	CBCS Scheme
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USN	D5CS36
	Third Samestar R F Dagree Everningtion Dec 2017/1- 2019
Third Semester B.E. Degree Examination, Dec.2017/Jan.2018	
	Discrete Mathematical Structures
Time	: 3 hrs. Max. Marks: 80
Note: Answer any FIVE full questions, choosing	
	ONE full question from each module.
	Module-1
1 a	the state of the propositions p, q, I [I r(q/I)] = ([p] r q)/ (p - r)]. Using that
h	table. (05 Marks)
U	Establish the validity of the argument: p → q
	$q \to (r \land s)$
	$\exists r \lor (\exists t \lor u)$
	pht
	∴ u (06 Marks)
C.	Prove that for all integers 'k' and 'l', it's and 'l' are both odd, then k + l is even and kl is
	odd by direct proof. (05 Marks)
	SOP S
2 a.	Determine the truth value of each of the following quantified statements; the universe being
	the set of all non - zero integers. (05 Marks)
	i) $\exists x, \exists y [xy = 1]$
	ii) $\exists x, \forall y [xy = 1]$
	iii) $\forall x, \exists y, [xy = 1]$ BANGALORE - 560 037
	$A_{\lambda} = A_{\lambda} = A_{\lambda$
b.	v) $\exists x, \exists y [(3x - y = 17), (2x + 4y = 3)].$ (06 Marks) Find whether the following arguments are valid or not for which the universe is set of all
0.	triangles. In triangle XYZ, there is no pair of angles of equal measure. If the triangle has two
	sides of equal length, then it is isosceles. If the triangle is isosceles, then it has two angles of
	equal measure. Therefore triangle XYZ has no two sides of equal length (05 Marks)
C.	
	propositions p_s , s for which the truth value of following compound proposition is 1. $[q \rightarrow \{(\neg p) \land p \land \neg s\}] \land \{\neg s \rightarrow (\neg r \land q)\}.$ (05 Marks)
	$[q \to \{(\neg p \lor r) \land \neg s\}] \land \{\neg s \to (\neg r \land q)\}. \tag{05 Marks}$
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Module-2

Prove by mathematical induction that, for every positive integer n, 5 divides n⁵

For the Fibonacci sequence F_0 , F_1 , F_2 - - - - prove that $F_n = \frac{1}{\sqrt{5}} \left[\left(\frac{1+\sqrt{5}}{2} \right)^n - \left(\frac{1-\sqrt{5}}{2} \right)^n \right]$

(06 Marks)

- Find the coefficient of: i) x^9y^3 in the expansion $(2x-3y)^{12}$ ii) x^{12} in the expansion $x^3(1-2x)^{10}$.

(05 Marks)

2 of 3

Module-4

- 7 a. Out of 30 students in a hostel; 15 study history 8 study economics and 6 study geography. It is known that 3 students study all these subjects. Show that 7 or more students study none of these subjects. (05 Marks)
 - b. Five teachers T₁, T₂, T₃, T₄, T₅ are to be made class teachers for five classes C₁, C₂, C₃, C₄, C₅, one teacher for each class. T₁ and T₂ do not wish to become the class teachers for C₁ or C₂, T₃ and T₄ for C₄ or C₅ and T₅ for C₃ or C₄ or C₅. In how many ways can the teachers be assigned work without displeasing any teacher. (06 Marks)
 - c. Solve the recurrence relation $a_n-6a_{n-1}+9a_{n-2}=0$ form $n\geq 2$.

(05 Marks)

OR

- 8 a. Solve the recurrence relation $a_n 3a_{n-1} = 5 \times 3^n$ for $n \ge 1$ given that $a_0 = 2$. (05 Marks)
 - b. Let a_n denote the number of n-letter sequences that can be formed using the letters A, B and C such that non terminal A has to be immediately followed by a B. Find the recurrence relation for a_n and solve it.

 (06 Marks)
 - c. Find the number of permutations of English letters which contain exactly two of the pattern car, dog, pun, byte. (05 Marks)

Module-5

9 a. Discuss Konigsberg bridge problem.

(05 Marks)

- b. Let G = G(V, E) be a simple graph with m edges and 'n' vertices. Then prove that :
 - i) $m \le \frac{1}{2}n(n-1)$
 - ii) For a complete graph k_n , $m = \frac{1}{2}n(n-1)$ edges

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iii) How many vertices and edges are there for K_{4.7} and K_{7, 11}.

(06 Marks)

c. Merge sort the list -1, 7, 4, 11, 5, -8, 15, -3, -2, 6, 10, 3.

(05 Marks)

OR

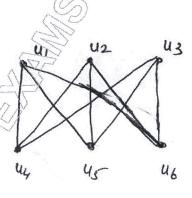
10 a. Prove that a tree with 'n' vertices has n-1 edges.

(05 Marks)

- b. Obtain an optimal prefix code for the message LETTER RECEIVED indicate the code and weight.

 (06 Marks)
- c. Determine whether the following graphs are isomorphic or not.

(05 Marks)



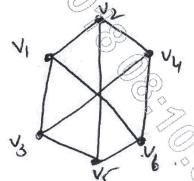


Fig.Q10(c)

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