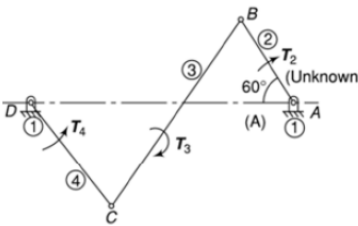
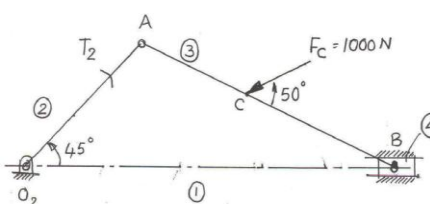


Improvement Test – Nov. 2017

Sub: Dynamics of Machinery	Max				
Date: <u>20/11/2017</u> Duration: <u>90 mins</u>	Marks:	<u>50</u>	Sem:	<u>V</u>	

Code:	15ME52
Branch:	MECH

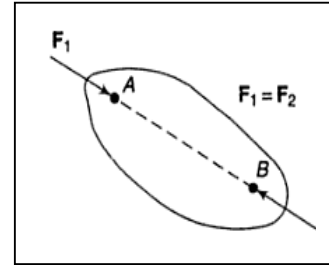
Note: Answer any **five** questions.

	Marks	OBE
		CO RBT
1 State the conditions for the equilibrium of following systems: i. Two force member ii) Three force member iii) Member with two force and torque	10	CO1 L2
2 In a four-link mechanism shown in fig (a), torque T_3 and T_4 have magnitudes of 30 N-m and 20 N-m respectively. The link lengths are $AD = 800$ mm, $AB = 300$ mm, $BC = 700$ mm and $CD = 400$ mm. For the static equilibrium of the mechanism, determine the required input torque T_2	10	CO1 L4
 fig (a)		
 fig (b)		
<small>AC=70mm, AB=150mm, O2A=40mm</small>		
3 Determine torque T_2 to keep the mechanism in equilibrium shown in fig (b).	10	CO1 L3
4 a. With usual notations and diagrams, derive an expression for the gyroscopic couple produced by a rotating disc. b. A disc of 5 kg mass with radius of gyration 70 mm is mounted at span on a horizontal shaft spins at 720 rpm in clockwise direction when viewed from the right hand bearing. If the shaft precesses about the vertical axis at 30 rpm in clockwise direction when viewed from the top, determine the gyroscopic couple.	5	CO3 L2
5 An aeroplane flying at 240 km/hr turns towards left and completes a quarter circle of 60 m radius. The mass of the rotary engine and the propeller of the plane amounts to 450 kg, with a radius of gyration of 320 mm. The engine speed is 2000 rpm clockwise when viewed from the rear. Determine the gyroscopic couple on the aircraft and state its effect. In what way the effect is changed when the aeroplane turns towards right?	10	CO3 L3
6 The turbine rotor of a ship has a mass of 3500 kg. It has a radius of gyration of 0.45 m and a speed of 3000 r.p.m, clockwise when looking from stern. Determine the gyroscopic couple and its effect upon the ship: i. When the ship is steering to the left on a curve of 100 m radius at a speed of 36 km/h. ii. When the ship is pitching in a simple harmonic motion, the bow falling with its maximum velocity. The period of pitching is 40 seconds and the total angular displacement between the two extreme positions of pitching is 12 degrees.	10	CO3 L4

Equilibrium of Two Force Members

A member under the action of two forces will be in equilibrium if

- The forces are of the same magnitude,
- The forces act along the same line, and the forces are in opposite directions



Equilibrium of Three Force Members

A member under the action of three forces will be in equilibrium if

- The resultant of the forces is zero, and
- The lines of action of the forces intersect at a point (known as *point of concurrency*).

