \sqrt{\frac{L}{C}}$

- 6 A series RLC circuit has $R=100\Omega$, $L=0.5H$, $C=0.4\mu F$. Calculate resonant frequency, half power frequencies, band width and quality factor. MARKS [10] CO5 L3

$$f_0 = 855.872, Q_0 = 11.18, BW = 31.83$$

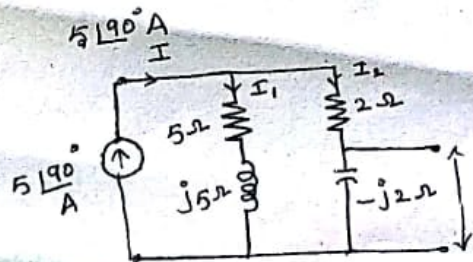
$$f_1 = 840.32, f_2 = 872.15$$

- 7 For the network shown in Fig.7, obtain Z parameters. MARKS [10] CO6 L3



$$Z = \begin{bmatrix} 4/3 & 1/3 \\ 1/3 & 3/2 \end{bmatrix}$$

- 8 State Reciprocity theorem and verify the same for the given network. (Fig. 8) MARKS 10 CO3 L3



$$V_x = 9.28 \angle 21.802^\circ V$$

$$I_2' = 1.64 \angle 111.802^\circ A$$

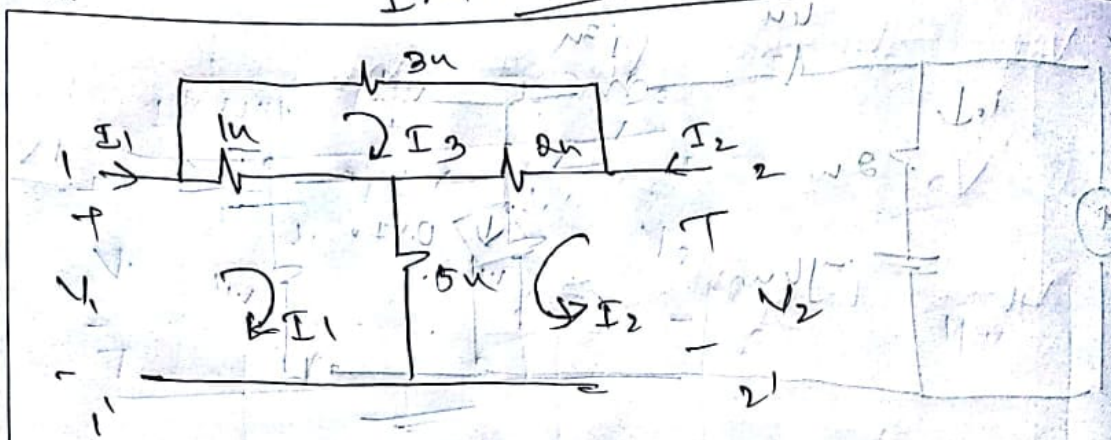
$$I_2'' = 1.313 \angle -23.198^\circ A$$

Fig. 8

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EAT - II

Q9



Applying KVL to loop (1), (2) & (3)

loop (2):

$$0 = 6I_3 - I_1 + 2I_2$$

$$I_3 = \frac{I_1 - 2I_2}{6}$$

loop (1):

$$V_1 = 6I_1 + 5I_2 - I_3$$

from eq (2)

$$V_1 = 6I_1 + 5I_2 - \left(\frac{I_1 - 2I_2}{6} \right)$$

$$V_1 = 6I_1 + 5I_2 - \frac{I_1}{6} + \frac{2I_2}{6}$$

$$V_1 = 5.83 I_1 + 5.33 I_2 \quad \text{--- (2)}$$

loop (1):

