


INSTITUTE OF TECHNOLOGY		USN											
Internal Assessment Test – 3													
Sub:	Design of Pre-stressed Concrete Structures (PSC)										Code:	10CV74	
Date:	18/ 11 / 2017	Duration:	90 mins	Max Marks:	50	Sem:	7	Branch:	CIVIL				
Answer any FIVE Full questions , USE of IS 1343 -1980 is Permitted , Density of Concrete = 25 KN/ Cu. M													
											Marks	OBE	
												CO	RBT
1	Using Two Critical Conditions (Max Prestress at Minimum Moment And Min Prestress at Maximum Load) Derive the mathematical Expression to Find Minimum Section Modulus , Prestressing Force and Eccentricity of Cable.										[10]	CO4	L3
2	Explain Limiting Zone For Pre- stressing Force and Give 4 equations for calculation of Eccentricity.										[10]	CO4	L2
3	Sketch the classification of Zones of failure under Shear for a cracked beam? Explain reasons for formation of Web Shear Cracks?										[10]	CO3	L2
4	A PSC rectangular beam 250mm x 450mm deep is prestressed by a parabolic cable having an eccentricity of +75mm at center span and -25mm at support. Effective prestressing force = 400KN , span = 9m , beam supports a Live load of 3 KN / M in addition to self weight. If $E_c = 38\text{Kn/ mm}^2$, calculate (a) short term deflection at center span due to LL +DL+PS (b) Long term deflection take loss ratio = 0.8 , creep coefficient = 1.6										[10]	CO3	L3

5	A Pre tensioned, PSC rectangular beam 500mm x 900mm (effective depth) have $A_p = 3200 \text{ sq.mm}$, effective prestress in the steel after all losses is 1100 N/ sq.mm , $F_{ck} = 40 \text{ N / sq.mm}$. estimate ultimate moment of resistance of section using IS 1343-1980	[10]	CO3	L3
6	A Concrete beam of rectangular section 200mm x 650mm depth is pre-stressed by a parabolic cable located at an eccentricity of 120mm at mid span and zero at support. If the beam has a span of 12m and carries a UDL Live load of 4.5 KN/M , find the Effective Pre-stressing force necessary for ZERO Shear stress at the support section. For this conditions calculate the principal stresses . the density of concrete = 24 KN/Cum . Take Load factor = 1.5	[10]	CO3	L3
7	The support Section of a PSC Beam is 150mm x 300mm is to resist a shear of 100KN. The prestress at centroidal axis is 5 N/Sq.mm . $F_{ck} = 40 \text{ N/Sq.mm}$. the cover to tension reinforcement is 45mm. Check the section for Shear and Design suitable shear reinforcement . USE IS 1343-1980	[10]	CO2	L3
8	A post tensioned PSC Beam 300mm wide is to be designed as a rectangular beam to support a Live Load of <u>18 Kn/ M</u> . Beam is simply supported over a span of <u>20m</u> . the load factor for Live Load and Dead load is 1.5. The stresses in Concrete must not exceed at all stages , for compression is 15 N/sqmm and for Tension it is ZERO. , Loss factor is 0.8 , ultimate tensile stress in steel is 1600 N/ Sq.mm , partial safety factor for steel = 1.15. Use 11wire strand of 7mm dia. Design the beam and determine Z_{min} , P_{min} , Eccentricity e and Number of Tendons	[10]	CO4	L4

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$$f_{sup} = \frac{Mg}{Z_t} = -1.2 - \frac{537.5 \text{ KN-m} \times 10^6}{63375000}$$

Civil

$$= -9.68 \text{ N/mm}^2$$

$$f_{inf} = \frac{1}{\eta} \left[f_{tw} + \frac{Mg}{Z_b} + \frac{Mg}{Z_b} \right]$$

$$= \frac{1}{0.82} \left[-1.2 + \frac{(537.47 + 810) \times 10^6}{63375000} \right]$$