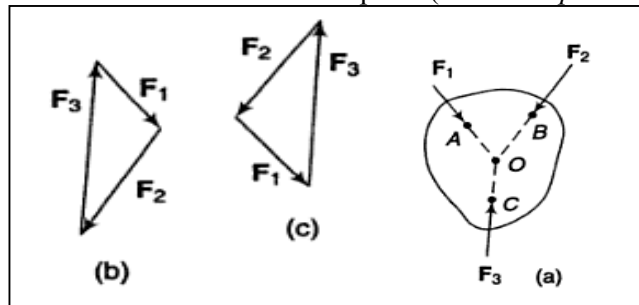


Figure (a) indicates an example for the three force member and (b) and (c) indicates the force polygon to check for the static equilibrium.

Member with two forces and a torque

A member under the action of two forces and an applied torque will be in equilibrium if

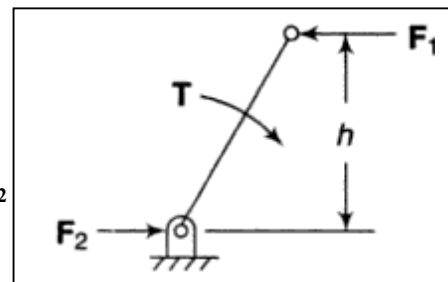
- The forces are equal in magnitude, parallel in direction and opposite in sense and
- The forces form a couple which is equal and opposite to the applied torque.

Figure shows a member acted upon by two equal forces F_1 , and F_2 and an applied torque T for equilibrium,