$$V_2 = 7 I_2 + 5 I_1 + 2 I_3$$

$$V_2 = 5 I_1 + 7 I_2 + \left(\frac{I_1 - 2 I_2}{6} \right)$$

$$V_2 = 5 I_1 + 7 I_2 + \frac{I_1}{6} - \frac{2 I_2}{6}$$

$$V_2 = 5.16 I_1 + 6.67 I_2 \quad \text{--- (3)}$$

By the definition of Z_{ij}

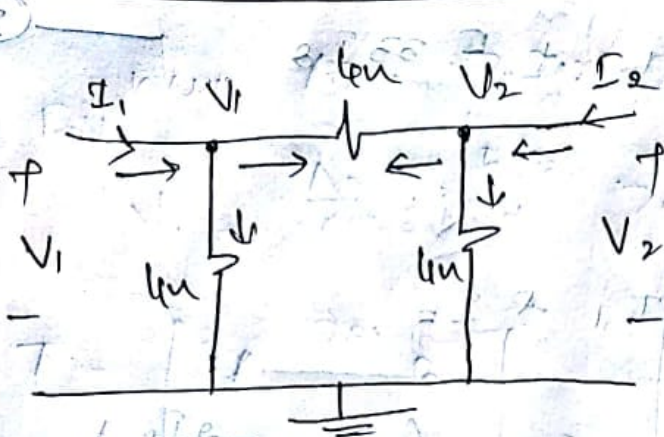
$$V_1 = Z_{11} I_1 + Z_{12} I_2 \quad \text{--- (4)}$$

$$V_2 = Z_{21} I_1 + Z_{22} I_2 \quad \text{--- (5)}$$

from eqⁿ (2), (3), (4) & (5)

$$Z \rightarrow \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} = \begin{bmatrix} 5.83 & 5.33 \\ 5.16 & 6.67 \end{bmatrix} \quad \underline{\underline{\quad}}$$

3/



Applying Nodal Analysis at V_1 & V_2

$$I_1 = \frac{V_1}{4} + \frac{V_1 - V_2}{4}$$

$$I_1 = 0.5 V_1 + 0.25 V_2 \quad \text{--- (1)}$$

Similarly

$$I_2 = \frac{V_2 - V_1}{4} + \frac{V_2}{4}$$

$$I_2 = -0.25 V_1 + 0.5 V_2 \quad \text{--- (2)}$$

From the definition of y

$$I_1 = Y_{11} V_1 + Y_{12} V_2 \quad \text{--- (3)}$$

$$I_2 = Y_{21} V_1 + Y_{22} V_2 \quad \text{--- (4)}$$

from eqⁿ (1), (2), (3) & (4)

$$Y = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} = \begin{bmatrix} 0.5 & -0.25 \\ -0.25 & 0.5 \end{bmatrix} \quad \underline{\underline{W}}$$

By the interrelation b/w Z & Y

$$Z = \begin{bmatrix} \frac{Y_{22}}{\Delta Y} & \frac{-Y_{12}}{\Delta Y} \\ \frac{-Y_{21}}{\Delta Y} & \frac{Y_{11}}{\Delta Y} \end{bmatrix}$$

