

Solutions for IAT 1 Question paper

Sem: V

Sections: A & B

Sub: DME I

Subcode: 15ME54

Staff: RPR.

- 1 (a) A machine element in the form of a cantilever, supported at ^{one} end and carrying a lateral load of 60 kN is 0.8 m long. The cross section is rectangular with its depth equal to thrice its width. The deflection is limited to 2 mm at the loading end. If the allowable stress in the material is 80 MPa, design the section. Take $E = 200 \text{ GPa}$.

Soln. data

$$F = 60 \text{ kN}$$

$$l = 800 \text{ mm}$$

$$d = 3b$$

$$y_{\text{max}} = 2.0 \text{ mm}$$

$$\sigma_d = 80 \text{ MPa}$$

$$E = 200 \times 10^3 \text{ N/mm}^2$$

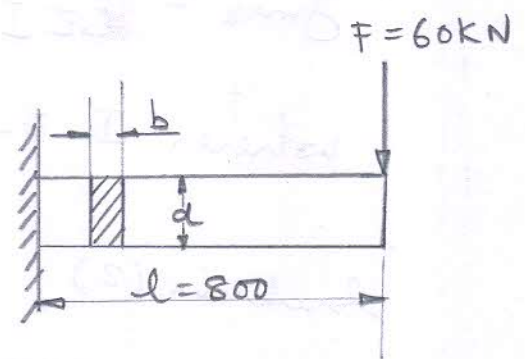
to find

b & d.

- (i) c/s dimensions limiting the stress:

$$\sigma_b = \frac{M_b}{z_b} \quad \text{--- (1)}$$

where $M_b = Fl$ (T2.8 / P2.34).



$$z_b = \frac{bh^2}{6} \quad (\text{T2.7/P2.33}) \quad (2)$$

$$\begin{aligned} \therefore M_b &= 60 \times 10^3 \times 800 \\ &= 48 \times 10^6 \text{ N-mm} \end{aligned}$$

$$z_b = \frac{bh^2}{6} = \frac{b(3b)^2}{6} = \frac{9b^3}{6} = \frac{3b^3}{2} \text{ mm}^3$$

Sub in (1),

$$80 = \frac{48 \times 10^6}{\left(\frac{3b^3}{2}\right)}$$

$$\Rightarrow b = 73.68 \text{ mm}$$

ii) c/s dimensions limiting the deflection

$$y_{\max} = \frac{Fl^3}{3EI} \quad (2) \quad (\text{T2.8/P2.34})$$

$$\text{where } I = \frac{bd^3}{12} \quad (\text{T2.7/P2.33})$$

Sub in (2),

$$2 = \frac{60 \times 10^3 \times 800^3 \times 12}{3 \times 200 \times 10^3 \times b(3b)^3}$$

$$\Rightarrow b = 58.07 \text{ mm}$$

Selecting the higher value for b , select $b = 74 \text{ mm}$
 $\therefore d = 222 \text{ mm}$

- b) A bracket shown in figure is subjected to a pull of 15 kN at 60° to the vertical. Det. the max. tensile stress in the bracket. (3)

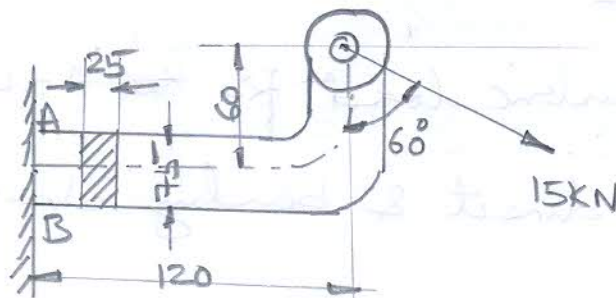
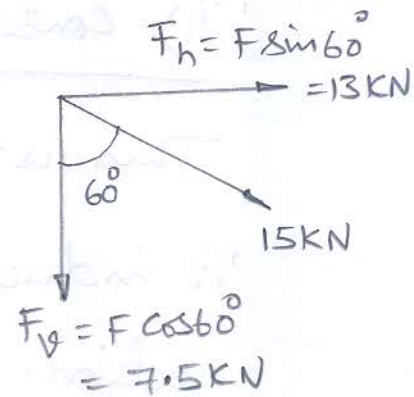


Fig 1(b)



data

$$b = 25 \text{ mm}$$

$$h = 75 \text{ mm}$$

$$A = 1875 \text{ mm}^2$$

to find

Max. tensile stress in the bracket.