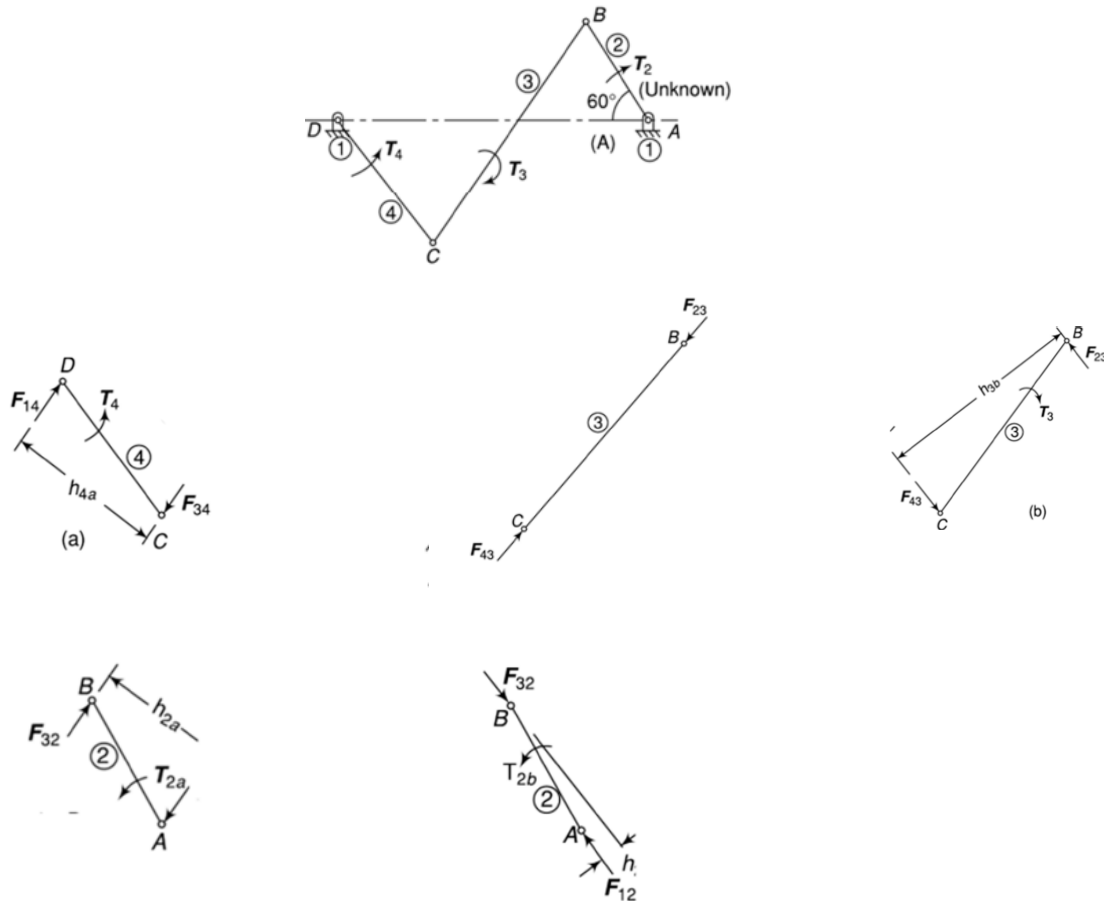
$$T = F_1 h = F_2 h$$

Where T , F_1 and F_2 are the magnitudes of T , F_1 and F_2 respectively.

T is clockwise whereas the couple formed by F_1 , and F_2 is counter-clockwise.



In a four-link mechanism shown in Fig., torque T_3 and T_4 have magnitudes of 30 N-m and 20 N-m respectively. The link lengths are $AD = 800$ mm, $AB = 300$ mm, $BC = 700$ mm and $CD = 400$ mm. For the static equilibrium of the mechanism, determine the required input torque T_2



Neglecting torque T_3

Torque T_4 on the link 4 is balanced by a couple having two equal, parallel and opposite forces at C and D. As the link 3 is a two-force member, F_{43} and therefore, F_{34} and F_{14} will be parallel to BC .

$$F_{34} = F_{14} = \frac{T_4}{h_{4a}} = \frac{20}{0.383} = 52.2 \text{ N}$$

$$\text{and } F_{34} = F_{43} = F_{23} = F_{32} = F_{12} = 52.2 \text{ N}$$

$$T_{2a} = F_{32} \times h_{2a} = 52.2 \times 0.274 = 14.3 \text{ N.m counter-clockwise.}$$

Neglecting torque T_4

F_{43} is along CD . The diagram is self-explanatory.

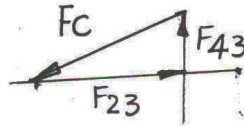
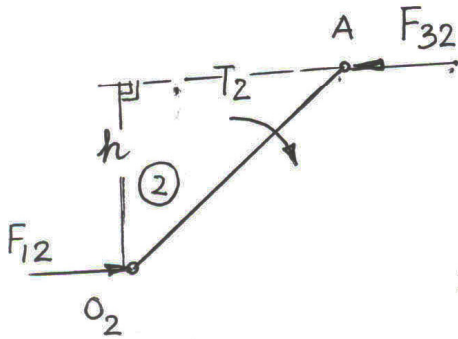
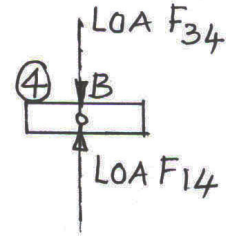
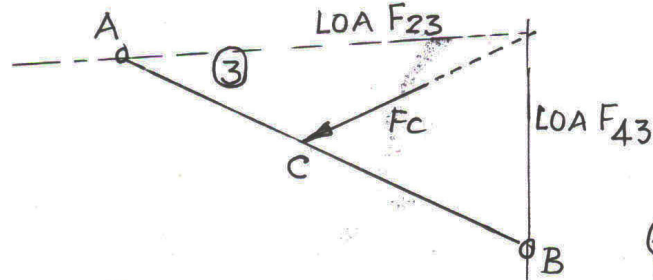
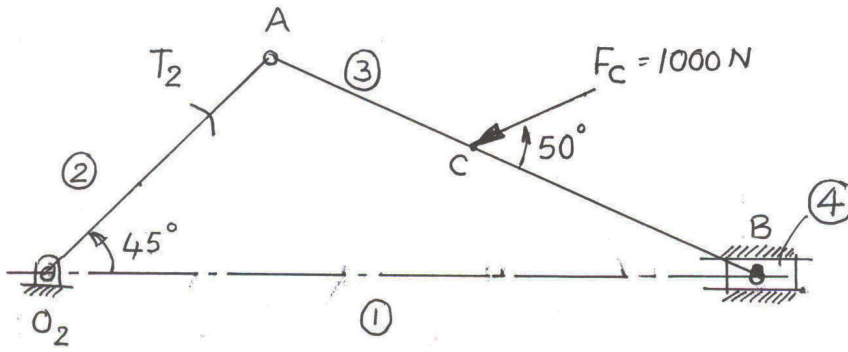
$$F_{43} = F_{23} = \frac{T_3}{h_{3b}} = \frac{30}{0.67} = 44.8 \text{ N} ; \quad F_{23} = F_{32} = F_{12} = 44.8 \text{ N}$$