$$= 24.46 \text{ N/mm}^2$$

Minimum prestressing Force

$$P = \frac{A [Z_b f_{inf} + Z_t f_{sup}]}{(Z_t + Z_b)}$$

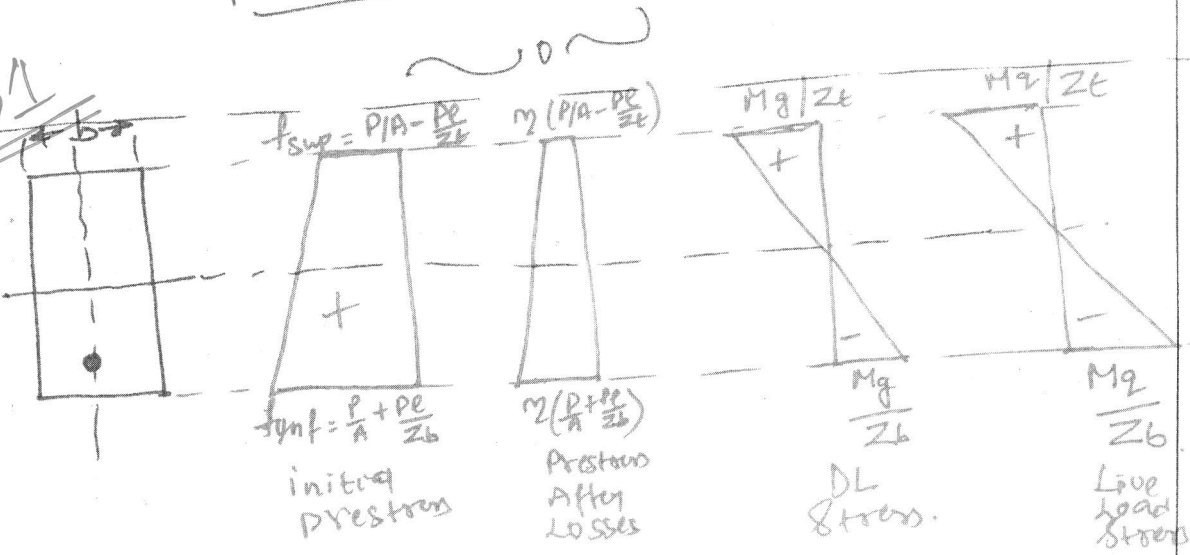
$$P = 2883.052 \text{ KN}$$

Eccentricity

$$e = \frac{Z_t Z_b (f_{sup} - f_{inf})}{A (f_{sup} Z_t + f_{inf} Z_b)}$$

$$e = 375 \text{ mm}$$

NO1



1 mark

2 marks

2 marks

1 mark



→ ASSUMPTION'S

Prestressed section under the action of flexure should satisfy the limit specified for permissible stresses @ the stage of transfer of PS and @ Service Loads

- Max prestressing force at transfer together with min moments sustained by the section.
- Min prestressing force after all losses in combination with max design moment for the serviceability limit state.

2 marks.

→ i) At transfer (PS + DL)

$$f_{top} \text{ @ } f_{sup} + \frac{M_g}{Z_t} \geq f_{ct} = \text{allowable tensile stress in concrete @ initial transfer of prestress.}$$

$$f_{bot} \text{ @ } f_{inf} - \frac{M_g}{Z_b} \leq f_{cc} = \text{allowable compressive stress in concrete @ initial transfer of prestress.}$$

ii) At working → PS + LL + DL

$$\eta f_{sup} + \frac{M_g}{Z_t} + \frac{M_l}{Z_t} \leq f_{cw} = \text{allowable comp stress in concrete under service loads.}$$

$$\eta f_{inf} - \frac{M_g}{Z_b} - \frac{M_l}{Z_b} \geq f_{tw} = \text{allowable tensile stress in concrete under service loads.}$$

Based on above formulation, students to arrive following results.

- a) Range of stress @ top fibre $f_{tr} \geq (f_{cw} - \eta f_{ct}) \geq \frac{(M_g + (1-\eta)M_l)}{Z_t}$
- b) Range of stress @ bottom fibre $f_{br} \geq (\eta f_{cc} - f_{tw}) \geq \frac{M_g + (1-\eta)M_l}{Z_b}$

c) Section Modulus

$$Z_t \geq \frac{(M_g + (1-\eta)M_l)}{f_{tr}}$$

$$Z_b \geq \frac{(M_g + (1-\eta)M_l)}{f_{br}}$$

1 mark.

d) Prestressing force

$$P = A_c \cdot \frac{\{f_{inf} \cdot Z_b + f_{sup} \cdot Z_t\}}{(Z_b + Z_t)}$$

2 marks.