where $\Delta Y = Y_{11}Y_{22} - Y_{12}Y_{21}$

$$\Delta Y = 0.1875 \dots$$

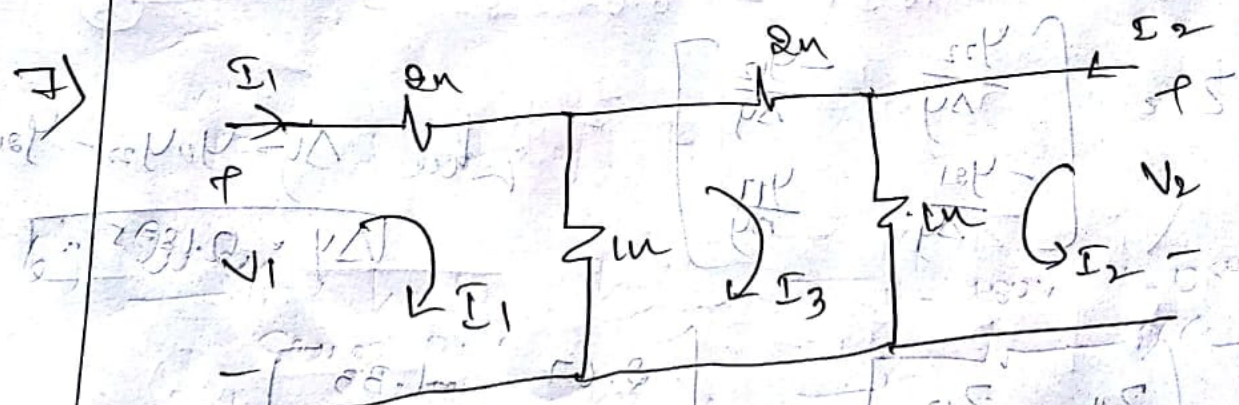
$$Z = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} = \begin{bmatrix} 2.67 & 1.33 \\ 1.33 & 2.67 \end{bmatrix} \quad \underline{\underline{W}}$$

By the interrelation b/w T & Z

$$T = \begin{bmatrix} A & B \\ C & D \end{bmatrix} = \begin{bmatrix} \frac{Z_{11}}{Z_{21}} & \frac{\Delta Z}{Z_{21}} \\ \frac{1}{Z_{21}} & \frac{Z_{22}}{Z_{21}} \end{bmatrix}$$

where $\Delta Z = \sqrt{2.212}$ $\sqrt{2.212}$
 $\Delta Z = 5.36$

$$T = \begin{pmatrix} A & B \\ C & D \end{pmatrix} = \begin{pmatrix} 2 & 4 \\ 0.75 & 2 \end{pmatrix}$$



Applying KVL to loop 1, 2 & 3

Loop (1):

$$0 = 4I_3 + I_1 + I_2$$

$$I_3 = \frac{I_1 - I_2}{4}$$

Loop 1:

$$V_1 = 3I_1 - I_3$$

from eqn (1)

$$V_1 = 3I_1 - \left(\frac{I_1 - I_2}{4} \right)$$

$$V_1 = 3I_1 - \frac{I_1}{4} + \frac{I_2}{4}$$

$$V_1 = 2.75 I_1 + 0.25 I_2$$

(2)

Loop 2:

$$V_2 = I_2 + I_3$$

$$V_2 = I_2 + \left(\frac{I_1 - I_2}{4} \right)$$

$$V_2 = I_2 + \frac{I_1}{4} - \frac{I_2}{4}$$

$$V_2 = 0.75 I_1 + 0.25 I_2$$

(3)

By the definition of Z

$$V_1 = Z_{11} I_1 + Z_{12} I_2 \quad \text{--- (1)}$$

$$V_2 = Z_{21} I_1 + Z_{22} I_2 \quad \text{--- (2)}$$

from eqⁿ (1), (2) & (3)

$$Z = \begin{bmatrix} Z_{11} & Z_{12} \\ Z_{21} & Z_{22} \end{bmatrix} = \begin{bmatrix} 9.75 & 0.25 \\ 0.25 & 0.75 \end{bmatrix} \Omega$$