$$T_2 = T_{2a} + T_{2b} = 14.3 + 1.88 = \underline{16.18 \text{ N}} \text{ Counter clockwise}$$

3

Determine T_2 to keep the mechanism in equilibrium

AC=70mm,
AB=150mm,
O₂A= 40mm



Force triangle for (3)

$$T_2 = F_{32} \times h = F_{12} \times h$$

F_{32} and F_{12} form a CCW couple and hence T_2 acts clock wise.

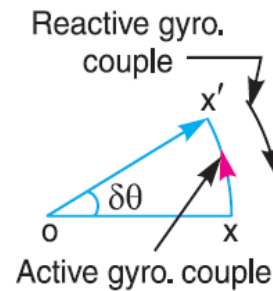
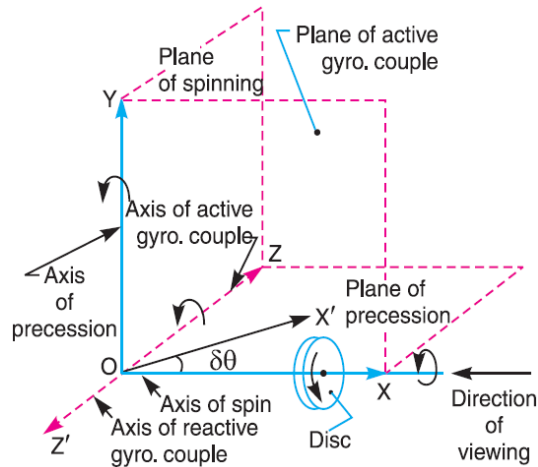
$$F_{23} = 840 \text{ N}; \quad F_{43} = 540 \text{ N}; \quad T_2 = 27.72 \text{ N-m}$$

4.a

Gyroscopic Couple

• Consider a disc spinning with an angular velocity ω rad/s about the axis of spin OX , in anticlockwise direction when seen from the front, as shown in Fig.

• Since the plane in which the disc is rotating is parallel to the plane YOZ therefore it is called plane of spinning.



Let I = Mass moment of inertia of the disc about OX , and

ω = Angular velocity of the disc.

Angular momentum of the disc = $I\omega$

\therefore Change in angular momentum

$$= \vec{OX'} - \vec{OX} = \vec{XX'} = \vec{OX} \cdot \delta\theta \quad \dots(\text{in the direction of } \vec{XX'})$$

$$= I \cdot \omega \cdot \delta\theta$$

and rate of change of angular momentum

$$= I \cdot \omega \times \frac{\delta\theta}{dt}$$

Since the rate of change of angular momentum will result by the application of a couple to the disc, therefore the couple applied to the disc causing precession,

$$C = \lim_{\delta t \rightarrow 0} I \cdot \omega \times \frac{\delta\theta}{\delta t} = I \cdot \omega \times \frac{d\theta}{dt} = I \cdot \omega \cdot \omega_p \quad \dots \left(\because \frac{d\theta}{dt} = \omega_p \right)$$

4. b

Angular velocity:

$$\begin{aligned}\omega &= \frac{2\pi N}{60} = \frac{2\pi \times 720}{60} \\ &= 75.4 \text{ rad/s}\end{aligned}$$

Angular velocity of precession: $\omega_p = \frac{2\pi N_p}{60}$

$$= \frac{2\pi \times 30}{60} = 3.14 \text{ rad/s}$$

Moment of inertia: $I = mk^2$

$$= 5 \times 0.07^2 = 0.0245 \text{ kg m}^2$$

Gyroscopic couple: $C = I \omega \omega_p$

$$\begin{aligned}&= 0.0245 \times 75.4 \times 3.14 \\ &= 5.8 \text{ Nm}\end{aligned}$$

5.