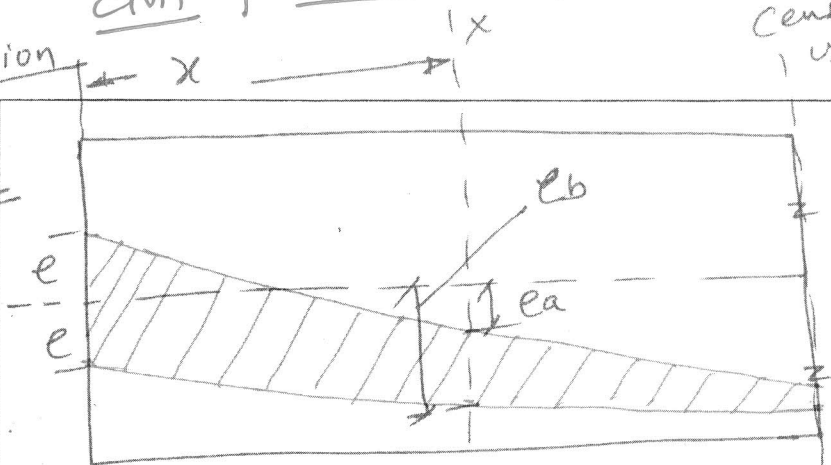
e) Eccentricity e

$$e = \frac{Z_t Z_b (f_{inf} - f_{sup})}{A (f_{sup} Z_t + f_{inf} Z_b)}$$

2 marks.

Solution

Centre line of beam.



Limiting zone for prestressing force.

1 mark

The prestress along the length of the beam is generally adjusted by varying the eccentricity of the post tensioned members. Pre-stressing force. — After having once determined the magnitude of the prestressing force for the critical section, it is possible to fix up the limiting zone for the force bounded by the upper limits & lower limits expressed as a function of the min moments, max moments, & sectional properties, prestressing force P and permissible stresses in concrete @ transfer and working loads.

2 marks

$$e_1 \leq \left[-\frac{z_t f_{ct}}{P} + \frac{z_t}{A} + \frac{M_{min}}{P} \right]$$

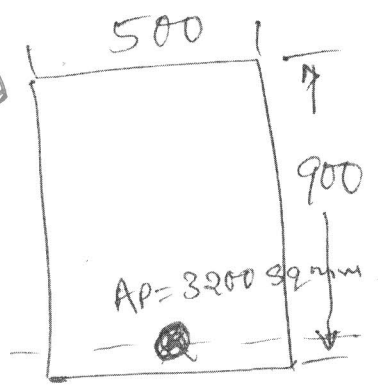
$$e_2 \leq \left[\frac{z_b f_{ct}}{P} - \frac{z_b}{A} + \frac{M_{min}}{P} \right]$$

$$e_3 \geq \left[-\frac{z_t f_{cw}}{\sigma P} + \frac{z_t}{A} + \frac{M_d}{\sigma P} \right]$$

$$e_4 \geq \left[\frac{z_b f_{cw}}{\sigma P} - \frac{z_b}{A} + \frac{M_d}{\sigma P} \right]$$

1 mark

Q5



$p_i = 1100 \text{ N/mm}^2$
 $f_{ck} = 40 \text{ N/mm}^2$
 $M_R = ?$

Pretensioned

use

$$M_R = f_{pu} A_p (d - 0.42 x_u) \quad (2)$$

Table no 11, IS 1843-1980.

$$\frac{A_p f_p}{b d f_{ck}} = \frac{3200 \times 1100}{500 \times 900 \times 40} = 0.1956 \quad (2)$$

$$\frac{A_p f_p}{b d f_{ck}}$$

pretension
 $\frac{f_{pu}}{0.87 f_p}$

$$\frac{x_u}{d}$$

$$0.326 + 0.099408 = 0.425408 \quad (2)$$

0.15
0.1956
 0.2

1.00
1.00
 1.00

$\therefore x_u = 0.4251 \times 900 = 382.59 \text{ mm}$
 $f_{pu} = (1.0)(0.87)(1100) = 957 \text{ N/mm}^2$

$$0.1956 - 0.15 = 0.0456$$

0.05 \rightarrow 0.109
 for 0.0456 \rightarrow ? 0.099408

$$M_R = \frac{(957)(3200)(900 - 0.42 \times 382.59)}{10^6} \text{ KN-m} = 2264.07 \text{ KN-m} \quad (2)$$