In fig 1.B, AB is the critical section.

i) consider F_v

This force produces B.M in section A-B.

$$\sigma_{b1} = \frac{M_b}{z_b} \quad \text{--- (1)}$$

$$\begin{aligned} \text{where } M_b &= F_v \times 120 \\ &= 7.5 \times 10^3 \times 120 \\ &= 9 \times 10^5 \text{ N-mm} \end{aligned}$$

$$z_b = \frac{bh^2}{6} = \frac{25 \times 75^2}{6} = 23.43 \times 10^3 \text{ mm}^3$$

$$\begin{aligned} \text{Sub in (1),} \\ \therefore \sigma_{b1} &= \frac{9 \times 10^5}{23.43 \times 10^3} = 38.41 \text{ N/mm}^2 \end{aligned}$$

$$(\sigma_{b1})_A = 38.41 \text{ N/mm}^2 \quad (4)$$

$$\& (\sigma_{b1})_B = -38.41 \text{ N/mm}^2$$

ii) consider F_h :

This is an eccentric load for sec A-B. Hence, it induces both direct & bending stresses in the section.

$$\sigma_T = \frac{F_h}{A} = \frac{13 \times 10^3}{25 \times 75} = 6.93 \text{ N/mm}^2$$

$$\sigma_{b2} = \frac{M_b}{z_b} = \frac{F_h \cdot e}{\left(\frac{bh^2}{6}\right)} = \frac{13 \times 10^3 \times 60}{\left(\frac{25 \times 75^2}{6}\right)} = 33.28 \text{ N/mm}^2.$$

$$(\sigma_{b2})_A = 33.28 \text{ N/mm}^2$$

$$(\sigma_{b2})_B = -33.28 \text{ N/mm}^2.$$

\therefore Max. tensile stress in section A-B

$$= \sigma_{b1} + \sigma_T + \sigma_{b2}$$

$$= 38.41 + 6.93 + 33.28$$

$$= 78.62 \text{ N/mm}^2 \quad (\text{at A of sec A-B}).$$

2(a)

A rod of circular section is to sustain a torsional moment of 300 kN-m and a bending moment of 200 kN-m . Selecting C45 steel ($\sigma_y = 353 \text{ MPa}$) and assuming a F.S of 3, determine the dia. of rod as per the following theories of failure. (5)

- i) Max. Shear stress theory
- ii) Distortion energy theory
- iii) Total energy theory

Ans: data

$$M_t = 300 \times 10^3 \text{ N-m}$$

$$= 300 \times 10^6 \text{ N-mm}$$

$$M_b = 200 \times 10^6 \text{ N-mm}$$

$$\sigma_y = \sigma_e = 353 \text{ N/mm}^2$$

$$n = 3$$

to find
 $d = ?$

$$\text{Torsional Shear stress } (\tau) = \frac{M_t}{Z_t}$$

$$= \frac{M_t}{\left(\frac{\pi d^3}{16}\right)}$$

$$= \frac{300 \times 10^6 \times 16}{\pi d^3}$$

$$= \left(\frac{1.527 \times 10^9}{d^3}\right) \text{ N/mm}^2$$

$$\text{Bending stress } (\sigma_b) = \frac{M_b}{Z_b}$$

$$= \frac{200 \times 10^6 \times 32}{\pi d^3}$$

$$= \left(\frac{2.037 \times 10^9}{d^3}\right) \text{ N/mm}^2$$

$$\therefore \text{Max. principal stress } (\sigma_1) = \frac{\sigma_b}{2} + \sqrt{\left(\frac{\sigma_b}{2}\right)^2 + \tau^2} \quad (1)$$

$$= \frac{(2.854 \times 10^9)}{d^3} \text{ N/mm}^2$$

$$\text{Min. principal stress } (\sigma_2) = \frac{\sigma_b}{2} - \sqrt{\left(\frac{\sigma_b}{2}\right)^2 + \tau^2} \quad (6)$$