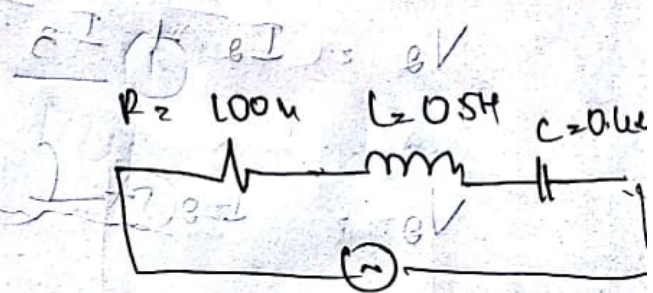
6) away

Series RLC

$$R = 100 \Omega$$

$$L = 0.5 \text{ H}$$

$$C = 0.4 \mu\text{F}$$



∴ Resonant frequency

$$f_0 = \frac{1}{2\pi \sqrt{LC}}$$

$$f_0 = \frac{1}{2\pi \sqrt{0.5 \times 0.4 \mu}}$$

$$f_0 = 355.88 \text{ Hz}$$

Band width, $B.W = \frac{R}{2\pi L}$

$$B.W = \frac{100}{2\pi(0.5)} = 31.83 \text{ Hz}$$

Quality factor, $Q = \frac{1}{R} \left(\frac{L}{C} \right)$

$$Q = \frac{1}{100} \sqrt{\frac{0.5}{0.4 \times 10^{-6}}}$$

$$Q = 11.18$$

half power frequencies, $f_1 = 9$
 $f_2 = 9$

WUT $B.W = \Delta f$

$$\Delta f = \frac{B.W}{2} = \frac{31.83}{2} = 15.915 \text{ Hz}$$

$$f_1 = f_0 - \Delta f = 355.88 - 15.915 = 339.965 \text{ Hz}$$

$$f_2 = f_0 + \Delta f = 355.88 + 15.915 = 371.795 \text{ Hz}$$

Y in terms of h

By definition of h

$$V_1 = h_{11} I_1 + h_{12} V_2 \quad \text{--- (1)}$$

$$I_2 = h_{21} I_1 + h_{22} V_2 \quad \text{--- (2)}$$

Was used, by definition of y

$$V_1 = y_{11} I_1 + y_{12} I_2$$

$$V_2 = y_{21} I_1 + y_{22} I_2$$



$$I_1 = y_{11} V_1 + y_{12} V_2 \quad \text{--- (3)}$$

$$I_2 = y_{21} V_1 + y_{22} V_2 \quad \text{--- (4)}$$

from eqⁿ (1)

$$V_1 = h_{11} I_1 + h_{12} V_2$$

$$h_{11} I_1 = V_1 - h_{12} V_2$$

$$I_1 = \frac{1}{h_{11}} V_1 - \frac{h_{12}}{h_{11}} V_2 \quad \text{--- (5)}$$

from eqⁿ (2)

$$I_2 = h_{21} I_1 + h_{22} V_2$$

Substituting the eqⁿ (5) in above eqⁿ

$$I_2 = h_{21} \left[\frac{1}{h_{11}} V_1 - \frac{h_{12}}{h_{11}} V_2 \right] + h_{22} V_2$$

$$I_2 = \frac{h_{21}}{h_{11}} V_1 - \frac{h_{21} h_{12}}{h_{11}} V_2 + h_{22} V_2$$

$$I_2 = \frac{h_{21}}{h_{11}} V_1 + \left(\frac{h_{11} h_{22} - h_{12} h_{21}}{h_{11}} \right) V_2 \quad \text{--- (6)}$$

from eqⁿ (3), (4), (5) & (6)

$$Y = \begin{bmatrix} Y_{11} & Y_{12} \\ Y_{21} & Y_{22} \end{bmatrix} = \begin{bmatrix} \frac{1}{h_{11}} & -\frac{h_{12}}{h_{11}} \\ \frac{h_{21}}{h_{11}} & \frac{\Delta h}{h_{11}} \end{bmatrix}$$

where $\Delta h = h_{11}h_{22} - h_{12}h_{21}$

Reciprocity Condition for ABCD parameters

By the definition of Reciprocity Condition

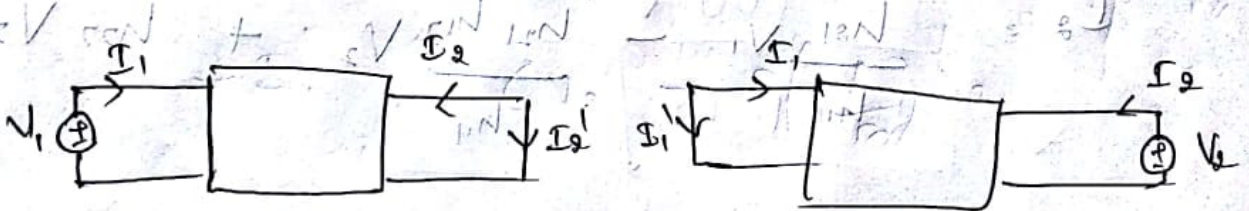


Fig (a) Fig (b)