10

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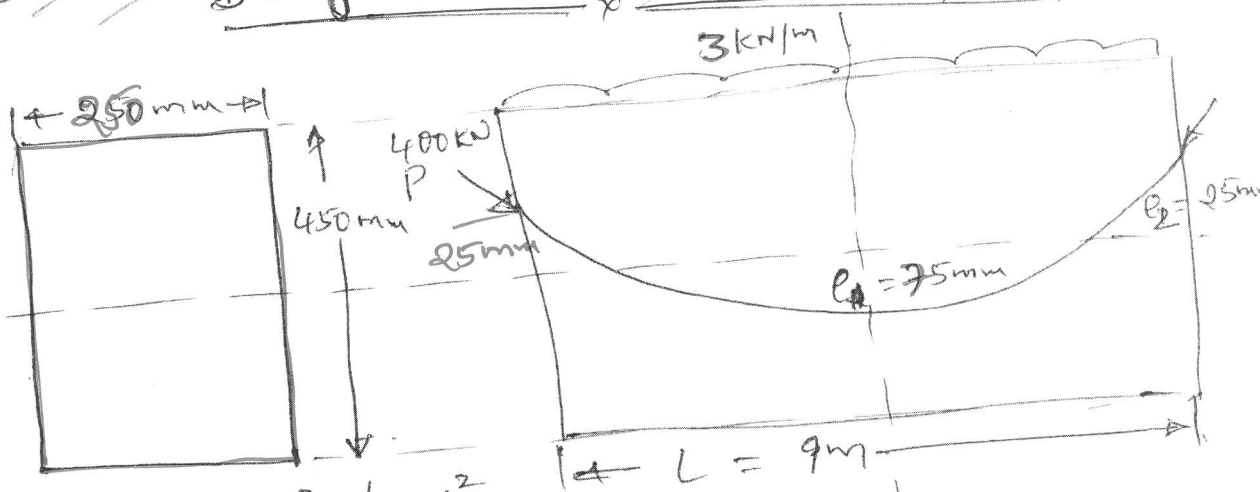
GMRTI
GNIPT

Solution.
Scheme.

Improvement
Tent

Design of prestressed concrete structure.

Q no 4



$E_c = 38 \times 10^3 \text{ N/mm}^2$
 $\eta = 0.8, \phi = 1.6$

a) Short term deflection = $\delta_{LL} + \delta_{DL} + \delta_{PS}$

$$\delta_{PS} = \frac{PL^2}{48EI} (-5e_1 + e_2)$$

$$= \frac{(400 \times 10^3)(9 \times 1000)^2}{(48)(38 \times 10^3)(1898.4375 \times 10^6)} (-5 \times 75 + 25)$$

$$= -3.275 \text{ mm} \uparrow \text{ upwards.}$$

$w_d = 0.25 \times 0.45 \times 24$
 $= 2.7 \text{ kN/m.}$

$$\delta_{DL} = \frac{(w_d)l^4}{EI} \times \frac{5}{384}$$

$$= \frac{2.7 \times (9000)^4}{(38 \times 10^3)(1898.4375) \times 10^6} \times \frac{5}{384} = 3.197 \text{ mm} \downarrow$$

$$\delta_{LL} = \frac{3 \times 9000^4}{(38 \times 10^3)(1898.4375) \times 10^6} \times \frac{5}{384} = 3.553 \text{ mm} \downarrow$$

Short term deflection = $3.197 + 3.553 - 3.275$
 $= 3.475 \text{ mm} \downarrow$

b) Long term deflection

$$\Delta_{LT} = [\Delta_{LL} + \Delta_{DL} + \Delta_{PS} \times \text{loss factor}] (1 + \phi)$$

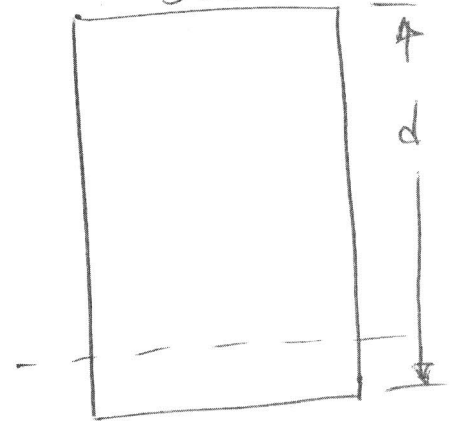
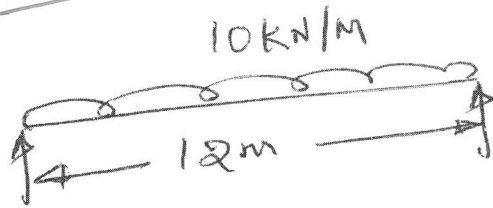
$$= (3.553 + 3.197 - 3.275 \times 0.8)(1 + 1.6)$$

$$= 10.738 \text{ mm} \downarrow$$

10

Q8

Q8



Factor of safety
LL & DL = 1.5
 $f_{cw} = f_{ct} = 15 \text{ N/mm}^2$
 $f_{tt} = f_{tw} = 0$

$\alpha = 0$
 $f_{pu} = 1600 \text{ N/mm}^2$, $\gamma_d = 1.15$
Steel - 4 Ay ϕ

Design the beam - z, P & e, No of strands = ?