$$= \frac{-(0.817 \times 10^9)}{d^3} \text{ N/mm}^2$$

(i) Max. shear stress theory

$$\sigma_1 - \sigma_2 = \frac{\sigma_e}{n}$$

$$\frac{(2.854 + 0.817) \times 10^9}{d^3} = \frac{353}{2}$$

$$\Rightarrow d = 314.83 \text{ mm}$$

ii) Distortion energy theory

$$\sqrt{\sigma_1^2 + \sigma_2^2 - \sigma_1 \sigma_2} = \frac{\sigma_e}{n}$$

$$\Rightarrow d = 305 \text{ mm}$$

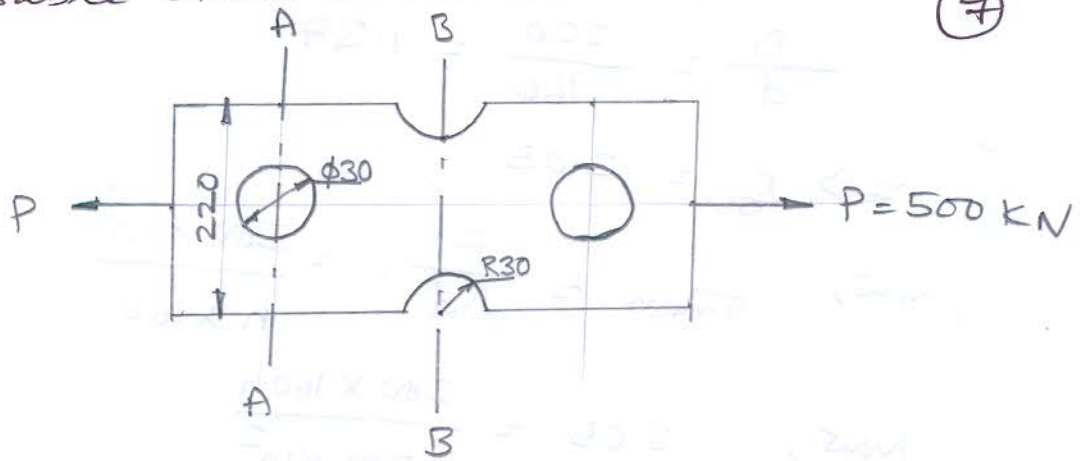
iii) Max. total energy theory

$$\sqrt{\sigma_1^2 + \sigma_2^2 - 2\nu \sigma_1 \sigma_2} = \frac{\sigma_e}{n}$$

assuming $\nu = 0.3$ for steel,

$$d = 300.58 \text{ mm}$$

2(b) A bar of rectangular section is subjected to an axial pull of 500 kN. Calculate the thickness if the allowable stress in the bar is 200 MPa. (7)



Ans: 1) Consider sec A-A

Refer Fig 4.5

$$d = 30 \text{ mm}$$

$$w = 220 \text{ mm}$$

$$\sigma_{\text{max}} = 200 \text{ N/mm}^2$$

$$\therefore \frac{d}{w} = 0.136$$

$$\Rightarrow K_f = 2.65$$

$$\sigma_{\text{nom}} = \frac{F}{(w-d)h} = \frac{500 \times 10^3}{(220-30)h} = \frac{500 \times 10^3}{190h}$$

$$\text{Now } K_f = \frac{\sigma_{\text{max}}}{\sigma_{\text{nom}}}$$

$$2.65 = \frac{200}{500 \times 10^3} \times 190h$$

$$\Rightarrow h = 34.86 \text{ mm}$$

2) Consider section B-B

Refer Fig 4.22A / P4.21.

$$r = 30 \text{ mm}$$

$$D = 220 \text{ mm}$$

$$d = 220 - 60 = 160 \text{ mm.}$$

(8)

$$\frac{r}{d} = \frac{30}{160} = 0.18$$

$$\frac{D}{d} = \frac{220}{160} = 1.37$$

$$\Rightarrow K_f = 2.05$$

$$\text{Now, } \sigma_{nom} = \frac{F}{hd} = \frac{500 \times 10^3}{h \times 160}$$

$$\text{Now, } 2.05 = \frac{200 \times 160h}{500 \times 10^3}$$

$$\Rightarrow h = 32.03 \text{ mm.}$$

Selecting the higher value of the above two,
select $h = 35 \text{ mm.}$

3(a) A steel rod is 1.5 m long. It has to resist longitudinally an impact of 2.5 kN falling under gravity at a velocity of 0.99 m/sec. Maximum computed stress is limited to 150 MPa. Design the dia. of rod. Take $E = 206.8 \text{ GPa.}$