$$V_1 = V_S, \quad I_2 = -I_2', \quad V_2 = V_S, \quad I_1 = -I_1'$$

$$V_2 = 0, \quad I_1' = I_1', \quad I_1 = 0, \quad I_2' = I_2'$$

for Reciprocity,

$$\boxed{\frac{I_2'}{V_1} = \frac{I_1'}{V_2}}$$

$$= \boxed{\frac{I_3'}{V_3} = \frac{I_4'}{V_3}}$$

Consider ABCD parameters eqn

$$V_1 = AV_2 - BI_2 \quad \text{--- (1)}$$

$$I_1 = CV_2 - DI_2 \quad \text{--- (2)}$$

Case (1):

$$V_2 = 0, \quad V_1 = V_3, \quad I_2 = -I_3'$$

from eqn (1)

$$V_1 = A(0) - B(-I_3')$$

$$V_1 = BI_3'$$

$$\frac{I_3'}{V_1} = \frac{I_4'}{V_3} = \frac{1}{B} \quad \text{--- (3)}$$

Case (ii)

$$V_1 = 0$$

$$V_2 = V_3$$

$$I_1' = -I_2'$$

from eqⁿ (1)

$$I_1 = CV_2 - DI_2$$

$$-I_1' = CV_2 - DI_2 \quad \text{--- (4)}$$

from eqⁿ (2)

$$0 = AV_2 - BI_2$$

$$AV_2 = BI_2$$

$$I_2 = \frac{A}{B} V_2$$

Substituting in eqⁿ (4)

$$-I_1' = (CV_2) - D\left(\frac{A}{B}\right)V_2$$

$$-I_1' = V_2 \left(\frac{BC - AD}{B} \right)$$

$$I_1' = V_2 \left(\frac{AD - BC}{B} \right)$$

$$\frac{F_1}{V_2} = \frac{AD - BC}{B} \quad \text{--- (5)}$$

∴ for Reciprocity Condition,

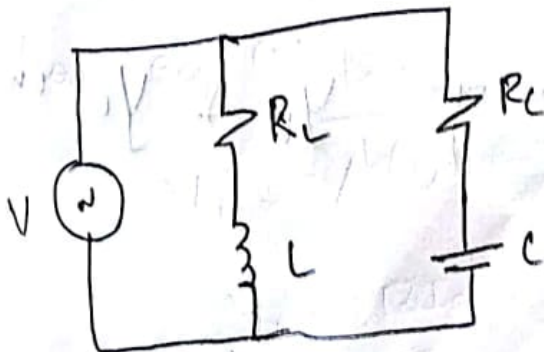
$$eq^n (3) = eq^n (5)$$

$$\frac{1}{B'} = \frac{AD - BC}{B}$$

$$AD - BC = 1$$

$$\Delta T = 1$$

when $\Delta T = AD - BC$



Consider the circuit as shown in figure.