Step-I

Moment due to dead load
 $M_g =$

$$1.5 \times b \times d \times 24 \times \frac{12^2}{8}$$

$$= 648 \times b d \text{ N-mm}$$

$$= 648 \times 300 d \text{ N-mm}$$

$$= 194400 d \text{ N-mm}$$

Live load moment
 $M_q =$

$$10 \times \frac{144}{8} \times 1.5 =$$

$$270 \text{ kN-m}$$

$$= 270 \times 10^6 \text{ N-mm}$$

Section modulus = $Z = \frac{bd^2}{6} = \frac{300}{6} d^2 = 50 d^2 \text{ mm}^3$

Now

$$Z_b = \frac{(M_q + (1.2)M_g)}{(0.8f_{ct} - f_{tw})} = \frac{(270 \times 10^6 + 0.2 \times 194400 d)}{0.8 \times 15 - 0}$$

$$= 50 d^2$$

$$d^2 - 64.80d - 450000 = 0$$

$$\frac{64.80 \pm \sqrt{(64.80)^2 - 4(1)(-450000)}}{2 \times 1}$$

$$d = \underline{1408 \text{ mm}}$$

Provide 1450 mm or 1500 mm

(2)

$$Z_{\text{provided}} = \frac{300 \times 1500^2}{\cancel{6}} = 112.5 \times 10^6 \text{ mm}^3 \quad (2)$$

$$A_c = 300 \times 1500 = 450000 \text{ mm}^2$$

To Find P.

$$f_{\text{sup}} = f_{\text{ct}} - \frac{M_g}{Z_t}$$

$$= 0 - \frac{194400 \times 1500}{450000 \times 112.5 \times 10^6}$$

$$= -2.592 \text{ N/mm}^2$$

$$f_{\text{st}} = \frac{1}{\alpha} \left[f_{\text{ct}} + \frac{M_g + M_f}{Z_b} \right]$$

$$= \frac{1}{0.8} \left[0 + \frac{270 \times 10^6 + 991600000}{112.5 \times 10^6} \right]$$

$$= 6.24 \text{ N/mm}^2$$

$$P = \frac{A_c}{2} \{ f_{\text{st}} + f_{\text{sup}} \}$$

$$= \frac{450000}{2} \{ 6.24 - 2.592 \} \quad (2)$$

$$= 820.8 \text{ kN}$$

$$\text{Nr of Strands} = \frac{820.8 \times 10^3}{\frac{11 \times \pi}{4} \times 49^2 \times \frac{1.5}{1.5}} = 1.3935 \times 4 \text{ nos} \quad (2)$$

$$e = \frac{Z}{A} \times \left\{ \frac{f_{mp} - f_{mp}}{f_{mp} + f_{mp}} \right\}$$

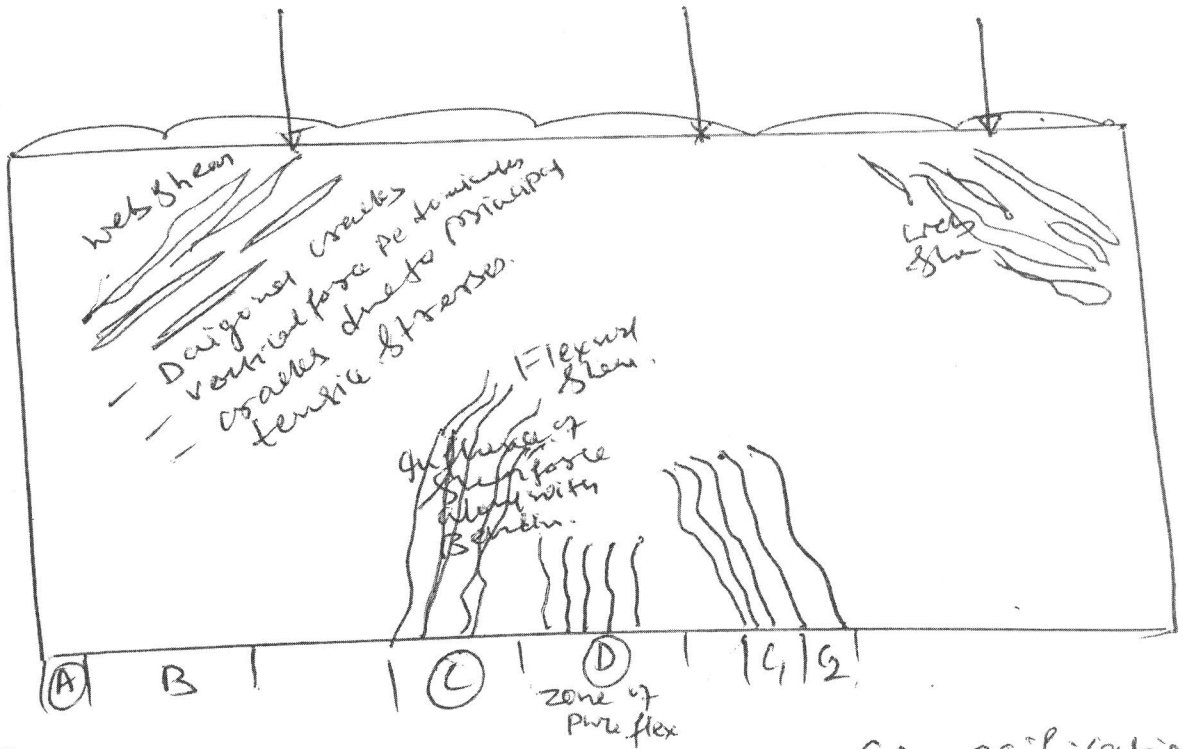
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$$= \frac{112500000}{450000} \times \left\{ \frac{6.24 - (-2.592)}{6.24 + (-2.592)} \right\}$$