Ans: data

$$L = 1500 \text{ mm.}$$

$$W = 2.5 \text{ kN}$$

$$V = 0.99 \text{ m/sec.}$$

$$\sigma_i = 150 \text{ N/mm}^2$$

$$E = 206.8 \times 10^3 \text{ N/mm}^2.$$

to find

$$d = ?$$

'd' is determined by equating Resilience of rod to K.E of mass. (9)

$$\left(\frac{\sigma_u^2}{2E}\right) \times V = \frac{1}{2} m v^2 \times 10^3$$

$$\left(\frac{150^2}{2 \times 206.8 \times 10^3}\right) \times \left(\frac{\pi d^2}{4} \times 1500\right) = \frac{1}{2} \times \frac{2500}{9.81} \times 0.99^2 \times 10^3$$

Solving $d = 44.14 \text{ mm}$
 $\approx 45 \text{ mm}$

3(b) A cantilever beam of span 800 mm has a rectangular c/s of depth 200 mm. The free end of beam is subjected to a transverse load of 1 kN that drops onto it from a height of 40 mm. Selecting C40 steel ($\sigma_y = 328.6 \text{ MPa}$), & F.S. = 3, determine the width of rectangular section. Take $E = 206.8 \text{ GPa}$.

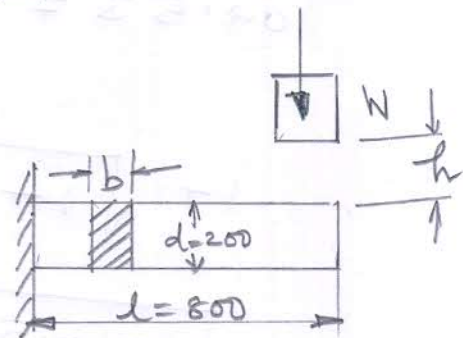
Ans: data

$l = 800 \text{ mm}$

$d = 200 \text{ mm}$, $n = 3$

$W = 1 \text{ kN}$

$h = 40 \text{ mm}$



$$\sigma_{bi} = \frac{\sigma_y}{FS} = \frac{328.6}{3} = 109.53 \text{ N/mm}^2$$

to find
 $b = ?$

$$\sigma_{bi} = (\sigma_b)_{st} \left[1 + \sqrt{1 + \frac{zh}{s_{st}}} \right] \quad \text{--- (1)} \quad (10)$$

$$\begin{aligned} (\sigma_b)_{st} &= \frac{M_b}{z_b} = \frac{Fl}{\left(\frac{bd^2}{6}\right)} \\ &= \frac{6 \times Fl}{b \times 200^2} \\ &= \left(\frac{120}{b}\right) \text{ N/mm}^2 \quad \text{--- (2)} \end{aligned}$$

$$\begin{aligned} \text{Now } y &= \frac{Fl^3}{3EI} \\ &= \frac{1 \times 10^3 \times 800^3 \times 12}{3 \times 206.8 \times 10^3 \times b \times 200^3} \\ &= \frac{1.24}{b} \quad \text{--- (3)} \end{aligned}$$

Sub (2) & (3) in (1).

$$109.53 = \frac{120}{b} \left[1 + \sqrt{1 + \frac{2 \times 40 b}{1.24}} \right]$$

$$1 + \sqrt{1 + 64.51b} = 0.912b.$$

$$\sqrt{1 + 64.51b} = (0.912b - 1)$$

Squaring on both sides,

$$1 + 64.51b = 0.831b^2 - 1.824b + 1$$

$$\text{ie } 0.831b^2 - 66.33b = 0$$

$$\Rightarrow b = 79.82 \text{ mm say } 80 \text{ mm.}$$