$$Y_i = Y_L + Y_C \quad \text{--- (1)}$$

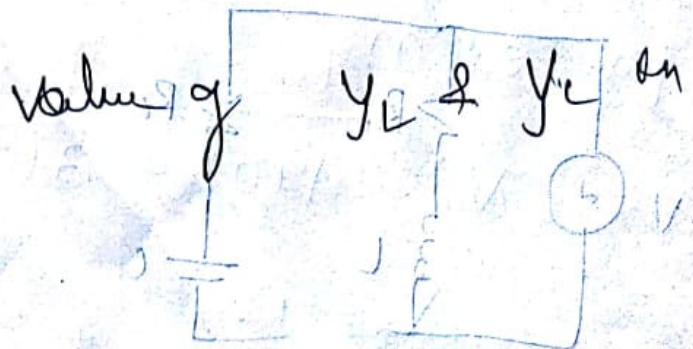
$$Y_L = \frac{1}{Z_L} = \frac{1}{R_L + jX_L} = \frac{R_L - jX_L}{R_L^2 + X_L^2}$$

$$Y_L = \frac{R_L - jL\omega}{R_L^2 + \omega^2 L^2} \quad \left(X_L = L\omega \right)$$

$$Y_C = \frac{1}{Z_C} = \frac{1}{R_C - jX_C} = \frac{R_C + jX_C}{R_C^2 + X_C^2}$$

$$Y_C = \frac{R_C + j/\omega C}{R_C^2 + 1/\omega^2 C^2}$$

Substituting the values of eqn (1) and (2)



$$Y = \frac{R_L - jL\omega}{R_L^2 + \omega^2 L^2} + \frac{R_C + j/\omega C}{R_C^2 + 1/\omega^2 C^2}$$

$$I_{rms} = \frac{1}{\sqrt{2}} \sqrt{\frac{1}{LC} - \frac{R^2 C}{L^2}}$$

$$I_{rms} = \frac{1}{\sqrt{2}} \sqrt{LC - \frac{R^2 C^2}{L}}$$

At resonance

$$L\omega = \frac{1}{C\omega}$$

$$\frac{R^2 + \omega^2 L^2}{R^2 + \frac{1}{\omega^2 C^2}} = \frac{R^2 + \frac{1}{\omega^2 C^2}}{R^2 + \frac{1}{\omega^2 C^2}}$$

$$L\omega \left(R^2 + \frac{1}{\omega^2 C^2} \right) = \frac{1}{C\omega} \left(R^2 + \omega^2 L^2 \right)$$

$$L\omega \left(\frac{R^2 C^2 \omega^2 + 1}{C^2 \omega^2} \right) = \frac{1}{C\omega} \left(R^2 + \omega^2 L^2 \right)$$