Given : $R = 60 \text{ m}$; $v = 240 \text{ km/hr} = \frac{240 \times 1000}{3600} = 66.67 \text{ m/s}$; $m = 450 \text{ kg}$; $k = 0.32 \text{ m}$

$N = 2000 \text{ r.p.m.}$ or $\omega = 2\pi N/60 = 2\pi \times 2000/60 = 209.43 \text{ rad/s}$

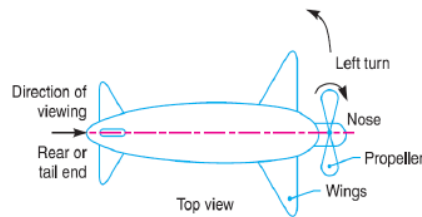
Mass moment of inertia of the rotor, $I = m k^2 = 450 (0.32)^2 = 46.08 \text{ kg-m}^2$

Angular velocity of precession, $\omega_p = \frac{v}{R} = \frac{66.67}{60} = 1.11 \text{ rad/s}$

Gyroscopic couple, $C = I \omega \omega_p = 46.08 \times 209.43 \times 1.11 = 10712.09 \text{ N-m}$

Effect

When the aero-plane turns towards left, the effect of the gyroscopic couple is to lift the nose upwards and tail downwards.



When the engine or propeller rotates in clockwise direction when viewed from the rear or tail end and the aeroplane takes a right turn, the effect of the reactive gyroscopic couple will be to dip the nose and raise the tail of the aeroplane.

6.

Given: $m = 3500 \text{ kg}$; $k = 0.45 \text{ m}$;

$N = 3000 \text{ r.p.m.}$ or $\omega = 2\pi \times 3000/60 = 314.2 \text{ rad/s}$

i. *When the ship is steering to the left*

Given: $R = 100 \text{ m}$; $v = \text{km/h} = 10 \text{ m/s}$

Mass moment of inertia of the rotor, $I = m k^2 = 3500 (0.45)^2 = 708.75 \text{ kg-m}^2$

Angular velocity of precession, $\omega_p = \frac{v}{R} = \frac{10}{100} = 0.1 \text{ rad/s}$.

Gyroscopic couple, $C = I \omega \omega_p = 708.75 \times 314.2 \times 0.1 = 22\,270 \text{ N-m} = 22.27 \text{ kN-m}$.

ii. *When the ship is pitching with the bow falling*

Given: $t_p = 40 \text{ s}$

Total angular displacement between the two extreme positions of pitching is 12° (i.e. $2\phi = 12^\circ$), therefore amplitude of swing,

$\phi = 12/2 = 6^\circ$; $6^\circ = \frac{6 \times \pi}{180} = 0.105 \text{ rad}$

Angular velocity of the simple harmonic motion,

$$\omega_1 = \frac{2\pi}{t_p} = \frac{2\pi}{40} = 0.157 \text{ r/s}$$

Maximum angular velocity of precession,

$$\omega_p = \phi \omega_1 = 0.105 \times 0.157 = 0.0165 \text{ rad/s}$$

Gyroscopic couple, $C = I \omega \omega_p$

$$= 708.75 \times 314.2 \times 0.0165 = 3675 \text{ N-m} = 3.675 \text{ kN-m}$$

When the bow is falling (i.e. when the pitching is downward), the effect of the reactive gyroscopic couple is to **move the ship towards port side**.