$$= 605.2632 \text{ say } \underline{\underline{606 \text{ mm}}}$$

2

Q8



10

- (A) NO crack zone
- (B) web shear crack zone
- (C) flexural shear crack zone.
- (D) flexural crack zone.
- (E) zone with parallel cracks.
- (C₁) zone with converging cracks
- (C₂) zone with converging cracks

Classification of zones in a cracked beam

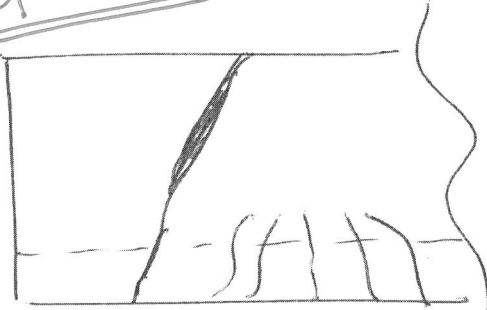
In the zone where the vertical force (Equilibrating force) in the section predominates the cracks develop in the web somewhere in the middle where shear stress intensity is high, this is due to principal tensile stresses that this zone is shear crack zone.

Q no 3

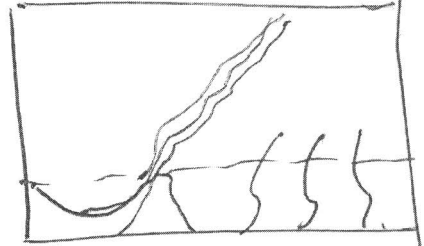
PSC

Test no 3

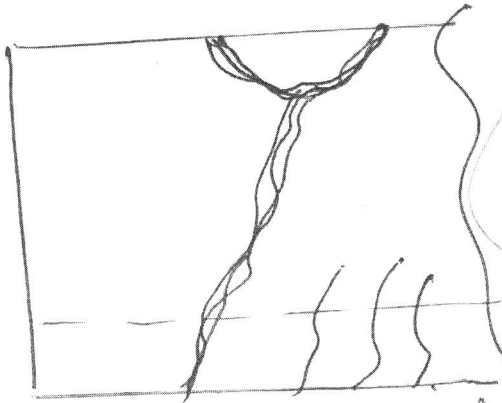
(6)



Diagonal tension
Crack failure.



Anchorage
failure.



Shear compression failure.

$SFC = 10$



web crushing.
web compression failure.