$$\frac{L}{C} \left(R^2 C^2 \omega^2 + 1 \right) = R^2 + \omega^2 L^2$$

$$L(R^2 C^2 \omega^2 + 1) = C(R^2 + \omega^2 L^2)$$

$$R^2 C^2 \omega^2 L + L = R^2 C + \omega^2 L^2 C$$

$$R^2 C^2 \omega^2 L - \omega^2 L^2 C = \frac{R^2 C L - L}{\omega^2}$$

$$\omega^2 (R^2 C^2 L - L^2 C) = \frac{R^2 C L - L}{\omega^2}$$

$$\omega^2 = \frac{R^2 C L - L}{R^2 C^2 L - L^2 C}$$

$$R^2 C L - L^2 C$$

$$\omega = \frac{1}{\sqrt{LC}} \left(\frac{R^2 C - L}{R^2 C - L} \right)$$

$$\omega = \frac{1}{\sqrt{LC}} \left(\frac{R^2 - 4/C}{R^2 - 4/C} \right)$$

$$\omega = \frac{1}{\sqrt{LC}} \sqrt{\frac{R^2 - 4/C}{R^2 - 4/C}}$$

$$\omega = \frac{1}{\sqrt{LC}} \sqrt{\frac{R^2 - 4/C}{R^2 - 4/C}}$$

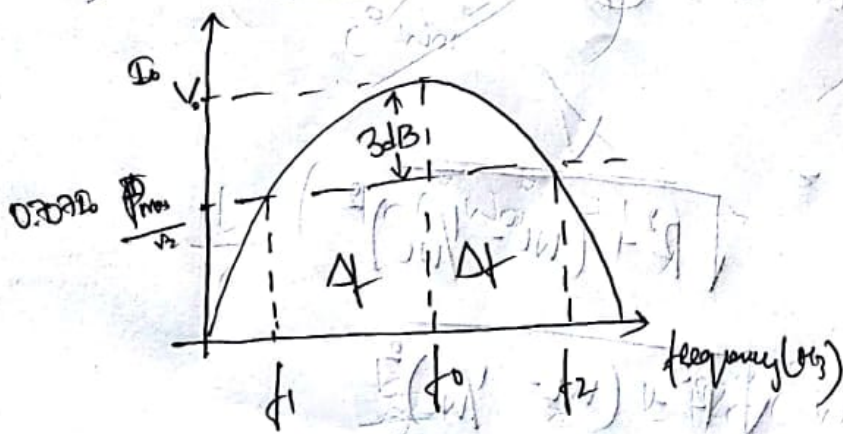
$$f_{0r} = \frac{1}{2\pi\sqrt{LC}} \sqrt{\frac{R_L^2 - 4LC}{R_C^2 - 4LC}}$$

$$\frac{V}{S} = E$$

∴ The circuit will resonate at all frequencies

$$R_L = R_C = \sqrt{4/LC}$$

$$f_{0r} = \frac{1}{2\pi\sqrt{LC}} \sqrt{\frac{R_L^2 - 4LC}{R_C^2 - 4LC}}$$



$$B.W = f_2 - f_1$$

Let

$$I = \frac{V}{Z}$$

$$\frac{V - 100}{V - 100} \sqrt{\frac{1}{R^2 + (X_L - X_C)^2}}$$

$$I = \frac{V}{\sqrt{R^2 + (X_L - X_C)^2}} \quad \text{--- (1) At Resonance}$$

Also At Resonance

$$I_0 = \frac{I}{\sqrt{2}}$$

Also $I_0 = \frac{V}{R}$

$$I = \frac{V}{\sqrt{2}R} \quad \text{--- (2)}$$

from eqⁿ (1) & (2)

$$\frac{V}{\sqrt{2}R} = \frac{V}{\sqrt{R^2 + (X_L - X_C)^2}}$$

On squaring

$$0 = 2R^2 + R^2 + (WL - \frac{1}{WC})^2$$

$$\left(\frac{2R^2 + R^2}{2WL - \frac{1}{WC}} \right) = (WL - \frac{1}{WC})^2$$

$$R^2 = (WL - \frac{1}{WC})^2$$

$$\Rightarrow (WL - \frac{1}{WC}) = \pm R$$

$$\rightarrow (WL - \frac{1}{WC}) = +R \quad \text{--- (3)}$$

$$(WL - \frac{1}{WC}) = -R \quad \text{--- (4)}$$

Adding eqn (3) & (4)

~~$$WL - \frac{1}{WC} = R$$~~

~~$$WL - \frac{1}{WC} = -R$$~~

$$W_1L - \frac{1}{W_1C} + W_2L - \frac{1}{W_2C} = 0$$

$$L(\omega_1 + \omega_2) \frac{1}{MC} - \frac{1}{C} \left(\frac{1}{\omega_1} + \frac{1}{\omega_2} \right) = 0$$

$$L(\omega_1 + \omega_2) \frac{1}{MC} = \frac{1}{C} \left(\frac{\omega_1 + \omega_2}{\omega_1 \omega_2} \right)$$

~~$$L(\omega_1 + \omega_2) \frac{1}{MC} = \frac{1}{C} \left(\frac{\omega_1 + \omega_2}{\omega_1 \omega_2} \right)$$~~

$$\omega_1 \omega_2 = \frac{1}{LC} \quad \left(\because \omega_0 = \frac{1}{\sqrt{LC}} \right)$$

⑤ $\omega_0^2 = \omega_1 \omega_2$

$$\boxed{\omega_0 = \sqrt{\omega_1 \omega_2}}$$

⑥ $f_0 = \sqrt{f_1 f_2}$