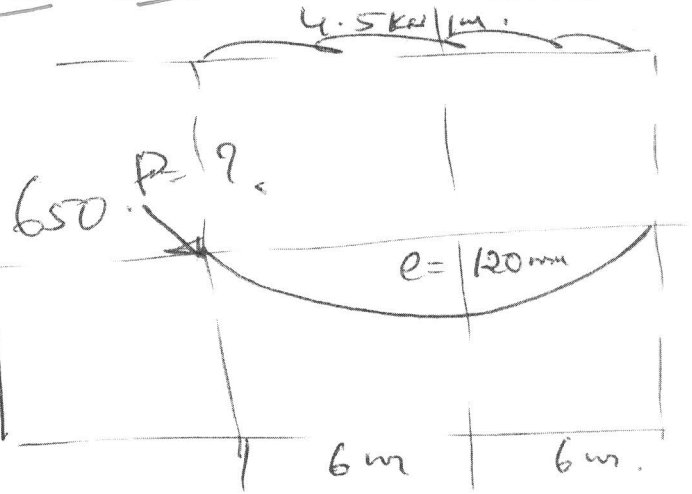
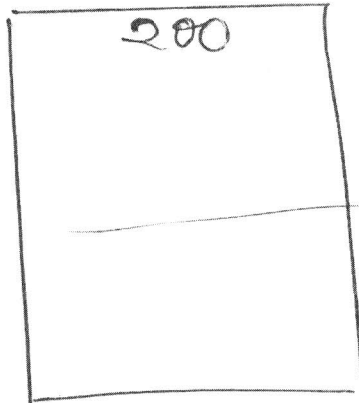
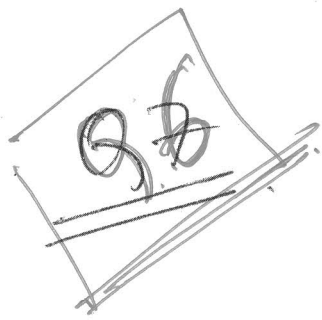
(10)



ARCH RIB failure.

Crack due to
eccentric
compression.

compression
thrust line.



$P = ?$

Zero shear @ support

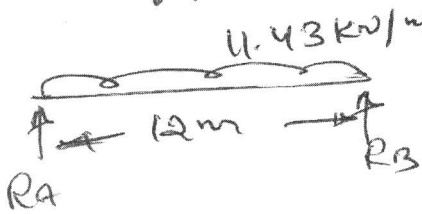
Concreteness = 24 kN/m³
Load Factor = 1.5

σ_1 & σ_2 ?

Solution

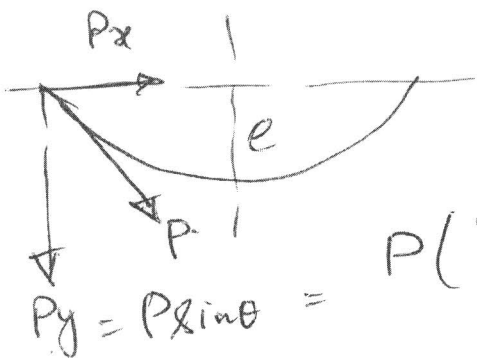
Dead load = $0.2 \times 0.65 \times 24 = 3.12 \text{ kN/m}$
Line load = 4.5 kN/m
Total load = 7.62 kN/m

∴ Ultimate load = $7.62 \times 1.5 = 11.43 \text{ kN/m}$



$R_A = R_B = \frac{11.43 \times 12}{2} = 68.58 \text{ kN}$

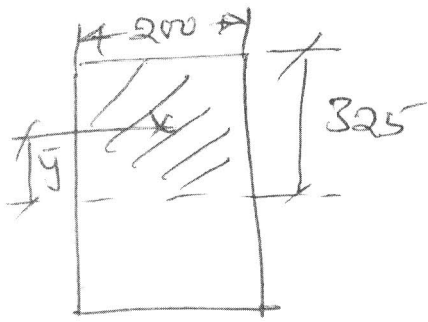
SF @ support = SF due to U+DL + SF due to prestress.
 $= 68.58 + P_y$



$P_y = P \sin \theta = P \left(\frac{4e}{l} \right) = P \left(\frac{4 \times 120}{12000} \right) = 0.04 P$
 $V_u = (68.58 - 0.04 P)$

Net Shear Stress @ support = $\tau_u = \frac{V_u \cdot A_y}{I \cdot b} = 0$

$$I = \frac{bd^3}{12} = \frac{200 \times 650^3}{12} = 4.6 \times 10^9 \text{ mm}^4$$



$$b = 200 \text{ mm}$$

$$A\bar{y} = 200 \times 325 \times \frac{325}{2} = 10.56 \times 10^6 \text{ mm}^3$$

$$\text{Now } 0 = \frac{(68.58 - 0.04P) (10.56 \times 10^6) \text{ mm}^3}{(4.6 \times 10^9) \text{ mm}^4 \times 200 \text{ mm}}$$

$$P = 1714.5 \text{ kN}$$

(2)

(6)

Principia Stressen

$$\tau_v = 0$$

$$f_y = 0$$

$$f_x = \frac{P}{A} = \frac{1714 \times 10^3}{200 \times 650}$$

NO vertical prestress.

$$= 13.18 \text{ N/mm}^2$$

$$\sigma_{\text{max/min}} = \frac{f_x + f_y}{2} \pm \frac{1}{2} \sqrt{(f_x - f_y)^2 + 4\tau_v^2}$$

$$= \frac{13.18 + 0}{2} \pm \frac{1}{2} \sqrt{(13.18 - 0)^2 + 4(0)}$$

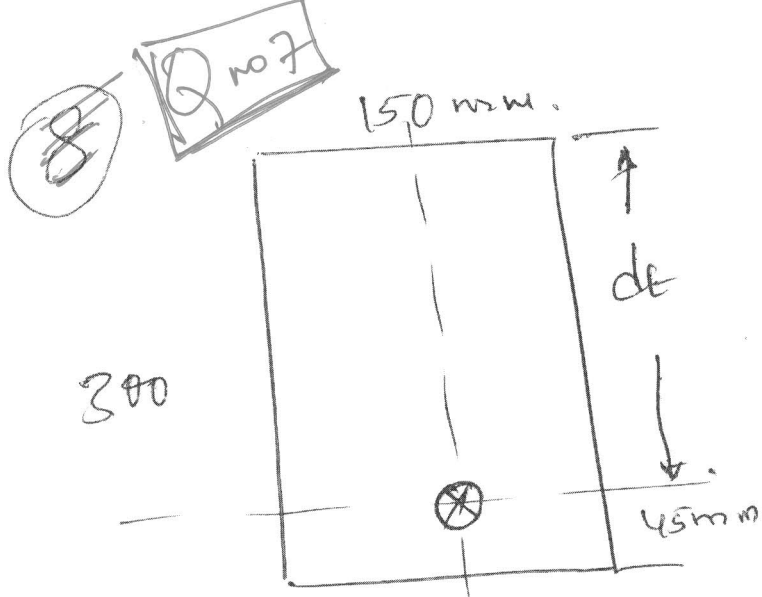
(4)

$$\sigma_1 = 13.18 \text{ N/mm}^2 \text{ Comp.}$$

$$\sigma_2 = 0$$

6+4=10

2017-18



$SF = 100 \text{ kN}$
 $f_{cp} = 5 \text{ N/mm}^2$
 $f_{ck} = 40 \text{ kN/mm}^2$
 $\text{Cover} = 45 \text{ mm}$

$\therefore de = 300 - 45 = 255 \text{ mm}$

$f_t = \text{tensile stress} = 1.5 \text{ N/mm}^2$

I Ultimate $SF = V_u = 1.5 \times 100 = 150 \text{ kN}$

II Internal shear resistance = V_{co}

$V_{co} = 0.67 b D \sqrt{f_t^2 + 0.8 f_{cp} f_t}$

Pg 46
 IS 1343
 -1980

$= 0.67 \times 150 \times 300 \times \sqrt{(1.5)^2 + 0.8 \times 5 \times 1.5}$

$V_{co} = 86.59 \text{ kN}$ — (1)

NOW $V_{co} < V_u$

Case II provide shear reinforcement

III using 2 legged - 8 mm ϕ vertical stirrups.

$A_{sv} = 2 \times \frac{\pi}{4} \times 64 = 100.53 \text{ mm}^2$

$\frac{A_{sv}}{S_v} = \frac{(V_u - V_{co})}{0.87 f_y d_b}$

IS 456:2000 Cl 22.4.3.2 Pg 48

$\frac{100.53}{S_v} = \frac{(150 \times 10^3 - 86.59 \times 10^3)}{0.87 \times 415 \times 255}$

$S_v = 145.96 \text{ mm}$
 9c.

(2)

Q no 7

Min Shear @ Centre.

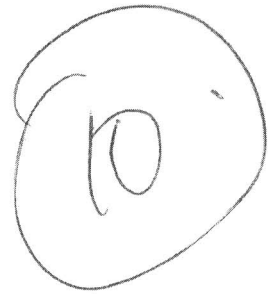
C 22.4.3.1 Pg 48

IS.
1343-1980

$$\frac{A_{sv}}{b \cdot sv} = \frac{0.4}{0.87 f_y}$$

$$\frac{100.53}{150 \times sv} = \frac{0.4}{0.87 \times 415}$$

$$sv = \frac{604.9 \text{ mm}}{2}$$



Also from max spacing conditions. 4x web th.
 max spacing $\leq 0.75 d_e \neq 0.75 \times 255 \neq 4 \times 150$
 $= 191.25 \text{ mm} \neq 600 \text{ mm}$

Consider least value.

At support section provide spacing of 140 mm c/c.
 @ centre span provide spacing @ 190 mm c/c.

